

Interoffice

# National Radio Astronomy Observatory

## Very Large Array

November 21, 1983

To: J. Findlay, H. Hvatum, P. Napier, G. Peery, T. Legg

From: W. Horne

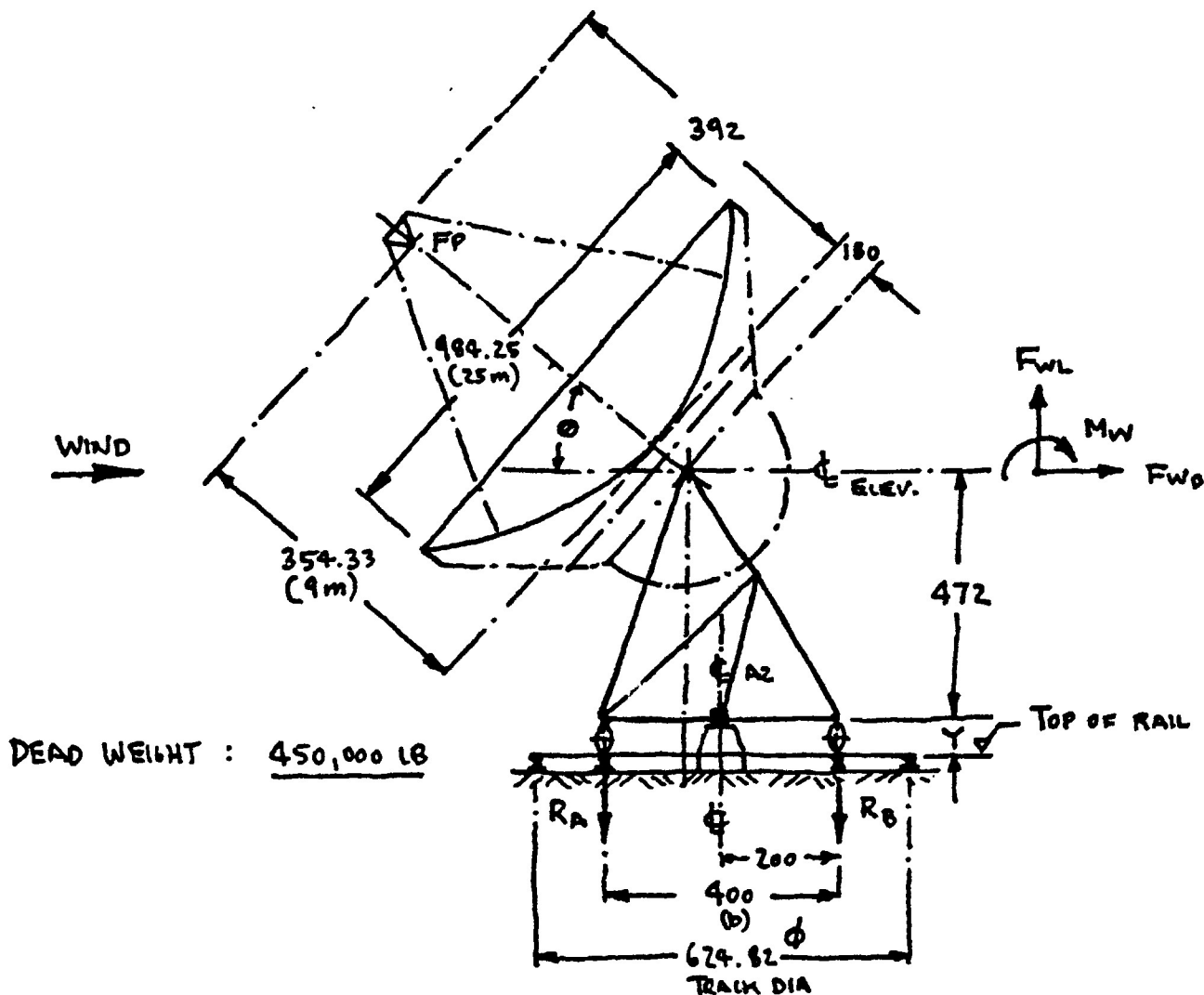
VLBA ANTENNA MEMO No. 4

Subject: Drive Design-VLBA Antennas

Attached for your information is VLBA Antenna Memo No. 4 covering the drive design for the VLBA antenna. This design was performed by O. HEINE of Systems Development Laboratories. We will make some revision in the area of the pintle bearing and perhaps in the azimuth gearbox/support wheel interface.

VLBA ADVANCED DESIGN  
WIND-LOADS AND MOMENTS

VLBA Antenna Memo #4



WINDLOADS & MOMENTS @ AXIS INTERSECTION (BASE FACTORS ONLY) *					
ANGLE OF ATTACK, $\theta$	$0^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$180^\circ$
DRAG FORCE, $F_{wD}$ (lb)	1,158,140	578,800	91,280	206,040	806,060
LIFT FORCE, $F_{wL}$ (lb)	-14,450	-1,086,200	59,720	124,680	21,440
MOMENT, $M_w$ (in-lb)	$14.76 \times 10^6$	$45.1 \times 10^6$	$90.9 \times 10^6$	$115.76 \times 10^6$	$21.06 \times 10^6$

\* BASED ON DATA SUPPLIED BY L. KING

### REACTIONS AND WHEEL LOADS :

$$R_{A,B} = \frac{1}{2} (DL + IL) \pm \frac{F_{WD}(\pm 12 + Y) + M_W + M_I}{b} - F_{WL}/2 ; b = 400 \text{ IN}$$

$$IL = \underline{40,000 \text{ LB}} \text{ (ICE LOAD)} ; M_I = \underline{-9.69 \times 10^6 \text{ IN} \cdot \text{LB}} \text{ @ } 0^\circ ; +9.69 \times 10^6 \text{ IN} \cdot \text{LB} \text{ @ } 180^\circ$$

(ICE UNBALANCE MOMENT)

$$DL = \underline{450,000 \text{ LB}} \text{ (DEAD LOAD)}$$

VLBA FORCES & MOMENTS @ INTERSECTION OF AXIS, $V_W = 60 \text{ MPH}$ , $.1 \text{ CM ICE}$ *						
ANGLE OF ATTACK, $\theta$		$0^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$180^\circ$
FWD (LB)		74,120	37,040	5,840	13,310	51,510
F <sub>WL</sub> (LB)		-925	-69,520	3,820	7,980	1,370
M <sub>W</sub> (IN·LB)		$.94 \times 10^6$	$2.89 \times 10^6$	$5.62 \times 10^6$	$7.41 \times 10^6$	$1.35 \times 10^6$
M <sub>I</sub> (IN·LB)		$-9.69 \times 10^6$	$-9.65 \times 10^6$	0	$4.65 \times 10^6$	$9.69 \times 10^6$

ASSUMED : WHEEL DIA. = 30.0 IN ;  $Y = 36.0 \text{ IN}$

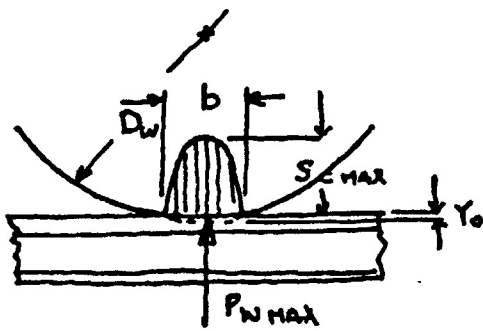
REACTIONS @ AZ TRACK (RAIL) @ $V_W = 60 \text{ MPH}$ , $.1 \text{ CM ICE}$						
ANGLE OF ATTACK, $\theta$		$0^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$180^\circ$
R <sub>A</sub> (LB)		173,205	237,619	221,123	193,456	151,196
R <sub>B</sub> (LB)		317,720	321,901	265,057	288,564	337,434

$$P_{W \text{ MAX}} = \frac{R_{B \text{ MAX}}}{2} = \frac{337,434}{2} \approx \underline{169,000 \text{ LB}} \text{ (OPERATIONAL LOAD)}$$

$$P_{W \text{ MAX}} = \frac{R_{B \text{ MAX}}}{2} = \frac{312,393}{2} \approx \underline{156,000 \text{ LB}} \text{ (SURVIVAL LOAD @ } 110 \text{ MPH, } \theta = 90^\circ)$$

$$\text{VS. } P_{\text{ALLOWABLE}} = 1600 \text{ WD} = 1600 \times 3.5 \times 30 = \underline{168,000 \text{ LB}}$$

GIVEN BY C.M.A.A. FOR CLASS C, MODERATE SERVICE  
ON 175 CR RAIL



$$F_w = \frac{P_w}{W} = \frac{169,000}{3.5} = \underline{48,286 \text{ lb/in}}$$

$$\bar{b} = 2.15 \sqrt{\frac{F_w D_w}{E}} = 2.15 \sqrt{\frac{169,000/3.5 (30)}{30 \times 10^6}} = \underline{.472 \text{ in}}$$

$$Y_0 = 2 F_w \frac{1-\nu^2}{\pi E} \ln \frac{\pi E W}{F_w (1-\nu^2)}$$

$$Y_{0 \text{ max}} = 2 \times 48,286 \frac{1-.25^2}{\pi \times 30 \times 10^6} \ln \frac{\pi 30 \times 10^6 \times 3.5}{48,286 (1-.25^2)} = \underline{.0085 \text{ in}}$$

$$Y_{0 \text{ min}} = 2 \times \frac{151,196}{2 \times 3.5} \frac{1-.25^2}{\pi \times 30 \times 10^6} \ln \frac{\pi 30 \times 10^6 \times 3.5}{21,600 (1-.25^2)} = \underline{.0042 \text{ in}}$$

POINTING ERROR DUE TO DIFFERENTIAL CONTACT DEFORMATION IS THEN:

$$\tan \epsilon = \frac{Y_{0 \text{ max}} - Y_{0 \text{ min}}}{400} = \frac{.0085 - .0042}{400} = \underline{1.075 \times 10^{-5}}$$

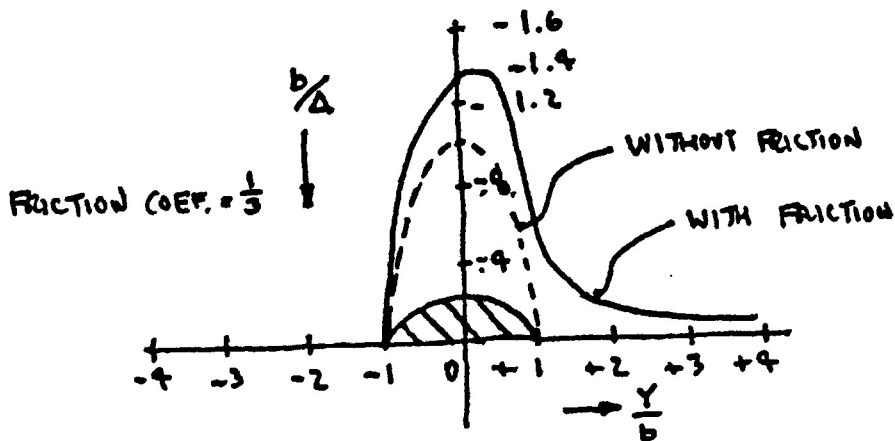
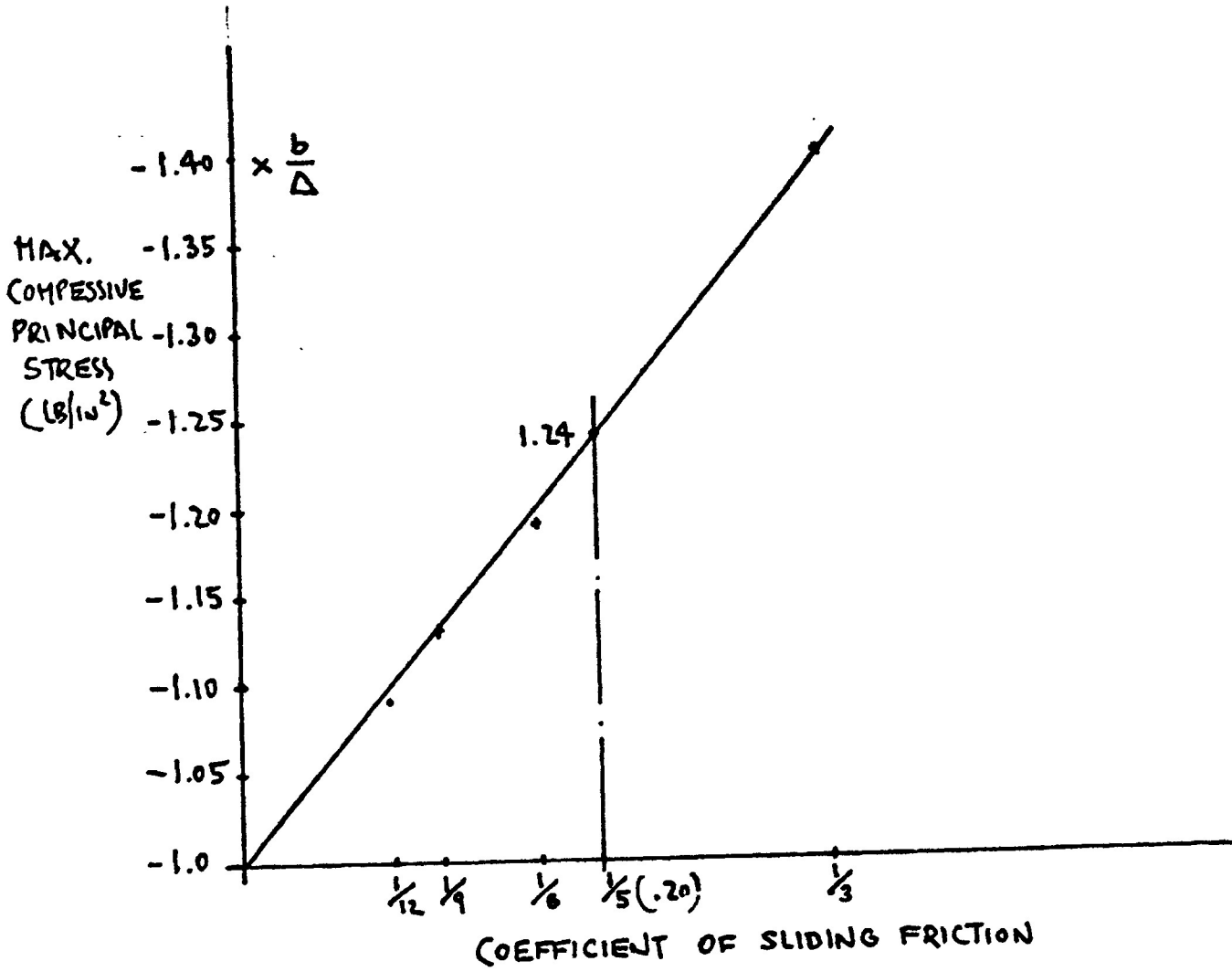
$$\epsilon = .00062^\circ \approx \underline{2.2 \text{ ARC SEC}} \quad \text{@ } V_w = 60 \text{ MPH (QUITE OK)}$$

$$S_{\text{MAX}} = 1.24 \times .591 \sqrt{\frac{F_w E}{D_w}}$$

$$S_{\text{MAX}} = 1.24 \times .591 \sqrt{\frac{48,286 \times 30 \times 10^6}{30}} = \underline{161,000 \text{ lb/in}^2}$$

THE FACTOR 1.24 ACCOUNTS FOR THE INCREASE IN CONTACT STRESS DUE TO SLIDING FRICTION COEFF. = .20. (SEE NEXT PAGE). THE MAX RECOMMENDED WHEEL LOAD OF 168,000 LB CORRESPONDS TO A CONTACT STRESS OF ABOUT 129,500 LB/IN<sup>2</sup>; THUS THE OVERLOAD FACTOR IS APPROX 25% OVER RATED LOAD FOR CLASS "C", MODERATE SERVICE.

