# NATIONAL RADIO ASTRONOMY OBSERVATORY SOCORRO, NEW MEXICO VERY LARGE ARRAY PROGRAM

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GAS TIGHT WAVEGUIDE WINDOWS FOR THE VLA WAVEGUIDE SYSTEM

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#### 1.0 INTRODUCTION

The circular TE node waveguide used in the VLA signal distribution and communication system is subject to environmental effects not experienced in other areas of the system. Due to the direct burial technique employed in the installation of the 60 mm diameter main trunk waveguide and the consequent deep manholes at each antenna station for coupler placement, the main guide is susceptible to water seepage and corrosion which can seriously impair the transmission performance. To overcome these possible problems the waveguide system is pressurized to 2 psi above normal atmospheric pressue with dry nitrogen in order to create a positive pressure against fluid penetration. To contain the gas and yet permit low loss, low reflection signal transmission with minimal spurious mode generation in the overmoded circular (20 mm diameter) antenna waveguide, high performance, gas tight waveguide windows are required. This report describes the design, construction and performance of the windows presently used in the VLA waveguide network.

## 2.0 THEORETICAL ANALYSIS

The windows used to seal the VLA waveguide are mechanically simple in concept, comprising two thin sheets of dielectric material clamped in a metal holder and spaced approximately 1/4 of a guide wavelength apart. The performance of such a structure

can be analyzed in the following manner. Consider an air/dielectric interface in circular waveguide as shown in Figure 1.



#### FIGURE 1

Consider an incident  $TE_{01}$  mode; the only possible higher order modes which should be considered are the  $TE_{0n}$  modes (by symmetry considerations). Let  $\underline{e}_i$ ,  $\underline{h}_i$  represent the electric and magnetic fields of the i<sup>th</sup> mode in Region 1, and  $\underline{e}'_i$ ,  $\underline{h}'_i$  the electric and magnetic fields of the same mode in Region 2. Then, if  $R_i$ ,  $T_{i12}$ represent the non-normalized reflection and transmission coefficients for the i<sup>th</sup> mode, by continuity

$$\underline{\mathbf{e}}_{\mathbf{i}} + \underbrace{\sum_{n=1}^{\infty} \mathbf{R}_{n} \mathbf{e}_{n}}_{n=n} = \underbrace{\sum_{n=1}^{\infty} \mathbf{T}_{n}}_{12} \underline{\mathbf{e}}_{n}^{\mathbf{i}}$$
$$\underline{\mathbf{h}}_{\mathbf{i}} - \underbrace{\sum_{n=1}^{\infty} \mathbf{R}_{n}}_{n=n} = \underbrace{\sum_{n=1}^{\infty} \mathbf{T}_{n}}_{12} \underline{\mathbf{h}}_{n}^{\mathbf{i}}$$

Defining

$$(\underline{e}_{i}, \underline{h}_{j}) = \iint_{S} (\underline{e}_{i} \times \underline{h}_{j}^{*}) \cdot i_{z} ds$$

there result

$$(\underline{e}_{i},\underline{h}_{i}') + \sum_{n=1}^{\infty} R_{n}(\underline{e}_{n},\underline{h}_{i}') = \sum_{n=1}^{\infty} T_{n}(\underline{e}_{n},\underline{h}_{i}')$$
$$(\underline{e}_{i}',\underline{h}_{i}) - \sum_{n=1}^{\infty} R_{n}(\underline{e}_{i}',\underline{h}_{n}) = \sum_{n=1}^{\infty} T_{n}(\underline{e}_{i}',\underline{h}_{n}')$$

For the TE modes

$$(\underline{e}_{i}, \underline{h}_{j}) = 0 \quad \forall \quad i \neq j$$
$$= \frac{\pi \omega \mu a^{2} B_{oi}^{2}}{k_{oi}^{2}} \beta_{oi} J_{o}^{2} (k_{oi}^{a}) \quad \text{if } i = j$$

where B is a normalization constant

 $\beta_{oi}$  is the waveguide propagation constant for the i<sup>th</sup> mode in Region 1. ( $\beta_{oi}$  in Region 2).  $k_{oi}$  is the i<sup>th</sup> root of J'( $\chi$ )=0. Similarly

$$(\underline{e}_{i}, \underline{h}_{j}^{i}) = 0 \quad \forall \quad i \neq j$$

$$= \frac{\pi \omega \mu a^{2B} o^{2}}{k_{oi}^{2}} \beta_{oi} \cdot J_{o}^{2}(k_{oi}a) \quad \text{if } i = j$$

$$(\underline{e}_{i}^{i}, \underline{h}_{j}) = 0 \quad \forall \quad i \neq j$$

$$= \frac{\pi \omega \mu a^{2B} o^{2}}{k_{oi}^{2}} \beta_{oi} \cdot J_{o}^{2}(k_{oi}a) \quad \text{if } i = j$$

Thus the continuity equations reduce to

$$1 + R_{1} = T_{1} \qquad \frac{\beta_{01}}{\beta_{01}} (1 - R_{1}) = T_{1} \qquad (i)$$

$$R_{i} \delta_{0i} = T_{i} - R_{i} \delta_{0i} = T_{i}$$
(ii)  
chosen so that  $(\underline{e}_{i}, \underline{h}_{j}) = \delta_{ij}$ 

where B was chosen so that  $(\underline{e}_i, \underline{h}_j) =$ From equations (ii), it follows

$$T_{i_{12}} = R_{i} = 0$$

Hence

$$R_{1} = \frac{\beta_{01} - \beta_{01}}{\beta_{01} + \beta_{01}} = R$$

and the unnormalized transmission coefficient

$$\mathbf{T}_{1_{12}} = \frac{2\beta_{01}}{\beta_{01} + \beta_{01}}$$

Note that, theoretically, no spurious higher order modes should be excited at the interface.

Similarly,

$$R_{1}' = \frac{\beta_{01}' - \beta_{01}}{\beta_{01}' + \beta_{01}} = -R$$
$$T_{1_{12}} = \frac{2\beta_{01}'}{\beta_{01}' + \beta_{01}}$$

The normalized transmission coefficients are given by

$$\mathbf{T} = \left(\frac{\mathbf{T}_{12} \mathbf{T}_{12}}{\left(\frac{\beta_{01}}{\beta_{01}}\right)}\right)^{\frac{1}{2}} = \frac{2\sqrt{\beta_{01}\beta_{01}}}{\left(\beta_{01} + \beta_{01}\right)}$$

Let  $a_1$ ,  $b_1$  be the amplitudes of the forward and reverse traveling waves in Region 1;  $a_2$ ,  $b_2$  be the amplitudes in Region 2. Thus

$$\begin{bmatrix} a_{1} \\ b_{1} \end{bmatrix} = \frac{1}{T_{1}} \begin{bmatrix} 1 & -R_{1}' \\ R_{1} & \frac{T_{1}}{12} \frac{1}{12} \end{bmatrix} \begin{bmatrix} a_{2} \\ b_{2} \end{bmatrix} = \frac{1}{T_{1}} \begin{bmatrix} 1 & R \\ R & 1 \end{bmatrix} \begin{bmatrix} a_{2} \\ b_{2} \end{bmatrix}$$

For a dielectric sheet of thickness t, the transmission matrix is

$$\begin{bmatrix} a_1 \\ b_1 \end{bmatrix} = \frac{1}{T_1} \begin{bmatrix} e^{j\beta_{01}t} & Re^{-j\beta_{01}t} \\ Re^{j\beta_{01}t} & e^{-j\beta_{01}t} \end{bmatrix} \begin{bmatrix} 1 & -R \\ -R & 1 \end{bmatrix} \begin{bmatrix} a_3 \\ 0 \end{bmatrix}$$

where  $a_3$  is the amplitude of the wave transmitted beyond the sheet. Then the reflection coefficient at the sheet in Region 1 is

$$S_{11} = \frac{R[e^{j\beta_{01}t} - e^{-j\beta_{01}t}]}{e^{j\beta_{01}t} - R^2e^{-j\beta_{01}t}}$$

and the transmission coefficient is

$$S_{12} = \frac{(1-R^2) e^{-j\beta_{01}t}}{1-R^2 e^{-2j\beta_{01}t}}$$

Similarly, for the double waveguide window, where the separation between the corresponding surfaces of the sheets is  $\ell$ , the total reflection coefficient is given by (to third order in R)

$$s_{11} = \frac{R\{(1-e^{-2j\beta_{01}t})[(1-R^{2}\cos(2\beta_{01}t)(1+e^{2j\beta_{01}\ell})-4R^{2}\sin^{2}(\beta_{01}t)(1+e^{-2j\beta_{01}\ell})]\}}{1-2R^{2}\cos(2\beta_{01}t)-8R^{2}\sin^{2}(\beta_{01}t)\cos(2\beta_{01}\ell)}$$

$$+ \frac{\{R^{2}(1-e^{2j\beta_{01}t})(1+e^{-2j\beta_{01}\ell})\}}{1-2R^{2}\cos(2\beta_{01}t)-8R^{2}\sin^{2}(\beta_{01}t)\cos(2\beta_{01}\ell)}$$