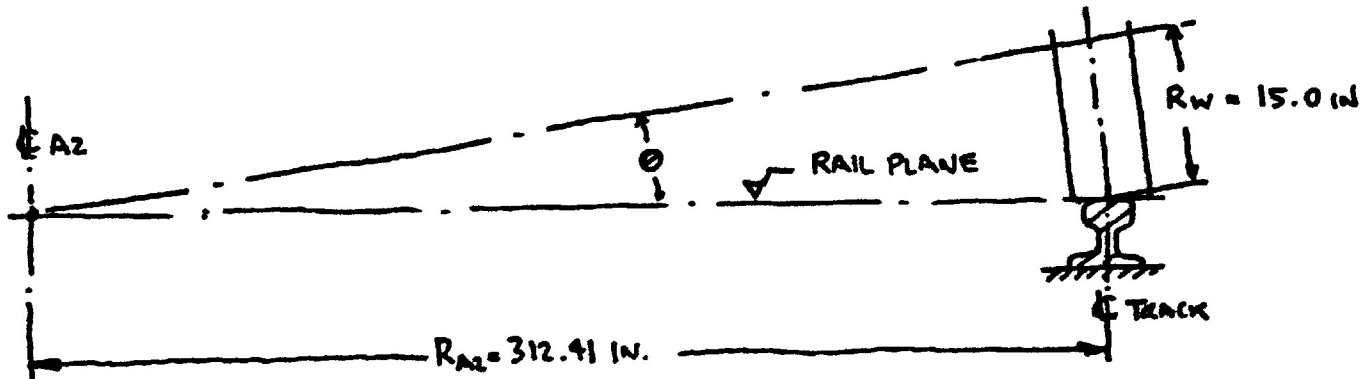
SOME HEAT TREATMENT OF THE RAIL & WHEELS MAY BE REQUIRED.



EFFECT OF TANGENTIAL FORCE DUE TO FRICTION ON CONTACT STRESS

REF: SEELY & SMITH, 21  
EDIT. ADVANCED MECHAN  
OF MATERIAL, PG. 7  
WILEY.

THE RAIL & WHEEL MAY EASILY BE HEAT TREATED (OIL QUENCHED & TEMPERED)  
 SINCE THE CARBON CONTENT OF THE RAIL STEEL IS TYPICALLY .67 ÷ .82%.

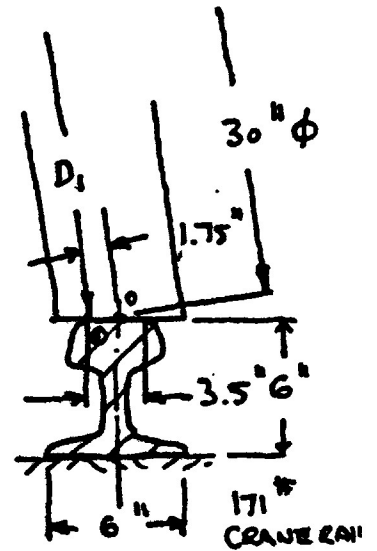


INCLINE OF WHEEL REQ'D TO AVOID SPIN FRICTION :

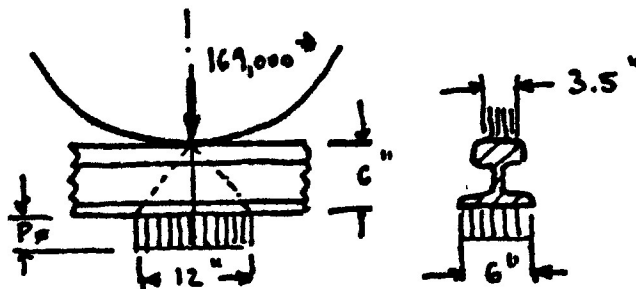
$$\sin \theta = \frac{15}{312.41} = .048 \quad ; \quad \theta = \underline{2.752^\circ}$$

$$D_1 = 30 - 2(\tan 2.752^\circ \times 1.75) = \underline{29.832 \text{ in}}$$

$$S_{\text{MAX} \textcircled{1}} = 1.24 \times .591 \sqrt{\frac{49,286 \times 30 \times 10^6}{29.832}} = \underline{161,500 \text{ lb/in}^2}$$



THIS IS ONLY MODERATELY HIGHER THAN THE COMPRESSIVE STRESS  
 AT POINT "O".



$$P_F = \frac{169,000}{6 \times 17} = \underline{2,347 \text{ lb/in}^2} \quad \text{DISTRIBUTED PRESSURE LOAD ON FOUNDATION.}$$

## FOUNDATION/RAIL INTERACTION :

HIGH STRENGTH CONCRETE HAS FOLLOWING PROPERTIES :

<u>TIME ELAPSE</u>	<u>COMPRESSIVE STRENGTH</u>	<u>MODULUS OF ELASTICITY, <math>E_c</math> (<math>lb/in^2</math>)</u>
3 MONTHS	7,810 $lb/in^2$	$4.45 \times 10^6$
1 YEAR	9,170 "	$5.53 \times 10^6$

SAFETY MARGIN AFTER 3 MONTHS :  $M_s = \frac{7,810}{2,347} = \underline{3.3}$  OK

THUS, THE RAIL MAY BE PLACED DIRECTLY (VIA GROUTING) ON THE CONCRETE FOUNDATION, BUT THIS MAY NOT BE PRACTICAL IN THIS CASE.

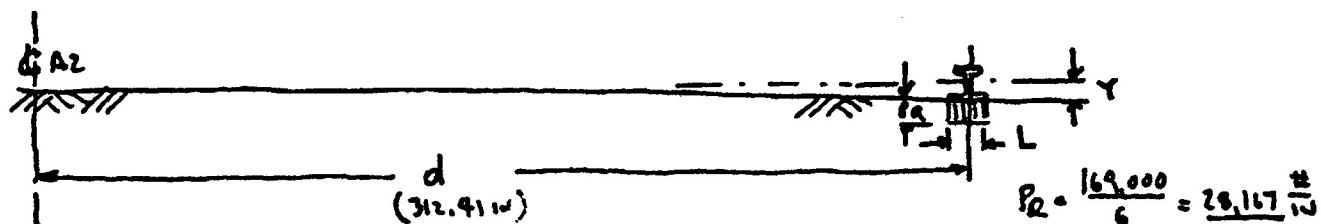
## ELASTIC DEFORMATION OF RAIL ON CONCRETE :



$$\beta = \sqrt[4]{\frac{R}{4EI}} \quad ; \quad M_{BMAX} = \frac{P_{WMAX}}{4\beta} \quad , \quad \text{AT THE LOAD, IN RAIL}$$

$$Y_{MAX} = \frac{P_{WMAX} \beta}{2R} \quad , \quad \text{AT THE LOAD}$$

$$I_{RAIL} = 73.4 \text{ in}^4 \quad \text{FOR 171}^{\#} \text{ RAIL}$$



$$P_R = \frac{169,000}{6} = 28,167 \frac{\text{lb}}{\text{in}}$$

$$Y = \frac{2P}{\pi E} \left( L \ln \frac{d}{L/2} \right) + PL \left( \frac{1 - \gamma_c}{\pi E c} \right)$$

RE: ROARK, 4th EDITION, CASE 11  
Pg. 322

$$\text{LET: } E_c = 4.40 \times 10^6 \frac{\text{lb}}{\text{in}^2}; \quad \gamma_c = .15$$

$$Y = \frac{2 \times 28,167}{\pi \cdot 4.40 \times 10^6} \left( 6.0 \ln \frac{312.41}{3} \right) + 28,167 \times 6.0 \left( \frac{1 - .15}{\pi \cdot 4.40 \times 10^6} \right) = \underline{.122 \text{ in}}$$

$$R = \frac{P_R L}{Y} = \frac{169,000}{.122} = \underline{1,385,246 \frac{\text{lb}}{\text{in}}}$$

$$\beta = \sqrt[4]{\frac{1,385,246}{4 \times 30 \times 10^4 \times 73.4}} = \underline{.112 \text{ in}^{-1}}$$

$$M_{B \text{ MAX}} = \frac{P_W}{4\beta} = \frac{169,000}{4 \times .112} = \underline{377,280 \text{ in lb}}$$

$$Y_{\text{MAX}} = \frac{P_W \beta}{2R} = \frac{169,000 \times .112}{2 \times 1,385,246} = \underline{.0068 \text{ in}}$$

(RAIL & FOUNDATION)

$$Y_{\text{MIN}} = \frac{75,598 \times .112}{2 \times 1,385,246} = \underline{.0031 \text{ in}}$$

$$\text{by POINTING ERROR, } \alpha = \frac{.0035}{400} = 8.75 \times 10^{-6}; \quad \alpha = \underline{1.80 \text{ ARC SEC}}$$

THIS IS WORST CASE @ 60 MPH.



TOTAL POINTING ERROR DUE TO COMBINED EFFECTS OF CONTACT AND BENDING DEFORMATION IS AT 60 MPH (WORST CASE) :

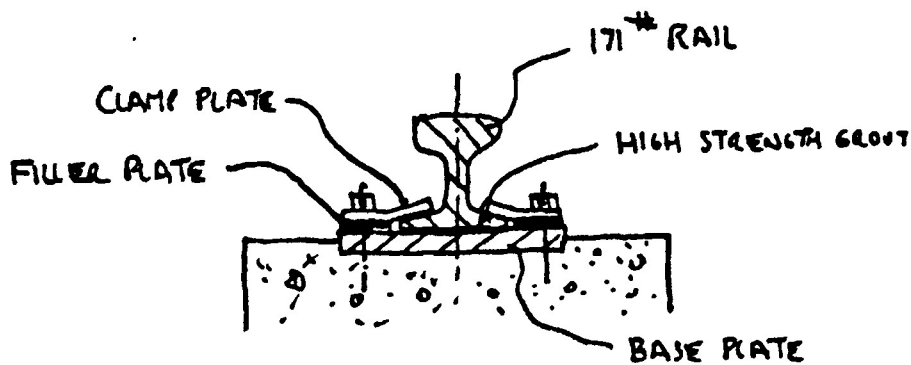
$$\gamma = \epsilon + d = 2.2 + 1.8 = \underline{4.0 \text{ ARCS SEC}}$$

THIS DOES NOT INCLUDE FOUNDATION/SOIL MASS TILT !

BENDING STRESS IN RAIL :

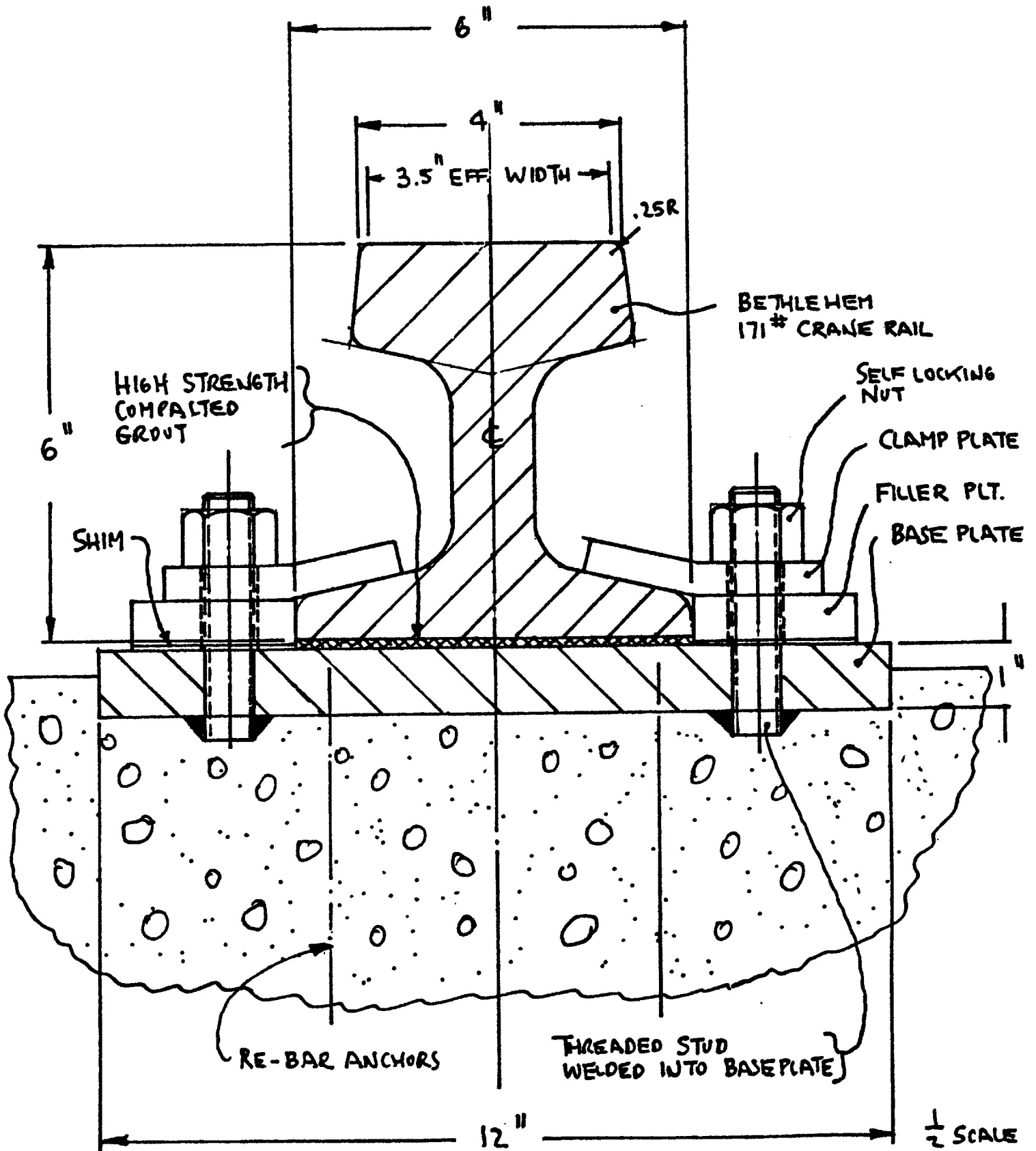
$$S_{Bmax} = \frac{M_{Bmax}}{Z_{MIN}} = \frac{377,280}{24.42} = \underline{15,450 \text{ LB/IN}^2} \text{ OK}$$

WHILE IT APPEARS TO BE FEASIBLE TO MOUNT THE RAIL/TRACK DIRECTLY ONTO THE CONCRETE BASE (FROM A LOAD/STRESS VIEWPOINT), IT IS PROBABLY DESIRABLE TO IMBED A BASE PLATE INTO THE FOUNDATION SURFACE SO THAT THE RAIL MAY BE ATTACHED SECURELY TO THE BASE VIA ADJUSTABLE, BOLTED CLIPS.



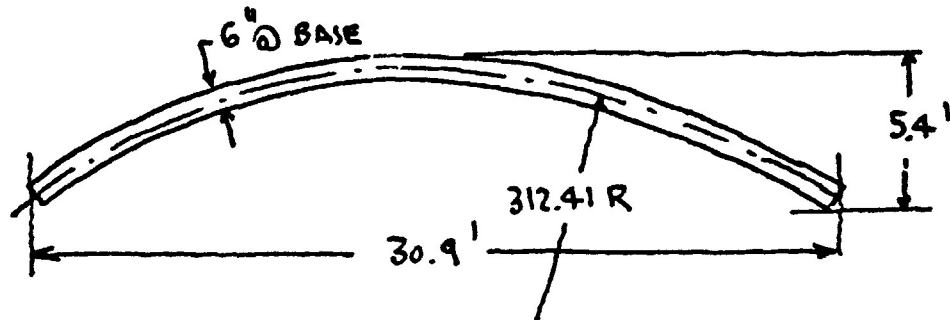
# VLBA - AZIMUTH TRACK - CROSS SECTION

9/26/83  
ORH.



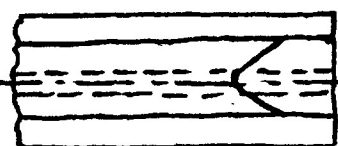
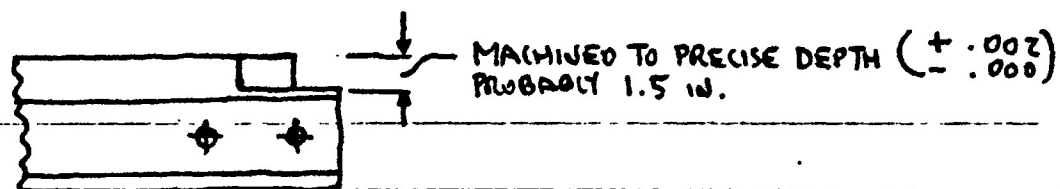
MANUFACTURING CONSIDERATIONS:

THE CIRCULAR AZ-CRANE RAIL TRACK WILL MOST LIKELY HAVE TO BE FABRICATED IN FIVE SEGMENTS SINCE THE STD. RAIL LENGTH IS 39 FT. . SPECIAL LENGTHS OF UP TO 60 FT CAN BE PROVIDED BY THE STEEL MILLS, BUT WOULD NOT BE AS EASILY SHIPPED & HANDLED. EACH OF THE FIVE SEGMENTS WOULD BE ABOUT 32.7 FT. LONG STRAIGHT, AND 30.9 FT LONG WHEN BENT AND WILL WEIGH APPROX. 2.8 TONS.



THE FIVE SEGMENTS REQUIRED TO MAKE A FULL CIRCLE COULD BE TEMPORARILY MOUNTED ON A SA1 1.0 IN THICK, FLAT STEEL PLATE. IN STAGGERED CONFIGURATION THE AREA REQUIRED WOULD BE 31 X 6 FT.. ALL FIVE SEGMENT COULD THEN BE GROUND FLAT VIA BLANCHARD GRINDER OR LARGE VERTICAL MILL PROVIDED WITH A GRINDING HEAD. OBVIOUSLY, THE SEGMENTS WOULD HAVE TO BE ROLLED, HEAT TREATED (HARDENED) AND END-MACHINED PRIOR TO THIS OPERATION.

SUBSEQUENTLY, THE RAIL SEGMENTS COULD BE PREPARED FOR PRECISION SPICING VIA MILLING AND DRILLING OPERATION.



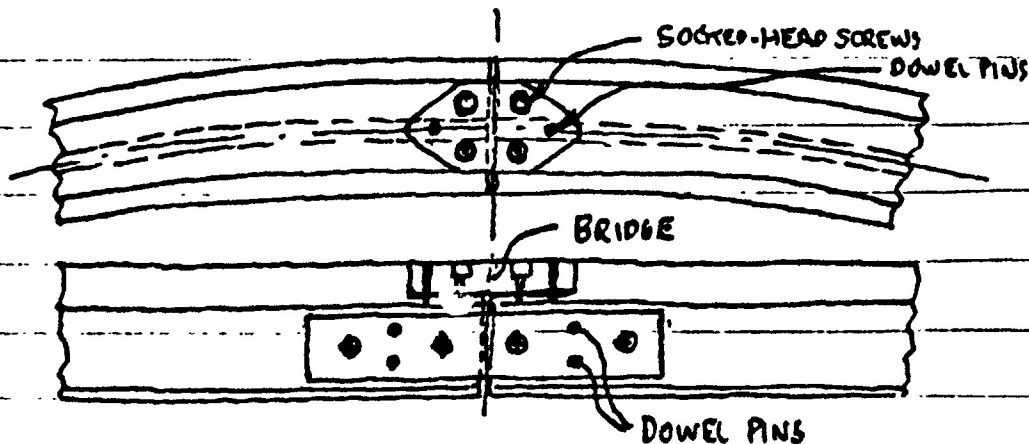
TOP VIEW

RAIL SEGMENT END PREPARATION.

AFTER THIS WORK HAS BEEN ACCOMPLISHED, ALL FIVE SEGMENTS ARE TEMPORARILY PLACED AND MOUNTED ON A SUITABLE, FLAT MOUNTING PLANE AND OPTICALLY ALIGNED TO BE CIRCULAR WITHIN  $\pm .030$  AND FLAT (IN PLANE) WITHIN  $\pm .003$  IN.

THEREAFTER THE SPICING IS APPLIED AND SECURED IN POSITION BY MEANS OF 2 DOWEL PINS ON EACH RAIL END. SPICES & RAIL ENDS ARE THAN MATCH-MARKED SO THAT THEY MAY BE RE-ASSEMBLED WITH THE SAME PRECISION IN THE FIELD.

WHEN THIS IS ACCOMPLISHED, THE FIVE PRECISION BRIDGES REQUIRED FOR SMOOTH SURFACE TRANSITION ARE FABRICATED VIA MATCH FITTING & ASSEMBLED.

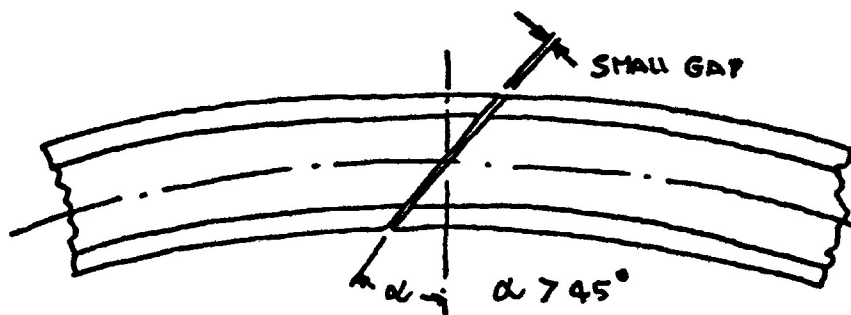


THE BRIDGES SHOULD BE MADE FROM A HIGH STRENGTH ALLOY SUCH AS SAE 4140 AND HEAT TREATED TO 58 RC SURFACE HARDNESS.

AFTER ASSEMBLING THE BRIDGES, THE SURFACE TRANSITION IS CHECKED VIA SUITABLE DIAL INDICATORS AND GROUND FLUSH VIA PORTABLE GRINDER, IF TOO HIGH, OR SHIMMED, IF TOO LOW.

AFTER MATCH-MARKING THE BRIDGES & RAIL ENDS, THE SEGMENTS ARE DISASSEMBLED AND READY FOR SHIPMENT TO THE SITE.

ANOTHER FEASIBLE AND PERHAPS MORE COST-EFFECTIVE METHOD FOR FABRICATION OF THE AZ-TRACK WOULD BE TO MACHINE THE JOINTS AS FOLLOWS:



IN THIS CASE A HIGH PRECISION MACHINING EFFORT IS REQUIRED TO MATCH THE ANGULAR CUT ENDS OF THE MATING SEGMENTS SO AS TO ACHIEVE A VERY SMALL GAP. PRE-GRINDING & SPLICING OPERATIONS WOULD BE THE SAME AS FOR THE KEYED BRIDGE VERSION.

TO ACHIEVE MINIMAL-OR NEAR ZERO DIMENSION GAPS WITH ALL 5 JOINTS, THE PROCEDURE WOULD BE TO ASSEMBLE 4 PRE-MACHINED SEGMENTS FIRST AND MATCH-FIT THE 5TH UNIT AFTER MAKING PRECISE MEASUREMENTS OF THE COORD LENGTH AND MITRE ANGLES.

AGAIN, THE SLICES & JOINTS WOULD BE MARK-MARKED TO ASSURE EASE OF ASSEMBLY AT SITE.

## ASSEMBLY AT SITE :

ASSEMBLY / INSTALLATION AT THE SITE INVOLVES THE FOLLOWING PROCEDURAL STEPS :

1. THE FIVE SEGMENTS ARE PLACED IN THE RIGHT ORDER PER MATCH MARKINGS ONTO THE BASE PLATE AND CENTERED WITH RESPECT TO THE PIVOT BEARING AS CLOSE AS POSSIBLE.
2. THE SLICE PLATES ARE MOUNTED AND FASTENED AFTER INSERTION OF POWER PINS.
3. THE ENTIRE ASSEMBLED TRACK IS NEXT RAISED A FRACTION OF AN INCH AND SHIFTED IN ITS FINAL CONCENTRIC POSITION.
4. THE TRACK IS THEN LEVELED VIA APPLICATION OF A JIB TRANSIT FITTED WITH OPTICAL MICROMETER AND PRECISION SCALE (OR EQUIVALENT LASER INSTRUMENT) BY RAISING OR LOWERING SPECIAL SECTIONS VIA SHIMS. THE ACHIEVABLE PRECISION IS PROBABLY ON THE ORDER OF  $\pm .005$  IN; THE ACCURACY OF THE OPTICAL TOOL IS APPROX.  $\pm .001$  IN.
5. AFTER LEVELING & ALIGNMENT HAS BEEN ACCOMPLISHED, HIGH STRENGTH (IRON-CEMENT TYPE) GROUT IS PLACED BETWEEN THE BASE PLATE AND RAIL AROUND THE TRACK AND COMPACTED BY SUITABLE MEANS.
6. FOLLOWING THE APPLICATION OF GROUT AND ITS SUBSEQUENT CURING, FILLER PLATES PLUS SHIMS ARE FITTED AND THE RAIL-TRACK IS CLAMPED DOWN FIRMLY VIA APPLIED CLAMP PLATES.

REQ'D VS. PROBABLE ACHIEVABLE AZ-ALIGNMENT ACCURACIES.