and the transmission coefficient by

$$S_{12} = \frac{(1-\beta)e^{-j\beta_{01}\ell}}{1-\beta e^{-2j\beta_{01}\ell}}$$

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where

$$\beta = \frac{4R^2 \sin^2(\beta_{01}t)}{2R^2 - e^{2j\beta_{01}t}}$$

The theoretical return loss as a function of frequency in waveguide channels 5 and 11 is plotted in Figures 2, 3 and 4 for a range of window material dielectric constants and thicknesses. It is clear that reducing the thickness of the dielectric broadens the bandwidth of the response, as does a decrease in dielectric constant. Furthermore, the bandwidth of the return loss response can be expected to remain approximately a constant percentage of the center frequency of the window - about 6% of the center frequency for a return loss of greater than -40 dB for  $\varepsilon_r = 3.0$ , t = 0.003" and about 12% of the center frequency for  $\varepsilon_r = 2.0$ , t = 0.003". It is clear that, with judicious choice of dielectric constant and thickness, a window can be designed to operate with low reflection in a number of waveguide channels, especially at the higher frequencies.

# 3.0 SYSTEM CONSIDERATION

The tolerated degradation in return loss is determined by the effect on the transmission response of the waveguide distribution system. If there exists two sources of reflection in the 20 mm diameter antenna waveguide, one source being the mismatch at the coupler coupled port and the other being the combined, almost coplanar, modem mismatch and waveguide window reflection, then the ripple in the waveguide amplitude response due to these reflection sources will have a period of approximately 3.75 MHz and a peak-topeak amplitude given by

$$A_{pp} = \frac{1 - \rho_{c} \rho_{m} e^{-2\alpha_{0} l \ell_{a}}}{1 + \rho_{m} \rho_{c} e^{-2\alpha_{0} l \ell_{a}}}$$

where  $\rho_c$ ,  $\rho_m$  are the coupler and modem/window reflection coefficients, respectively.  $\alpha_{01}$  is the TE<sub>01</sub> mode attenuation coefficient in the 20 mm

diameter antenna waveguide ( $\sim 0.1 \text{ dB/meter}$ ). l is the distance between reflection sources ( $\sim 40 \text{ meters}$ ).

Typically, A is required to be less than 1% of the overall average waveguide loss. Furthermore,  $\rho_c$  is found experimentally to be 0.1259, thus

is required for a peak-to-peak ripple of less than 1%. In terms of return loss

$$R_{m}$$
 > 18 dB.

The return loss of the modem by itself is of the order of 25 dB, so the window must not degrade the return loss by more than 7 dB. The worst case window return loss allowable (reflected signals in phase) is then  $23 \cdot 5$  dB. The criterion for application of a given window in a certain waveguide channel will be that the return loss in that channel should be greater than 35 dB, resulting in a maximum peak-to-peak ripple of 0.75%.

### 4.0 MECHANICAL DESIGN

The window is designed to interface with the standard 20 mm waveguide flange used throughout the VLA system. As shown in Figure 5 through 8, it is comprised of three major sections - two clamping flanges and a spacer of accurately determined thickness. The flanges and spacer are held together, as shown in Figure 8, by counter-sink screws, clamping the mylar dielectric material  $(\varepsilon_r = 2.6, t = 0.003")$  in the recess provided. The structure is rendered gas tight by the two '0' ring seals between flanges and spacer. The optimum spacer thickness for a given waveguide channel is indicated in the table in Figure 5.









#### 5.0 PERFORMANCE

After assembly, the return loss of each waveguide window for channels 1 through 9 was measured using the test configuration indicated in Figure 9. The measured responses are shown in Figures 9 through 17. In each plot, the reference trace indicates the return loss of a standard waveguide termination inserted following the window. Hence, the return loss of the window is approximately given by the difference in loss between the traces with and without the window in position. It can be seen that the windows perform adequately for the design channel and that the higher frequency devices (channels 5 through 9) are capable of covering at least two waveguide bends.

The maximum withstandable pressure differential has been tested on two production windows, and in both cases no rupture was observed for pressures up to 60 psi. Clearly, there exists an adequate safety margin, since the envisaged operating pressure is no more than 20 psi.

In order to investigate the effect on electrical performance of distortion of the mylar window material at high pressure gradients, the return loss was measured before and after pressurization to 60 psi (for a channel 5 window). As can be seen from Figures 18-19 the observed performance degradation is sufficiently small to be of little significance under normal operating condition. The magnitude of the  $TE_{02}$  mode generated by the device, with a  $TE_{01}$  mode incident, was measured and was found to be at least 35 dB below the transmitted  $TE_{01}$  power level in any given channel.

\*These measurements were made with the window unpressurized.

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FIGURE 10

CHANNEL TWO (0.1084 "SAICER)

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FIGURE 11





CA4

FIGURE 12





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FILURE 17

CHANNEL HINE (0.0633" SPACER)



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FIGURE 19

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