<u>ALIGNMENT ERROR</u>	<u>MAX. ALLOWABLE ERROR (ARC SEC)</u>	<u>EST'D ACHIEVABLE ACCURACY (ARC-SEC)</u>
AZ-AXIS TILT (W. RESPECT TO GRAVITY)	15	5
AZ-AXIS RUN OUT	10	5
AZ-AXIS NON-REPEATABLE	4	2

AZ-AXIS DRIVE REQUIREMENTS :

- NONIN. SPEED @ 40.3 MPH (45.9 MPH W. GUSTS) :  $90^\circ/\text{MIN} = \underline{.25 \text{ RPM}}$
- MINIM. SPEED @ 54.0 MPH (60 MPH MAX. WIND) :  $60^\circ/\text{MIN} = \underline{.167 \text{ RPM}}$

WIND INDUCED MOMENT @ AZ-AXIS AT 45.9 MPH : (MAXIMUM VALUE)

$$M_{t \text{ AZ NOM.}} = \frac{.00256 (45.9)^2}{144} \times 57.88 \times 10^6 (2) = 4.335 \times 10^6 \text{ IN LB}$$

$$= \underline{361,310 \text{ FT LB}}$$

WIND INDUCED MOMENT @ AZ-AXIS AT 60 MPH : (MAXIMUM VALUE)

$$M_{t \text{ AZ MAX}} = \frac{.00256 (60)^2}{144} \times 57.88 \times 10^6 (2) = 7.9064 \times 10^6 \text{ IN LB}$$

$$= \underline{617,367 \text{ FT LB}}$$

SPEED REDUCTION REQ'D @ 1800 RPM INPUT SPEED OF DC-DRIVE MOTOR(S)  
AND .25 RPM AZ-AXIS SPEED WITH 30" DIA WHEELS ON 624.82" DIA TRACK :

$$i_{CT} = \frac{1800}{624.82 \cdot 1} = 345.7 : 1 \quad @ 1800 \text{ RPM WIND SPEED}$$

$$i_{GT} = \frac{2500}{624.62/30 \cdot \frac{1}{4}} = 480.1 : 1 \quad \text{① 2500 RPM INPUT SPEED}$$

CONSIDER STO. QUADRUPLE REDUCTION SPEED REDUCER WITH  $i = 450 : 1$   
REDUCTION & 97% OVERALL EFFICIENCY FOR HELICAL GEAR :

$$N_{A2} = \frac{2500}{450} \cdot \frac{30}{624.62} = \underline{.27 \text{ RPM}} = 96^\circ/\text{MIN. (OK)}$$

ROLLING FRICTION LOSSES :

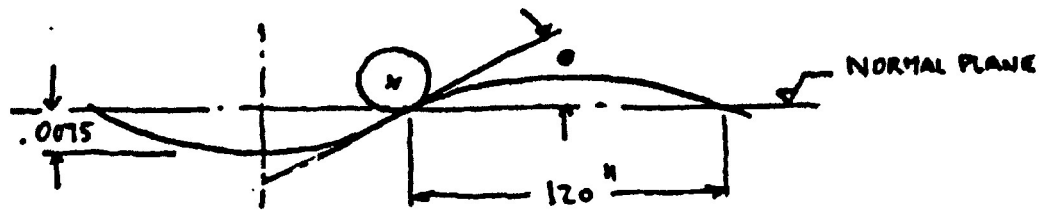
AVERAGE WHEEL LOAD IS WITH 1 m ICE :

$$\bar{F}_W = \frac{490,000}{4} = \underline{122,500 \text{ LB}}$$

ROLLING FRICTION LOSS  $\bar{F}_{FR} \approx \frac{\bar{F}_W}{R_W} f_R$  ;  $f_R = .010$  (FOR STEEL ON STEEL)  
RUSTY SURFACE

$$\bar{F}_{FR} = \frac{122,500}{15} \cdot .010 = \underline{81.67 \text{ LB/WHEEL}} = \underline{326.67 \text{ LB TOTAL (4 WHEELS)}}$$

IN ADDITION, THERE COULD BE WAVINESS IN THE TRACK WHICH WOULD  
REQUIRE ADDITIONAL RESISTANCE. ASSUMING THAT THIS MAY RESULT  
(WORST CASE ASSUMPTION) IN A MAXIMUM SLOPE OF  $2 \times \tan^{-1} \frac{.0075}{60} = .014^\circ$   
AND THAT ALL 4 WHEELS WOULD ENCOUNTER THE SAME SLOPE SIMULTANEOUSLY.



$$\bar{F}_{FR} = 326.67 + 4 \times 122,500 \tan .014^\circ = \underline{446.4 \text{ LB}}$$



REFERRED TO AZ-AXIS :  $\bar{M}_{bFR} = 446.4 \times 26.035 = \underline{11,622 \text{ FT-LB}}$

WHEEL BEARING FRICTION LOSS :

$\bar{M}_{bB6} = DL \times BG. \text{RADIUS} \times f_{B6}$  ;  $f_{B6} = .0018$  FOR TAPERED ROLLER B6.

$\bar{M}_{bB6} = 490,000 \times .25 \times .0018 = \underline{220.5 \text{ FT-LB}}$

REFERRED TO AZ-AXIS :  $\bar{M}_{E86} = 220.5 \times \frac{624.62}{30} = \underline{4,592 \text{ FT-LB}}$

RUNNING FRICTION @ AZ-AXIS =  $F_{AZ} = 16,214 \text{ FT-LB}$

ADDING CABLE FRICTION & PINTLE B6. FRICTION, SAY  $F_{AZ} = \underline{20,000 \text{ FT-LB}}$

AZIMUTH INERTIA :  $I_{AZ} = 168.56 \times 10^6 \text{ IN}^2\text{SEC}^2$  WITHOUT MOTOR (SEE PAGE 23)  
 $I_{AZ} = \underline{14.047 \times 10^6 \text{ SLUG-FT}^2}$

ACCELERATION =  $\frac{W}{t}$  ;  $t_{acc.} @ 45.9 \text{ MPH WIND} = 2 \text{ SEC}, 0 \div 90^\circ/\text{MIN}$   
 $t_{acc.} @ 60 \text{ MPH WIND} = 4 \text{ SEC}, 0 \div 60^\circ/\text{MIN}$

$a_1 = \frac{.0262 \text{ RAD/SEC}}{2} = \underline{.0131 \text{ RAD/SEC}^2} = .75^\circ/\text{SEC}^2$   
 $a_2 = \frac{.0175 \text{ RAD/SEC}}{4} = \underline{.0044 \text{ RAD/SEC}^2} = .25^\circ/\text{SEC}^2$

PEAK TORQUE REQ'D @ AZ-AXIS :

1) @ 45.9 MPH,  $T_{45.9} = 361,310 + 20,000 + 184,016 = \underline{565,326 \text{ FT-LB}}$

2) @ 60 MPH,  $T_{60} = 617,367 + 20,000 + 61,607 = \underline{699,194 \text{ FT-LB}}$

GEARBOX OUTPUT TORQUES:

A) DIRECT WHEEL DRIVE,  $i = 450 : 1$

$$i_{AZ \text{ WHEEL/TRACK}} = \frac{624.82}{30} = \underline{20.83 : 1}$$

$$M_t @ 45.9 \text{ MPH } 1) = \frac{565,326}{20.83} = \underline{27,140 \text{ FT-LB}} \quad (2 \text{ UNITS})$$

$$M_t @ 60 \text{ MPH } 2) = \frac{699,194}{20.83} = \underline{33,567 \text{ FT-LB}} \quad (2 \text{ UNITS})$$

INPUT TORQUE @ 80% MINIMUM OVERALL EFFICIENCY:

$$M_{\text{MOTOR } 1) = \frac{27,140}{2 \times 0.80} \frac{1}{450} = 37.69 \text{ FT-LB} = \underline{452 \text{ IN-LB}} @ 2393 \text{ RPM}$$

$$M_{\text{MOTOR } 2) = \frac{33,567}{2 \times 0.80} \frac{1}{450} = 46.62 \text{ FT-LB} = \underline{559 \text{ IN-LB}} @ 1562 \text{ RPM}$$

B) DRIVE THROUGH BULGEAR BUILT INTO WHEEL,  $i = 100 : 1$

$$M_t @ 45.9 \text{ MPH } 1) = \frac{565,326}{20.83} \frac{35}{150} \frac{1}{.98} = \underline{6,462 \text{ FT-LB}} \quad (2 \text{ UNITS})$$

$$M_t @ 60 \text{ MPH } 2) = \frac{699,194}{20.83} \frac{35}{150} \frac{1}{.98} = \underline{7,992 \text{ FT-LB}} \quad (2 \text{ UNITS})$$

$$M_{\text{MOTOR } 1) = \frac{6,462}{2 \times 0.80} \frac{1}{100} = 40.39 \text{ FT-LB} = \underline{485 \text{ IN-LB}} @ 2232 \text{ RPM}$$

$$M_{\text{MOTOR } 2) = \frac{7,992}{2 \times 0.80} \frac{1}{100} = 49.95 \text{ FT-LB} = \underline{599 \text{ IN-LB}} @ 1468 \text{ RPM}$$

DRIVE INPUT POWER REQUIREMENTS : (BOTH MOTORS DRIVING, ZERO BUCKING)

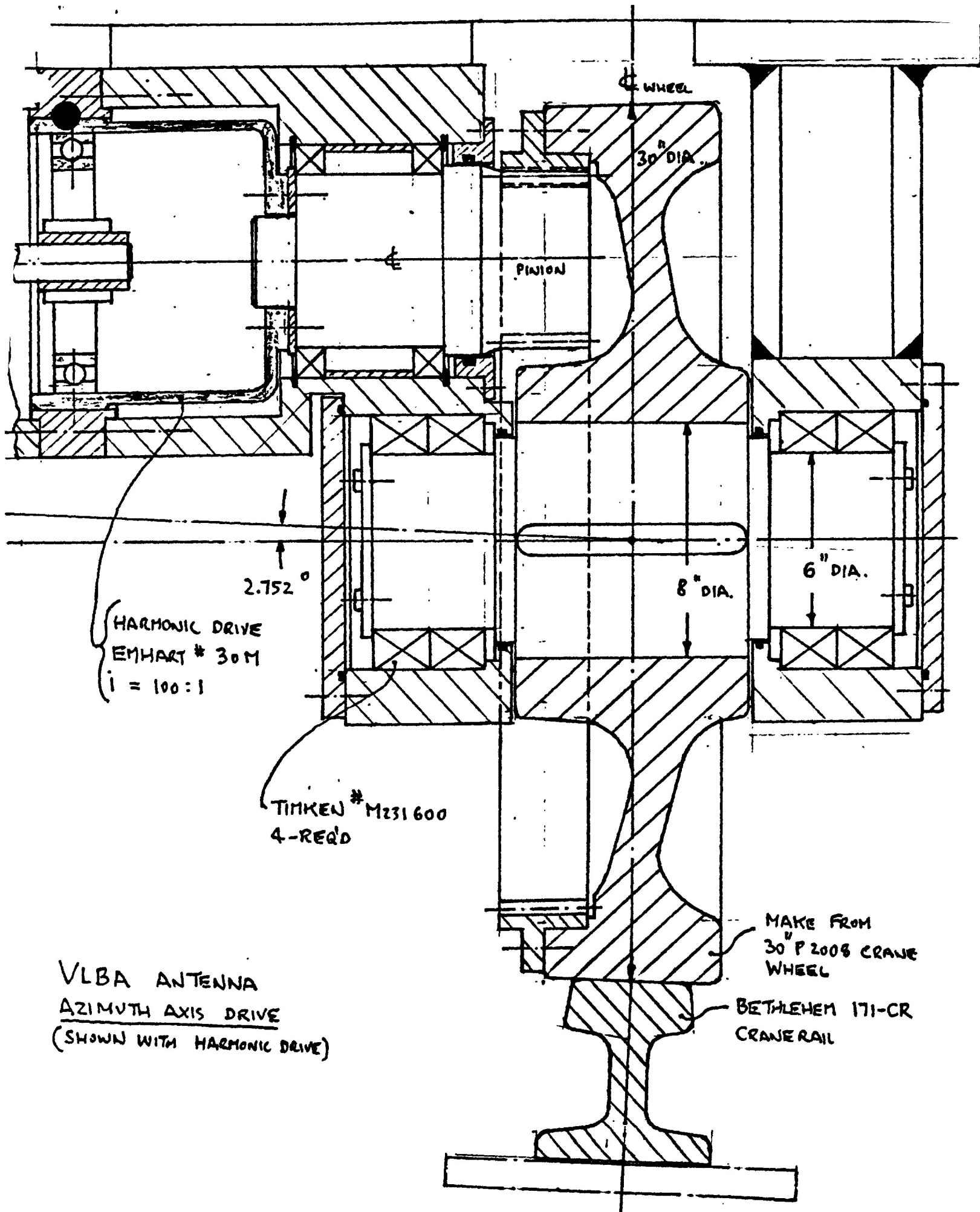
$$A_1) = \frac{37.69 \times 2393}{5252} = \underline{16.81 \text{ HP, MAX}}$$

$$A_2) = \frac{46.62 \times 1562}{5252} = \underline{13.87 \text{ HP, MAX}}$$

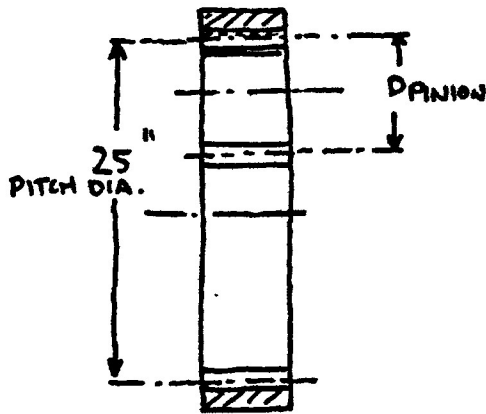
$$B_1) = \frac{40.39 \times 2232}{5252} = \underline{17.16 \text{ HP, MAX}}$$

$$B_2) = \frac{49.95 \times 1468}{5252} = \underline{14.15 \text{ HP, MAX}}$$





VLBA ANTENNA  
 AZIMUTH AXIS DRIVE  
 (SHOWN WITH HARMONIC DRIVE)



LET :  $N_T$  BULL GEAR = 150 TEETH  
 $N_T$  PINION = 35 "  
 DIAMETRAL PITCH = 6  
 PINION PITCH DIA =  $\frac{35}{6} = 5.833$  IN  
 $i$  BULL GEAR / PINION =  $\frac{25}{5.833} = \frac{150}{35} = \underline{4.286 : 1}$

$$n_{\text{INPUT}} = 100 \times \frac{150}{35} \times 20.627 \times .25 = \underline{2,232 \text{ RPM}}$$

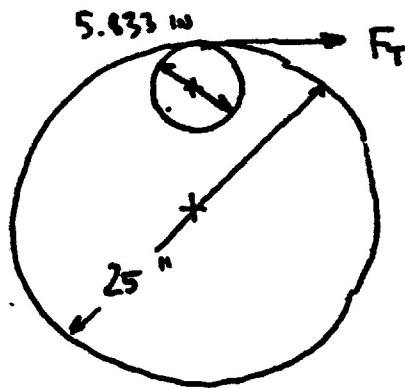
$$i_{AZ} = 100 \times \frac{150}{35} \times 20.627 = \underline{8,925.86 : 1}$$

$$M_{\text{EMAX}} = \frac{i_{AZ}}{1_{\text{DRIVE}}} \frac{33,000}{12} \cdot 4 = \frac{8,925.86}{100} \frac{33,000}{12} \cdot 4 = \underline{981,445 \text{ FT LB}}$$

TORQUE CAPABILITY

VS. 699,194 FT LB APPLIED

USE MAX. TORQUE CAPABILITY OF 33,000 IN LB TO SIZE GEARS !

CHECK GEARING

$$F_{T \text{ MAX}} = 33,000 \frac{2}{5.833} = \underline{11,315 \text{ LB}}$$

LET  $b = \text{FACE WIDTH} = 3.0 \text{ IN}$

$C = \text{VELOCITY FACTOR} = \frac{600}{600 + V_m}$

$V_m = \text{PITCH LINE VELOCITY} = \frac{2731.5}{100} \frac{5.833 \pi}{12} = \underline{34 \text{ FT/MIN.}}$

$C = \frac{600}{634} = \underline{.946}$

$S_0 = \frac{F_t P_D}{C b Y}$  ;  $Y = \text{LEWIS FACTOR} = .373 \text{ FOR } 20^\circ$

$S_0 = \frac{11,315 \times 6}{.946 \times 3 \times .373} = \underline{64,133 \text{ LB/IN}^2}$  (OK FOR HIGH STRENGTH STEEL SAE 4140 HEAT TREATED TO 210 ÷ 245 BARWELL HARDNESS)

CHECK "K" FACTOR : (RE: PRACTICAL GEAR DESIGN, DUDLEY)

$Q = \frac{N}{RPM_{AV.}} \frac{(i_{\text{GEAR/DRIVER}} + 1)^3}{1 + i^2} = \frac{9.67}{21.32} \frac{(4.29 + 1)^3}{4.29} = \underline{14.95 \times}$

$K = \frac{F_T}{b D_{P.D.}} \frac{(i_{G/P} + 1)}{1 + i^2} = \frac{11,315}{3 \times 5.833} \frac{(5.29)}{(4.29)} = \underline{800 \text{ (OK)}}$

\* ... = 2... .. K = 500 (OK)

ALLOWABLE 'K' FACTOR = 1500 FOR AUTOMOTIVE GEAR (LOW GEAR)  
HAVING A SURFACE HARDNESS OF 58 RC.

STIFFNESS OF GEAR MESH :

$$\frac{F_T}{Y} \cong b \times 2 \times 10^6 = 3.0 \times 2 \times 10^6 = \underline{6 \times 10^6} \text{ LB/IN}$$

$$\frac{M_T}{\theta} = \frac{F_T}{Y} \left(\frac{D_{PIN}}{2}\right)^2 = 6 \times 10^6 \left(\frac{5.833}{2}\right)^2 = \underline{5.1 \times 10^7} \text{ IN LB/RAD @ OUTPUT}$$

STIFFNESS OF PINION SHAFT :

EFFECTIVE LENGTH OF SHAFT : 8.5 IN (SCALED)

EFFECTIVE DIA. OF SHAFT : 6.0 IN

$$\frac{M_T}{\theta} = \frac{.5 R^4 \pi G}{L E} = \frac{.5 (3)^4 \pi 11.6 \times 10^6}{8.5} = \underline{1.74 \times 10^8} \text{ IN LB/RAD}$$

TOTAL STIFFNESS OF HARMONIC DRIVE & PINION/GEAR/SHAFT :

$$\frac{1}{K_{TOTAL}} = \frac{1}{K_{HD}} + \frac{1}{K_{GM}} + \frac{1}{K_{SHAFT}}$$

$$K_{TOTAL} = \left[ (7.5 \times 10^6)^{-1} + (5.1 \times 10^7)^{-1} + (1.74 \times 10^8)^{-1} \right]^{-1}$$

$$K_{TOTAL} = 6.3 \times 10^6 \text{ IN LB/RAD}$$

$K_{TOTAL}$  REFERED TO ANTENNA AXIS :

$$K_{TOTAL_{A2}} = 4 \times 6.3 \times 10^6 \times \left( 20.83 \times \frac{150}{35} \right)^2 = \underline{2.01 \times 10^{11}} \text{ IN LB/RAD}$$

MOMENT OF INERTIA REFERED TO AZ-AXIS :

$$I_{AZ} = 14.54 \times 10^9 \text{ LB-IN}^2 = \underline{37.67 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{GEAR BOXES (MATH. DRIVE)}} = 156 \times 4 \times 8,925.86 \frac{1}{366} = \underline{130.45 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{MOTORS}} = 4 \times \overset{\text{ASSUMED}}{(3.0)} 144 \frac{1}{366} (8,925.86)^2 = \underline{356.66 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{PIVOTS}} = 4 \times 414 \frac{1}{366} (89.27)^2 = \underline{.034 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{WHEELS}} = 4 \left( \frac{800 \times 15^2}{2} \right) \frac{1}{366} 20.93^2 = \underline{.405 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{AZ, \text{TOTAL}} = \overset{\text{DISK} + \text{GEARBOXES} + \text{MOTORS} + \text{PIVOTS} + \text{WHEELS}}{(37.67 + 130.45 + 356.66 + .034 + .405)} 10^6 = \underline{525.22 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$f_n \cong \frac{1}{2\pi} \sqrt{\frac{K}{I}} \cong \frac{1}{2\pi} \sqrt{\frac{2.01 \times 10^{11}}{5.252 \times 10^6}} \cong \underline{3.11 \text{ CPS}}$$

VS. IN COMPARISON : (FOR VLA ANTENNA)

$$I_{AZ} = 11.25 \times 10^9 \text{ LB-IN}^2 = \underline{29.145 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{GEARBOXES}} = 2 \times 1.34 \times 10^9 \frac{1}{366} = \underline{6.94 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{\text{MOTORS}} = 2 \times 1.36 \times 144 \frac{1}{366} \times (10,342.5)^2 = \underline{108.54 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$I_{AZ, \text{TOTAL}} = (29.145 + 6.94 + 108.54) 10^6 = \underline{144.63 \times 10^6 \text{ LB-IN-SEC}^2}$$

$$K_{AZ} = 2 \times 5 \times 10^6 \times 12 \times (10.5)^2 = \underline{1.32 \times 10^{10} \text{ IN-LB/RAD}}$$

$$f_n \cong \frac{1}{2\pi} \sqrt{\frac{1.32 \times 10^{10}}{144.63 \times 10^6}} \cong 1.52 \text{ CPS}$$



$f_n$  (FOR 2 MOTOR/DRIVES DRIVING WHEEL AXLES):

$$I_{A2} = 14.54 \times 10^7 \text{ LB-IN}^2 = \underline{37.67 \times 10^6 \text{ LB-IN}^2}$$

$$I_{\text{GEMBOXES (ESTIMATED)}} = \underline{10 \times 10^6 \text{ LB-IN}^2}$$

$$I_{\text{MOTORS}} = 2(.037)12 \times 9372^2 = \underline{76 \times 10^6 \text{ LB-IN}^2}$$

15HP @ 2500RPM  
FRAME & 812A

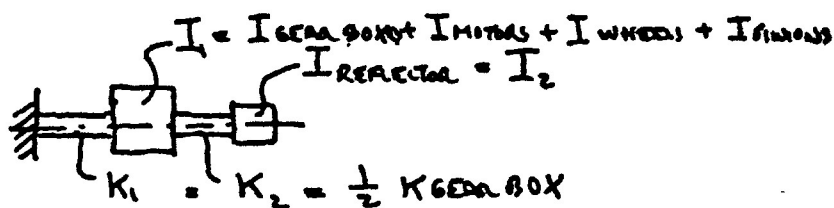
$$I_{\text{WHEELS}} = \underline{.405 \times 10^6 \text{ LB-IN}^2}$$

$$I_{A2} = (37.67 + 10.0 + 76.0 + .405)10^6 = \underline{126.1 \text{ LB-IN-SEC}^2 (\times 10^6)}$$

$$K = 20.827^2 \times 12 \times 10^7 = \underline{5.705 \times 10^{10} \text{ IN-LB/RAD}}$$

$$f_n = \frac{1}{2\pi} \sqrt{\frac{K}{I}} = \frac{1}{2\pi} \sqrt{\frac{5.705 \times 10^{10}}{126.1 \times 10^6}} = \underline{3.23 \text{ CPS}}$$

A MORE REALISTIC MODEL:



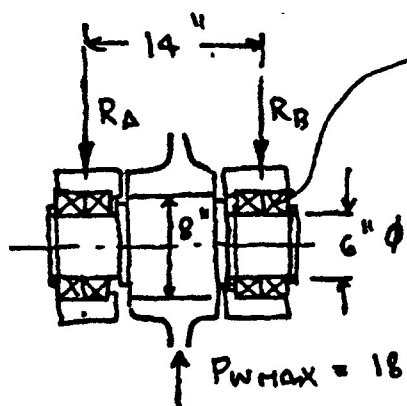
$$f_{NAZ} = \frac{1}{2^{1.5} \pi} \left\{ \left( \frac{K_1}{I_1} + \frac{K_2}{I_1} + \frac{K_2}{I_2} \right) \pm \left[ \left( \frac{K_1}{I_1} + \frac{K_2}{I_1} + \frac{K_2}{I_2} \right)^2 - \frac{4 K_1 K_2}{I_1 I_2} \right]^{1/2} \right\}^{1/2}$$

$$f_{NAZ} = \frac{1}{2^{1.5} \pi} \left\{ \left( \frac{1.05 \times 10^{11}}{467.55 \times 10^6} + \frac{1.05 \times 10^{11}}{467.55 \times 10^6} + \frac{1.05 \times 10^{11}}{37.67 \times 10^6} \right) \pm \left[ \left( 3,216.09 \right)^2 - \frac{4 (1.05 \times 10^{11})^2}{(467.55 \times 37.67) \times 10^{12}} \right]^{1/2} \right\}^{1/2}$$

$f_{NAZ} = \underline{2.20 \text{ CPS}}$  (FOR NEW DESIGN) THIS IS (OK)

VS.  $f_{NAZ} = \underline{2.10 \text{ CPS}}$  (FOR VLA) VS. 2.15 CPS MEASURED

WHEEL AXLE & BEARINGS:



TIMKEN TAPERED ROLLER BEARING # M231600  
 BORE: 6.010 ; O.D: 6.750 IN  
 WIDTH: 1.8437, BLR = 15,000 @ 500 RPM

$R_A = R_B = \frac{P_{WMAX}}{2} = \underline{92,000 \text{ LB}}$

LOAD ON EACH OF 4 BEARINGS =  $\frac{R_A}{2} = \frac{R_B}{2} = \underline{46,000 \text{ LB}}$

SPEED FACTOR,  $SF = \left( \frac{500}{n} \right)^3 = \left( \frac{500}{5.21} \right)^3 = \underline{3.93}$

BASIC LOAD RATIO @ 5.21 RPM =  $15,000 \times 3.93 = \underline{58,950 \text{ LB}}$  VS.

46,000 APPLIED, @ B<sub>10</sub> LIFE = 3000 HRS. (OK)

STRESS IN AXLE:

$$M_{B\text{MAX}} = P_{W\text{MAX}} \frac{l}{4} = 194,000 \frac{14}{4} = \underline{694,000 \text{ IN LB}}$$

$$Z_0 = \frac{I}{R} = \pi \frac{R^3}{4} = \pi \frac{4^3}{4} = \underline{50.27 \text{ IN}^3}$$

$$S_{B\text{MAX}} = \frac{694,000}{50.27} = \underline{12,810 \frac{\text{LB}}{\text{IN}^2}} \text{ (OK)}$$

TORSIONAL STRESS IN AXLE IF DIRECTLY DRIVEN:

$$M_{t\text{MAX}} = \frac{29,999}{2} \cdot 1.10 = 16,500 \text{ FT LB} \approx \underline{198,000 \text{ IN LB}} \text{ @ } 10\% \text{ BUFFER}$$

$$\approx 18,000 \text{ " } = \underline{216,000 \text{ IN LB}} \text{ @ } 20\% \text{ "}$$

$$S = \frac{\pi D^3}{16} = \frac{\pi 6^3}{16} = \underline{42.41 \text{ IN}^3}$$

$$S_{T\text{MAX}} = \frac{216,000}{42.41} = \underline{5,093 \frac{\text{LB}}{\text{IN}^2}} \text{ (OK) AXLE MAY BE DRIVEN DIRECTLY.}$$

MINIMUM INPUT-SPEED @ SIDEREAL TRACKING:

$$i_{\text{TOTAL}} = 8,925.86 : 1$$

$$N_{\text{OUTPUT}} = 1 \text{ RPD} = \frac{1}{24 \times 60} = \underline{6.94 \times 10^{-4} \text{ RPM}}$$

$$N_{\text{INPUT}} = i_{\text{TOTAL}} \times N_{\text{OUTPUT}} = 8,925.86 \times 6.94 \times 10^{-4} = \underline{6.2 \text{ RPM}}$$

$$\text{DRIVE SPEED RANGE} = \frac{.25}{6.94 \times 10^{-4}} = \underline{360 : 1}$$

MINIMUM TORQUE REQUIRED @ ZERO WIND VELOCITY  
(ABOUT AZ-AXIS)

$$T_{1 \text{ MIN.}} = M_{t \text{ FR}} + M_{t a} = 4,817 + 7,975 = \underline{12,792 \text{ FT LB}}$$

ASSUMING 60% SLIPPING AT THIS CONDITION TO GET HIGHER  
SPEED REDUCER EFFICIENCY (SEE PAGE 10 OF EMHART BROCHURE):

$$T_{1 \text{ HW DRIVE}} = 1.8 \times 12,792 \approx \underline{23,026 \text{ FT LB}}$$

REFERRED TO PINION SHAFT @  $i = 69.27:1$  @ .98% EFFICIENCY OF  
BUCKET/PINION MESH:

$$T_{\text{MIN PINIONS}} = \frac{23,026 \times 12}{69.27 \times .98} = \underline{3,158 \text{ IN LB}} \text{ VS. } 26,000 \text{ IN LB}$$

RATED TORQUE FOR UNITS

$$\frac{T_{\text{MIN PINION}}}{T_{\text{RATED}}} = \frac{3,158}{2 \times 26,000} = \underline{.06} \text{ (6\%)}$$

EFFICIENCY IS ONLY ~ 20% AT THIS POINT

ASSUMING THAT SLIPPING TORQUE IS MUCH HIGHER SO THAT UNIT  
WOULD BE OPERATED MORE OR LESS AT CONSTANT TORQUE REGARDLESS  
OF SPEED OR TORQUE DEMAND:

$$\text{LET DRIVE TORQUE @ AZ-AXIS} = 26,000 \times 2 \times .98 \times 69.27 \times \frac{1}{12} = \underline{425,095 \text{ FT LB}}$$

$$\text{BUCKET TORQUE} = 425,095 - 12,792 = \underline{412,303 \text{ FT LB}} \text{ (97\%)}$$

DRIVE EFFICIENCY WOULD BE AT LEAST 61%.

$$\text{AT 50 \% RATED TORQUE} = 14,000 \times 2 \times .96 \times 69.27 \times \frac{1}{12} = \underline{204,131 \text{ FT LB}}$$

$$\text{BUCKING TORQUE} = 204,131 - 12,792 = \underline{191,339 \text{ FT LB}} \\ (94\%)$$

EFFICIENCY WOULD BE ABOUT 60% (SEE PAGE 10 OF ETHART BROCHURE)

SUMMARY :

- APPLICATION OF HARMONIC DRIVE GEAR TRAINS FOR THE AZIMUTH DRIVE OF THE VLBA ANTENNAS APPEARS TO BE FEASIBLE, PROVIDED THE SERVO LOOP CAN BE SUCCESSFULLY CLOSED. THIS REQUIRES SOME FURTHER EVALUATION BY ELECTRO STALE.
- 4 DRIVES WOULD BE REQUIRED (ONE ON EACH WHEEL) WITH GEAR/PINION ARRANGEMENT AS SHOWN ON PAGE M)
- THE UNITS MAY HAVE TO BE OPERATED AT NEAR CONSTANT TORQUE TO ACHIEVE GOOD DRIVE EFFICIENCIES.
- THE COMPONENT GROUP COSTS \$ 2210.-, FOR THE 30M DRIVE, IN QUANTITIES OF 25 ÷ 49. THIS RELATIVELY LOW COST MAY MAKE THE APPLICATION OF HARMONIC DRIVES ATTRACTIVE IN THIS CASE, ALTHOUGH THIS MUST BE TRADED OFF AGAINST THE INCREASE IN COST DUE TO THE ADDITIONAL SERVO DRIVE (ALIAS) REQUIRED FOR 4 DRIVES WHICH WOULD COST ABOUT \$ 120,000.-

# Systems Development Laboratory

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619

Mr. Michael J. Hardiman  
Manager, Special Products Division  
PHILADELPHIA GEAR CORPORATION  
King of Prussia, PA 19406

October 12, 1983

Dear Mr. Hardiman:

Attached are preliminary Azimuth Axis drive requirements for the VLBA Antenna as discussed with you during our recent telcon on the 10th of October.

Please review these requirements and indicate the option you would prefer and also provide the needed information as indicated on sheet 28 at your earliest convenience.

Very truly yours,

SYSTEMS DEVELOPMENT LABORATORY

Otto R. Heine

P.S : THE ELEV. GEARBOXES WOULD BE IDENTICAL TO THE VLA UNITS  
WITH EXCEPTION OF THE MAXIMUM "SLEW TO STOP" OUTPUT TORQUE  
REQUIREMENT WHICH WILL BE FOR THE VLBA :

$$M_e \text{ MAX} = \frac{1,021,137}{2(.98)36.71} (12) = \underline{170,300 \text{ IN-LB}}$$

MAX. WINDMOMENT @ 60MPH + 1cm ICE UNBALANCE  
@ 120° ELEVATION ANGLE

@  $n = 774$  RPM INPUT SPEED ( $\frac{1}{3}$  RPM @ ELEV. AXIS = 10°/MIN.)

MAX. SLEW SPEED IS 2322 RPM (INPUT) FOR VLBA ; TOTAL ELEV. GEAR  
RATIO IS 27,868 : 1

10/11/63  
ORH.

## VLBA ANTENNA

### AZIMUTH AXIS DRIVE REQUIREMENTS :

#### HELICAL OR PLANETARY GEAR UNITS

4 OR 2 UNITS, (DRIVEN VIA DC-SERVO MOTORS WITH 2500 RPM MAX. INPUT SPEED)

AZ-AXIS SPEED RANGE : SIDEREAL TO .25 RPM (360:1)

MAX. TORQUE @ AZ-AXIS (TRACKING): 374,102 FT-LB @ .25 RPM

MAX. TORQUE @ AZ-AXIS (DRIVE TO STOP): 624,883\* FT-LB @ .167 RPM

TYPE OF DRIVE ARRANGEMENT : BIASING, ANTI-BACKLASH (BUCKING)

WHEEL / TRACK RATIO : 20.827 : 1 (30 IN WHEELS ON 624.82 IN TRACK)

#### OPTION 1 :

##### DRIVE THROUGH INTERNAL BULL GEARS BUILT INTO 30 IN WHEELS

NO. OF GEAR TRAINS : 4

PITCH DIA. OF BULL GEARS (INTERNAL GEAR, BUILT INTO WHEELS) : 25 IN ; PD = 6 ; N<sub>TEETH</sub> = 150

PITCH DIA. OF PINIONS : 5.833 IN ; N<sub>TEETH</sub> = 35

RATIO BULLGEAR / PINION : 4.286 : 1

RATIO OF SPEED REDUCERS : 100 : 1

TOTAL RATIO : 8,925.86 : 1

MAX. INPUT SPEED : 2232 RPM (@ .25 RPM OUTPUT SPEED)

MAX. INPUT POWER (EACH UNIT) : 11 HP @ 2232 RPM WITH 20% BUCKING TORQUE

SPRING CONSTANT OF SPEED REDUCER :  $7.5 \times 10^6$  IN-LB / RAD (MINIMUM)  
REFERRED TO OUTPUT SHAFT

NOTE: RATIO MAY BE CHANGED TO ACHIEVE A MAX. INPUT SPEED OF 2500 RPM.

#### OPTION 2 :

SAME AS OPTION 1, WITH EXCEPTION OF THE FOLLOWING:

NO. OF GEAR TRAINS : 2

MAX INPUT POWER (EACH UNIT) : 22 HP @ 2232 RPM WITH 20% BUCKING TORQUE

SPRING CONSTANT OF SPEED REDUCER :  $15 \times 10^6$  IN-LB / RAD (MINIMUM)  
REFERRED TO OUTPUT SHAFT

10/11/63  
O.M.

### OPTION 3:

DRIVE WHEELS DIRECTLY

NO OF GEAR TRAINS	:	4	
RATIO OF SPEED REDUCERS	:	450 : 1	<u>NOTE</u> : RATIO MAY BE CHANGED TO ACHIEVE A MAX. INPUT SPEED OF 2500 RPM
TOTAL RATIO	:	9,372.15 : 1	
MAX. INPUT SPEED	:	2343 RPM	
MAX. INPUT POWER (EACH UNIT)	:	11 HP @ 2343 RPM W. 20% BUCKING TORQUE	
SPRING CONSTANT OF SPEED REDUCER	:	$3.0 \times 10^7$ IN/LB/RAD. (MINIMUM) RELEASED TO OUTPUT SHAFT.	

### OPTION 4:

SAME AS OPTION 3 WITH EXCEPTION OF THE FOLLOWING:

NO. OF GEAR TRAINS	:	2	
MAX. INPUT POWER/UNIT	:	22 HP @ 2343 RPM W. 20% BUCKING TORQUE	
SPRING CONSTANT OF SPEED REDUCER	:	$6.0 \times 10^7$ IN/LB/RAD (MINIMUM) RELEASED TO OUTPUT SHAFT	

### NOTE: \*

WHEN DRIVING TO STOP, BUCKING IS NOT REQUIRED, THUS ALL 4 (OR 2 RESPECTIVELY) UNITS SHARE THE LOAD.

### INFORMATION NEEDED:

1. OUTLINE DIMENSIONS, SHAFT DIMENSIONS, MOUNTING ARRANGEMENT.
2. WEIGHT
3. APPROX. COST FOR 40 (RESPECTIVELY 20) UNITS
4. CHECK BULLGEAR/PINION DIMENSIONS; DETERMINE FACE WIDTH REQUIRED BASED ON HIGH STRENGTH STEEL & 58 RC SURFACE HARDNESS.
5. APPROX. COST OF BULLGEAR & DRIVE PINION.



# VLBA ANTENNA

10/12/83  
ORH

## ELEVATION DRIVE REQUIREMENTS:

CONSIDER VLA - ELEVATION DRIVE :

GEAR BOX RATIO	:	564 : 1	(541.077)
BULL GEAR / PINION RATIO	:	36.71 : 1	(36.706)
ELEVATION GEAR RATIO	:	20,704 : 1	OVERALL (19,860.71)
BULL GEAR DIA. (PITCH DIA)	:	312 IN	
PINION PITCH DIA	:	8.5 IN	
DIAMETRAL PITCH, P	:	2	
GEAR BOX STIFFNESS CONSTANT	:	$3.5 \times 10^6$ FT LB / RAD @ OUTPUT	
GEAR BOX INERTIA	:	$7.0 \times 10^9$ LB-IN <sup>2</sup> @ ELEV. AXIS	

VLBA ELEVATION DRIVE : (ASSUME VLA GEARBOX IS UTILIZED)

BULL GEAR PITCH DIA	:	420 IN
MAX. AXIS SPEED	:	$\frac{1}{12}$ RPM (30° / MIN)
BULL GEAR / PINION RATIO	:	<u>49.41</u> : 1 ( $\frac{420}{8.5}$ )
ELEVATION GEAR RATIO	:	<u>27,868.24</u> : 1 (49.41 x 564) 26,736 : 1
MAX. INPUT SPEED	:	<u>2,322</u> RPM (OK VS. 2500 ALLOWABLE) <u>2226</u> RPM

- 1) MAX. WIND MOMENT @ EL-AXIS @ 45.9 MPH,  $\theta = 120^\circ$ ,  $M_{W1} = 361,310$  FT LB
  - 2) MAX. " " @ 60 MPH,  $\theta = 120^\circ$ ,  $M_{WMAX} = 617,367$  "
- ICE UNBALANCE MOMENT :  $9.69 \times 10^6$  IN LB @  $\theta = 0$ ,  $M_I = 403,750$  " @  $\theta = 120^\circ$

MAX. MOMENT DUE TO WIND @ 60 MPH + LOW ICE,  $M_{MAX} = \underline{1,021,137}$  FT LB

(UNIT IS DRIVEN VIA. BOTH DRIVE UNITS AT THIS POINT)  
@ 10° / MIN.

$N_{INPUT(1)} = \frac{361,310}{5252} \frac{1}{12} \frac{1}{.95} 1.2 = \underline{7.24 \text{ HP}}$ , AT NORMAL OPERATING CONDITION, ASSUMING AN OVERALL GEARTRAIN EFFICIENCY OF 95% AND BIAS TORQUE OF 20%.

$N_{INPUT(2)} = \frac{1,021,137}{2 \times 5252} \frac{1}{36} \frac{1}{.95} = \underline{2.64 \text{ HP}}$ , AT DRIVE TO STOP OPERATING CONDITION (60 RPM &  $10^\circ/\text{MIN.}$ )

INERTIA @ ELEV. AXIS (ADV. DES.) :  $I_{ELEV} = 15.44 \times 10^9 \text{ LB-IN}^2$   
 $= \underline{40 \times 10^6 \text{ LB-W-SEC}^2}$

$I_{GEARBOXES} = 2 \times 7.0 \times 10^9 \left( \frac{27,868}{20,704} \right)^2 \frac{1}{306} = \underline{65.7 \times 10^6 \text{ LB-W-SEC}^2}$   
(2 x .037 x 12) x 27,868<sup>2</sup>  
 $I_{MOTORS} = 2 \times 1.36(144) \frac{1}{306} (27,868)^2 = \underline{748.1 \times 10^6 \text{ LB-W-SEC}^2}$

$I_{ELEV. TOTAL} = \text{REACTOR GEARS MOTORS} = (40.0 + 65.7 + 748.1) 10^6 = \underline{893.8 \times 10^6 \text{ LB-W-SEC}^2}$   
795.3 x 10<sup>6</sup>

$K_{ELEV.} = 2 \times 3.5 \times 10^8 \times 12 \times 49.41^2 = \underline{2.05 \times 10^{11} \text{ IN-LB/RAD}}$

$f_n \approx \frac{1}{2\pi} \sqrt{\frac{K}{I}} = \frac{1}{2\pi} \sqrt{\frac{2.05 \times 10^{11}}{895.8 \times 10^6}} = \underline{2.41 \text{ CPS}}$   
2.55 CPS (ON)

VS. IN COMPARISON: (FOR VLA ANTENNA)

$I_{ELEV} = 8.65 \times 10^9 \frac{1}{206} = \underline{22.93 \times 10^6 \text{ LB-W-SEC}^2}$

$I_{GEARBOXES} = 2 \times 7.0 \times 10^9 \frac{1}{306} = \underline{36.3 \times 10^6 \text{ LB-W-SEC}^2}$

$I_{MOTORS} = 2 \times 1.36 \times 144 \frac{1}{206} (20,704)^2 = \underline{435 \times 10^6 \text{ LB-W-SEC}^2}$

$$I_{\text{ELEV. TOTAL}} = (22.93 + 36.3 + 435.0) 10^6 = \underline{494.23 \times 10^6 \text{ LB. IN. SEC}^2}$$

$$K_{\text{ELEV.}} = 2 \times 3.5 \times 10^6 \times 12 \times 36.71^2 = \underline{1.13 \times 10^{11} \text{ IN. LB. / RAD}}$$

$$f_n \approx \frac{1}{2\pi} \sqrt{\frac{1.13 \times 10^{11}}{494.23 \times 10^6}} \approx \underline{2.41 \text{ CPS (FOR VLA)}}$$

THIS IS IN GOOD AGREEMENT WITH  $f_n \approx 2.41 \text{ CPS}$  CALCULATED FOR THE VLBA ADVANCED DESIGN.

HENCE, THE VLA - GEARBOXES ARE CONSIDERED SUITABLE FOR THE ELEVATION DRIVE OF THE VLBA ANTENNA.

MORE ACCURATELY :

$$f_n = \frac{1}{2^{1.5} \pi} \left\{ \left( \frac{K_1}{I_1} + \frac{K_2}{I_2} + \frac{K_2}{I_2} \right) + \left[ (a)^2 - \frac{4K_1 K_2}{I_1 I_2} \right]^{\frac{1}{2}} \right\}^{\frac{1}{2}}$$

$$f_n = \frac{1}{2^{1.5} \pi} \left\{ \left( \frac{1.025 \times 10^{11}}{853.6 \times 10^6} + \frac{1.025 \times 10^{11}}{853.6 \times 10^6} + \frac{1.025 \times 10^{11}}{40 \times 10^6} \right) + \left[ 2802.6^2 - \frac{4 \times (1.025 \times 10^{11})^2}{(853.6 \times 40) \times 10^{12}} \right]^{\frac{1}{2}} \right\}^{\frac{1}{2}}$$

$$f_{n_{\text{REV}}} = \underline{1.70 \text{ HZ}}$$

$$\text{LIKEWISE, } f_{n_{\text{ELEV}}} = \underline{1.70 \text{ HZ}} \\ \text{FOR VLA}$$

ALSO, GOOD AGREEMENT (OK)

VS. 2.07 HZ ACTUALLY MEASURED FOR VLA ANTENNAS.

THE ACTUAL LOCKED ROTOR RESONANT FREQUENCY WILL PROBABLY BE AROUND 2.1 HZ FOR THE VLBA ADVANCED DESIGN.



83-RNW-0242  
18 October 1983

Mr. Otto R. Heine, Consultant  
13372 Calle Colina  
Coway Roway, California 92064

Attention: Mr. Otto R. Heine

Subject: VLBA

Reference: O. Heine/R. White Telecon of 10 Oct 83

Gentlemen:

The following information is enclosed in support of your VLBA study efforts:

1. Reliance Electric DC Motor Dimension Sheet
2. Stearns Brakes Series 87,000 Data Sheet
3. Proposal for A Standard A Antenna Control System with Linear DC Drives

The DC motors can be purchased for C-Face or D-Flange mounting. The 1750 RPM motors are currently optimum in terms of availability and price. We have encouraged most designs around them, but we also have recent applications with 1150 and 2500 RPM motors. In this VLBA case, the 2500 RPM base speed would increase the drive-train ratio and help on the minimum smooth velocity characteristic. As we discussed, the Reliance motors with the special options included with our orders have proven to be excellent torque sources for antenna drives.

The oil filled helical gear main speed reducers used on VLA have provided the best compliance and minimum smooth velocity characteristics of the various approaches that we have experienced. The oil shear losses are higher in these reducers at high speed, but their other advantages justify them overall.

In addition to the servo interface with the radio telescope drive train, another critical interface is the axis position pick-off design. Assuming an accurate position transducer is used, its mechanical tie-in with respect to the true antenna boresight is



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Mr. Otto R. Heine  
18 October 1983  
Page 2

very critical. Making sure no or little main load paths are involved in the pick-off attachment design has historically been difficult.

The proposal enclosed addresses an INTELSAT Standard A commercial communication antenna control system (32 Meter diameter antenna operating at 4/6 GHZ). The control system hardware presented would be applicable to this VLBA requirement. Photographs and block diagrams depict our existing designs. We are an engineering house and can design to meet most requirements, but taking advantage of as much as possible of our present equipment will keep the costs minimized.

Please contact Don Heitzman or myself if we can be of further assistance.

Very truly yours,

ELECTROSPACE SYSTEMS, INC.

Ralph N. White  
Division Manager,  
Antenna and Control Systems

RNW/djm

Enclosures

# Systems Development Laboratory

ENGINEERING CONSULTANTS  
13372 CALLE COLINA  
POWAY, CALIFORNIA 92064  

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 (714) 485-5657

Mr. Ralph N. White  
Division Manager  
Antenna and Control Systems  
ELECTROSPACE SYSTEMS, INC.  
Box 1359, Richardson, Texas 75080

21 October 1983

Dear Mr. White:

Thank you for the information you supplied with your letter of 18 October.

Attached are the presently anticipated VLBA drive requirements, the applicable operating conditions and environmental conditions, along with pertinent information on the Harmonic Drive (AZ option A) to be considered. Please review this material and provide the following information, needed for budgetary purpose and to prepare realistic design specifications, at your earliest convenience.

1. Recommended DC-servo motors for AZ- option A and or option B, and EL axes. Please include specific information on motor characteristics, brakes and tachometers.
2. Estimated performance of Servo/Drive system under the various operating conditions. Please provide supporting engineering calculations where applicable.
3. Estimated cost of control system hardware excluding, but interfacing with data system, considering the VLA control system hardware requirements as a guideline. Please consider that 10 Telescopes would be required, as a minimum.

A system description will not be necessary if the control system hardware described in your INTELSTAT Standard A commercial communication antenna control system would indeed be applicable to the VLBA requirements.

Very truly yours,

SYSTEMS DEVELOPMENT LABORATORY

Otto R. Heine

cc. William G. Horne, NRAO

VLBA - OPERATING CONDITIONS

<u>ITEM</u>	<u>NOMENCLATURE</u>	<u>CONDITION</u>	<u>REQUIREMENT</u>
1	<u>PRECISION I</u> FULL ACCURACY	WIND VELOCITY (NO ICE)	13.92 ± 2.24 MPH (GUST)
2	<u>PRECISION II A</u> REDUCED ACCURACY	" "	40.26 ± 5.59 MPH (GUST)
3	<u>PRECISION II B</u> REDUCED ACCURACY	" "	53.69 MPH (NO GUST)
4	DRIVE TO STOP	" + 1cm ICE	60 MPH
5	AXIS ACCELERATION	PRECISION I, II <sub>A</sub> , AZIMUTH	.0131 RAD/SEC <sup>2</sup>
6	AXIS ACCELERATION	" I, II <sub>A, B</sub> , ELEVATION	.0044 RAD/SEC <sup>2</sup>
7	AXIS ACCELERATION	PRECISION II <sub>B</sub> , AZIMUTH	.0044 RAD/SEC <sup>2</sup>
8	AXIS ACCELERATION	" , ELEVATION	.0044 RAD/SEC <sup>2</sup>
9	AXIS SPEED	PRECISION I, II <sub>A</sub> , AZIMUTH	.25 RPM, MIN.
10	AXIS SPEED	PRECISION I, II <sub>A, B</sub> , ELEVATION	.0633 ( $\frac{1}{16}$ ) RPM, MIN.
11	AXIS SPEED	PRECISION II <sub>B</sub> , AZIMUTH	.167 ( $\frac{1}{6}$ ) RPM, MIN.
12	AXIS SPEED	DRIVE TO STOP, ELEVATION	.0276 ( $\frac{1}{36}$ ) RPM, MIN.
13	SKY COVERAGE	TRAVEL LIMITS	± 270° AZ, 5° - 125° ELEV.

ENVIRONMENTAL CONDITIONS

a)	TEMPERATURE RANGE	PRECISION I	0°F - 86°F
b)	TEMPERATURE RANGE	PRECISION II A & B	-22°F - 104°F
c)	RELATIVE HUMIDITY	PRECISION I	0 - 50%
d)	RELATIVE HUMIDITY	PRECISION II A, B & DRIVE TO STOP	0 - 98%
e)	RAINFALL	PRECISION II A, B & DRIVE TO STOP	2 IN/HR
f)	ICE & SNOW	" "	1cm, 4 LB/FT <sup>2</sup>
g)	ELEVATION	ALL	0 - 10,000 FT
h)	SURVIVAL WIND VELOCITY		110 MPH, 1cm ICE

# VLBA - DRIVE PARAMETERS

10/21/63  
ORX.

		<u>AZIMUTH (A)</u>	<u>AZIMUTH (B)</u>	<u>ELEVATION</u>
K <sub>WT</sub>	- WIND TORQUE CONSTANT		172, EL = 0°	172° EL = 120°
V	- WIND VELOCITY, MPH			
I <sub>AX</sub>	- INERTIA @ AXIS, SLUG-FT <sup>2</sup>		14.05 x 10 <sup>6</sup>	8.81 x 10 <sup>6</sup>
A	- AXIS LEVEL ACCELER., RAD/SEC <sup>2</sup>			
UB	- UNBALANCE, FT-LB			5,000 New 349,000 (KE)
F <sub>AX</sub>	- AXIS LEVEL RUNNING FRICTION, FT-LB		20,000	10,000
N <sub>AX</sub>	- OVERALL GEAR RATIO	8,926	9,372	27,868
N <sub>MR</sub>	- MAIN REDUCER GEAR RATIO	100	450	564**
F	- MOTOR LEVEL RUNNING FRICT., FT-LB			
I <sub>S</sub>	- MOTOR INERTIA, SLUG-FT <sup>2</sup>			
η	- EFFICIENCY, MAIN REDUCER	.80	.80	.80
f <sub>n</sub>	- LOCKED ROTOR RESONANCE, CPS		2.1 MINIMUM	2.4 MINIMUM
K	- AXIS LEVEL SPRING CONSTANT, FT-LB/RAD		1.68 x 10 <sup>10</sup>	1.71 x 10 <sup>10</sup>
n	- NUMBER OF DRIVES	4	2	2
Type	- TYPE OF GEAR BOXES	HARMONIC DRIVE, 30 M OR. TORQUE REDUCING MELCAL	QUADRANT REACTION MELCAL	QUADRANT REACTION MELCAL
N <sub>M</sub>	- MAX. MOTOR SPEED, RPM		2500	2500
E <sub>SS</sub>	- SERVO SYSTEM ERROR, PRECISION I, ARC-SEC			1.5*
D <sub>R</sub>	- DATA SYSTEM RESOLUTION, BIT			21
E <sub>DS</sub>	- DATA SYSTEM ERROR, ARC SEC			1.24* (20 BIT)
V <sub>MIN</sub>	- MINIMUM SMOOTH VELOCITY, %/SEC			<.002; <.0004*(1)
B	- BIAS TORQUE RATIO @ PRECISION I, %			10 - 20

NOTES:

(1) STICK SLIP THRESHOLD VELOCITY IS EST'D AT .0004 %/SEC @ PRECISION I.

\* TARGET

\*\* SAME AS USED IN VLA



SIZING OF DRIVE MOTORS :  $T_M = \frac{KWT V^2 + I_{AX} A + F_{AX} + U_B}{n N_{AX} \eta} + F + I_B N_{AX} A$

ASSUME : (AZIMUTH DRIVE & ELEV. DRIVE)

$F_{AZ} (A) ; F_{EL} = .75 \text{ FT-LB} ; F_{AZ} (B) = 1.5 \text{ FT-LB}$

$I_{SAZ} (A) ; I_{SEL} = .042 \text{ SLUG-FT}^2 ; I_{AZ} (B) = .08 \text{ SLUG-FT}^2$

$T_{MAZ(A)}^{IIA} = \frac{\text{(WIND)} \quad \text{(INERTIA)} \quad \text{(BC. FRICTION)} \quad \text{(UNBALANCE)}}{4 (8926) \cdot 80} + .75 + .042 (8926) \cdot 0.0131 = \frac{25.46 \text{ FT-LB}}{\text{(PEAK VALUE) NO. COST}}$

$T_{MAZ(A)}^{IIB} = \frac{172 (57.96)^2 + 14.05 \times 10^6 \times .0044 + 20,000 + 0}{4 (8926) \cdot 80} + .75 + .042 (8926) \cdot 0.0044 = \underline{22.80 \text{ FT-LB}}$

VS. RATED OUTPUT TORQUE OF 22.8 FT-LB WITH SHORT TERM OVERLOAD CAPABILITY OF 34.2 FT-LB. FOR 5 HP @ 1150 RPM VLA MOTOR (OK)

PEAK HP =  $\frac{25.46 \times 2232}{5252} \approx \frac{11 \text{ HP @ } 2232 \text{ RPM } (.25 \text{ RPM AXIS SPEED})}{4 \text{ MOTORS}}$  (OK)

$T_{MAZ(B)}^{IIA} = \frac{172 (95.85)^2 + 14.05 \times 10^6 \times .0131 + 20,000 + 0}{2 (9372) \cdot 80} + 1.5 + .08 (9372) \cdot 0.0131 = \underline{49.04 \text{ FT-LB}}$

$T_{MAZ(B)}^{IIB} = \frac{172 (57.96)^2 + 14.05 \times 10^6 \times .0044 + 20,000 + 0}{2 (9372) \cdot 80} + 1.5 + .08 (9372) \cdot 0.0044 = \underline{43.65 \text{ FT-LB}}$

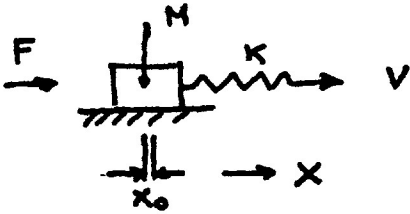
VS. RATED OUTPUT TORQUE OF 52 FT-LB WITH SHORT TERM OVERLOAD CAPACITY OF 66 FT-LB FOR 15 HP @ 1750 RPM INTERMEDIATE DRIVE MOTOR (OK)

PEAK HP =  $\frac{49.04 \times 2343}{5252} \approx \frac{22 \text{ HP @ } 2343 \text{ RPM } (.25 \text{ RPM AXIS SPEED})}{2 \text{ MOTORS}}$  (OK)

$T_{M'ELEV. (A)}^{II B} = \frac{172 (45.85)^2 + 8.61 \times 10^6 \times .0044 + 10,000 + 5,000}{2 (27,818) \cdot 80} + .75 + .042 (27,818) \cdot 0.0044 = \underline{18.34 \text{ FT-LB}}$  (OK)

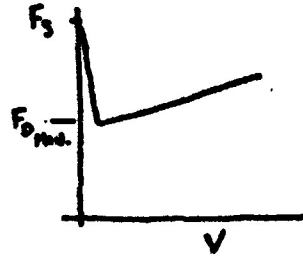
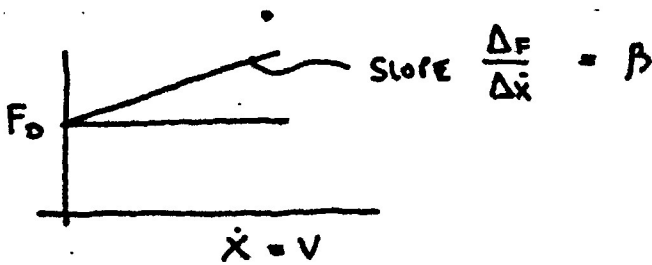
# STICK / SLIP THRESHOLD

SIMPLE SPRING MASS SYSTEM



$$M\ddot{x} + \beta\dot{x} + Kx + F_D = F$$

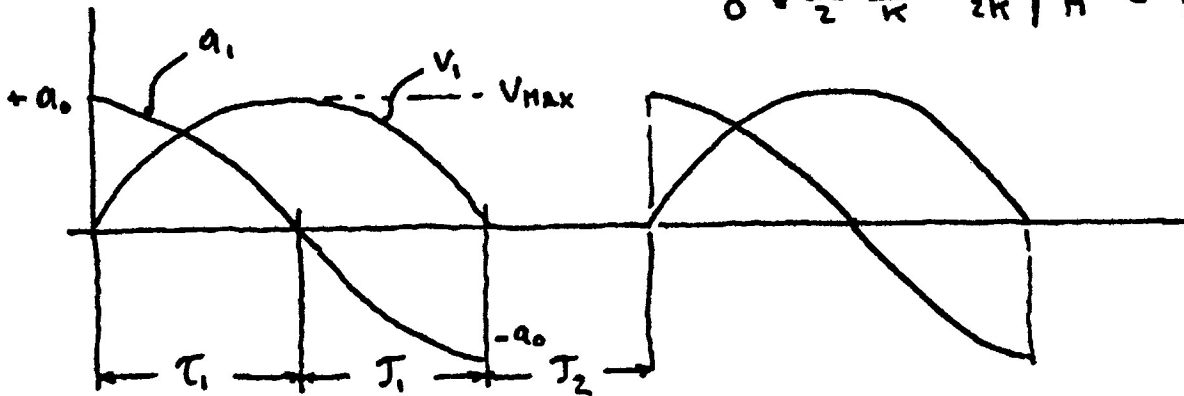
DYNAMIC FRICTION FORCE      DAMPING FORCE



$$M\ddot{x} + \beta\dot{x} + Kx = F - F_D \quad ; \quad x = \frac{F - F_D}{Ms^2 + \beta s + K}$$

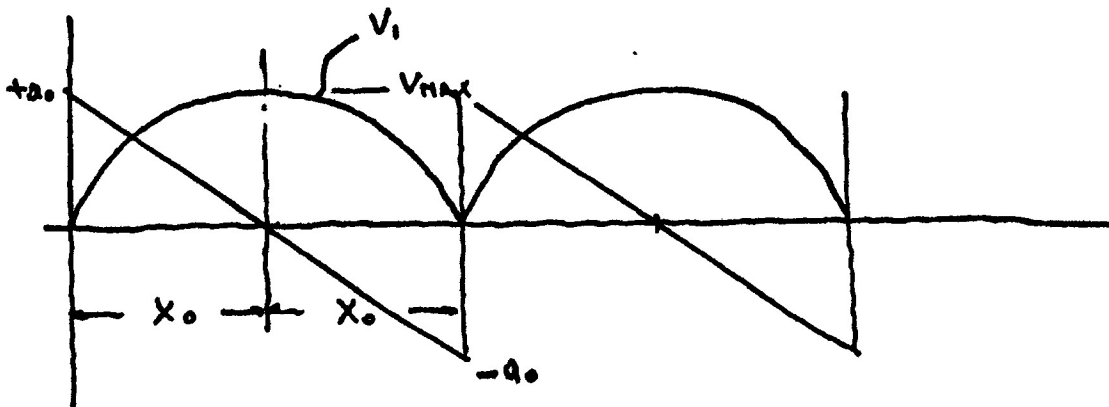
$$x = \frac{F - F_D}{K} \frac{1}{\frac{M}{K}s^2 + \frac{\beta}{K}s + 1} \quad ; \quad \omega_n = \sqrt{\frac{K}{M}} \quad ; \quad \frac{2\zeta}{\omega_n} = \frac{\beta}{K}$$

$$\zeta = \frac{\beta}{2} \frac{\omega_n}{K} = \frac{\beta}{2K} \sqrt{\frac{K}{M}} = \frac{\beta}{2} \sqrt{\frac{1}{KM}}$$



STICK / SLIP CONDITION

$$\bar{v}_{HW} > v$$



STICK / SLIP THRESHOLD  
(BOUNDARY CONDITION)

$$v_1 = \sqrt{a_0 x_0} \sin\left(\sqrt{\frac{a_0}{x_0}} \tau\right) ; \frac{dv_1}{dt} = a_1$$

$$a_1 = a_0 \cos\left(\sqrt{\frac{a_0}{x_0}} \tau\right) = a_0 \sqrt{1 - \frac{v^2}{a_0 x_0}} ; \frac{da_1}{dt} = -a_0 \sqrt{\frac{a_0}{x_0}} \sin\sqrt{\frac{a_0}{x_0}} \tau$$

$$\boxed{\tau_1 = \frac{\pi}{2} \sqrt{\frac{x_0}{a_0}}}$$

$$v_1 = \sqrt{a_0 x \left(2 - \frac{x}{x_0}\right)} ; a_1 = a_0 - \frac{a_0}{x_0} x$$

$$\frac{dv_1}{dx} = \sqrt{\frac{a_0}{x}} \frac{\left(1 - \frac{x}{x_0}\right)}{\sqrt{2 - \frac{x}{x_0}}} ; \frac{da_1}{dx} = -\frac{a_0}{x_0}$$

$$v_{MAX} = \sqrt{a_0 x_0}$$

$$\boxed{\tau_2 = \frac{2x_0}{\bar{v}} - 2\tau_1}$$

WHEN  $\tau_2 = 0$   $\bar{v} = \bar{v}_{MIN}$  (STICK SLIP THRESHOLD)

$v > \bar{v}_{MIN}$  DEFINES SMOOTH VELOCITY!

$$\bar{v}_{MIN} = \frac{2}{\pi} \sqrt{a_0 x_0} ; x = x_0 \left(1 - \frac{a_0}{a}\right) = x_0 \left(1 - \sqrt{1 - \frac{v^2}{a_0 x_0}}\right)$$

$x_0 = \frac{F - F_0}{k}$  ; LET  $F = F_s =$  STATIC FRICTION FORCE

$$\boxed{x_0 = \frac{F_s - F_0}{k}}$$

LET  $\mu = \frac{F_s}{F_0}$

$$\boxed{x_0 = \frac{\mu - 1}{k} F_0}$$

$$a_0 = \frac{1}{M} (F_s - F_0) ; \boxed{a_0 = \frac{F_0}{M} (\mu - 1)}$$

SINCE  $F_0 = \mu W = \mu M g$  AND  $\frac{1}{\omega} = \sqrt{\frac{M}{k}}$

$$x_0 = \frac{(\mu - 1) \mu W}{k} = \frac{(\mu - 1) \mu M g}{k} = \frac{M g (\mu - 1)}{\omega_n^2}$$

$$\bar{v}_{MIN} = \frac{2 \mu W}{\pi \sqrt{M k}} (\mu - 1) = \frac{2 \mu g}{\pi} \sqrt{\frac{M}{k}} (\mu - 1) = \frac{2}{\pi} \frac{\mu g}{\omega_n} (\mu - 1)$$

$$\bar{V}_{\text{MIV}} = \frac{2}{\pi} \sqrt{\frac{F_D}{M} (R-1) \frac{(R-1)}{K} F_D} = \boxed{\frac{2}{\pi} \frac{F_D}{\sqrt{KM}} (R-1)}$$

### PHYSICAL EXPLANATION:

DURING STICK/SLIP THRESHOLD CONDITIONS THE FORWARD MOVING MASS "M" OSCILLATES IN DISCRETE STEPS OF  $\frac{1}{2}$  CYCLES OF THE RESONANT FREQUENCY OF THE SPRING-MASS SYSTEM, REPEATING EACH  $\frac{1}{2}$  CYCLE IN SUCCESSION, SINCE  $T_2 = 0$ . ANY VELOCITY ABOVE THIS THRESHOLD VELOCITY HAS TO BE CONSIDERED AS SMOOTH SINCE FORWARD MOTION IS CONTINUOUS.

AS THE RESONANT FREQUENCY OF THE SIMPLE SPRING-MASS SYSTEM IS :

$$f_n = \frac{1}{2\pi} \sqrt{\frac{K}{M}}$$

AND THE FORCE AVAILABLE DUE TO THE WINDUP OF THE SYSTEM WHEN THE APPLIED FORCE EQUALS THE STATIC FRICTION FORCE " $F_S$ " AND THE STORED ENERGY IS RELEASED AS F IS REDUCED TO THE DYNAMIC FRICTION FORCE " $F_D$ ", IS :

$$x_0 = \frac{F_S - F_D}{K}$$

THE STICK/SLIP VELOCITY THRESHOLD BECOMES :

$$\bar{V}_{\text{MIV}} = 4 x_0 f_n$$

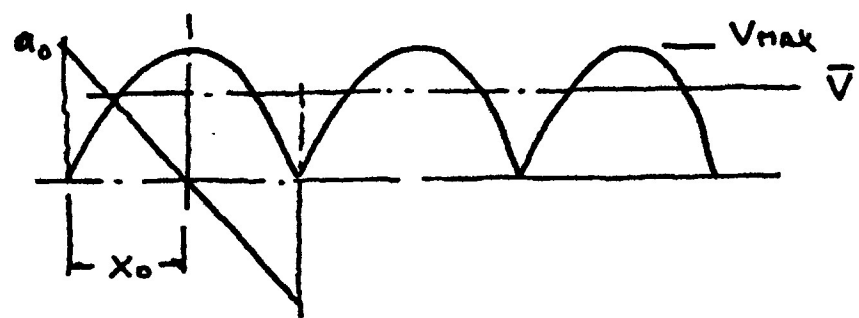
$$\bar{V}_{\text{MIV}} = \frac{4(F_S - F_D)}{K} \frac{1}{2\pi} \sqrt{\frac{K}{M}} \quad ; \quad \text{LET } R = \frac{F_S}{F_D}$$

$$\boxed{\bar{V}_{\text{MIV}} = \frac{2}{\pi} \frac{F_D}{\sqrt{KM}} (R-1)}$$

$$V_{\text{SMOOTH}} > \bar{V}_{\text{MIV}}$$

MINIMUM-SMOOTH VELOCITY AND POSITION ERROR:

CONSIDER STICK/SLIP MOTION THRESHOLD:



$$R = F_s / F_D = M_{TS} / M_{TD}$$

$$x_0 = \frac{R-1}{K} M_{TD}$$

$$a_0 = \frac{M_{TD}}{I} (R-1)$$

$$\bar{V}_{MIN} = \frac{2 M_{TDYN}}{\pi \sqrt{KI}} (R-1)$$

$$M_{TDYN AZ} = \underline{20,000} \text{ FT-LB, MIN.} ; 15.56^2 (172) + 20,000 = \underline{61,644} \text{ FT-LB, MAX.} @ \text{ CONDITION I}$$

$$M_{TSTAT. AZ} = 1.5 \times 20,000 = \underline{30,000} \text{ FT-LB, MIN.} ; \underline{71,644} \text{ FT-LB MAX}$$

$$R_{MAX} = \frac{30,000}{20,000} = \underline{1.5} ; R_{MIN} = \frac{71,644}{61,644} = \underline{1.16} \text{ MIN}$$

$$I_{AZ} = 43.8 \times 10^6 \text{ SLUG-FT}^2 \text{ (INCLD. MOTOR)}$$

$$K_{AZ} = 1.68 \times 10^{10} \text{ FT-LB/RAD}$$

$$\bar{V}_{MIN AZ(1)} = \frac{2 (20,000)}{\pi \sqrt{1.68 \times 10^{10} \times 43.8 \times 10^6}} (1.5-1) = 7.42 \times 10^{-6} \text{ RAD/SEC} = \underline{.000425} \text{ } ^\circ \text{/SEC}$$

@ 0 WIND VELOCITY

$$\bar{V}_{MIN AZ(2)} = \frac{2 (61,644)}{\pi \sqrt{1.68 \times 10^{10} \times 43.8 \times 10^6}} (1.16-1) = 7.32 \times 10^{-6} \text{ RAD/SEC} = \underline{.000419} \text{ } ^\circ \text{/SEC}$$

@ 15.56 MPH

$$x_{0(1)} = \frac{1.5-1.0}{1.68 \times 10^{10}} 20,000 = 5.95 \times 10^{-7} \text{ RAD} = \underline{.125} \text{ ARC SEC}$$

$$2 x_{0(1)} = .25 \text{ ARC SEC (DISCRETE STEPS)} = \text{UNCONTROLLABLE DYNAMIC POINTING ERROR @ AZ}$$

$$X_{0(2)} = \frac{1.16-1}{1.60 \times 10^{10}} 61,644 = 5.87 \times 10^{-7} \text{ RAD} = \underline{.12 \text{ ARC SEC}}$$

$2 X_{0(2)} = \underline{.24 \text{ ARC SEC}}$  @ 15.56 MPH, UNCONTROLLABLE DYNAMIC POINTING ERROR @ AZ

$$I_{ELEV} = 41.18 \times 10^6 \text{ SLUG-FT}^2 \text{ (INCLD. MOTOR)}$$

$$K_{ELEV} = .942 \times 10^{10} \text{ FT-LB/RAD}$$

LET :  $M_{TDYN EL} = \underline{10,000 \text{ FT-LB, MIN.}} ; \underline{51,644 \text{ FT-LB, MAX}}$

$M_{TSTAT. EL} = \underline{15,000 \text{ FT-LB, MIN.}} ; \underline{56,644 \text{ FT-LB, MAX}}$

$$R_{MAX} = \frac{15,000}{10,000} = \underline{1.5} ; R_{MIN} = \frac{56,644}{51,644} = \underline{1.10}$$

$$\bar{V}_{MIN EL(1)} = \frac{2(10,000)}{\pi \sqrt{.942 \times 10^{10} \times 41.18 \times 10^6}} (1.5-1) = 5.11 \times 10^{-6} \text{ RAD/SEC} = \underline{.000293 \text{ }^\circ/\text{SEC}}$$

@ 0 MPH

$$\bar{V}_{MIN EL(2)} = \frac{2(51,644)}{\pi \sqrt{.942 \times 10^{10} \times 41.18 \times 10^6}} (1.10-1) = 5.24 \times 10^{-6} \text{ RAD/SEC} = \underline{.0003 \text{ }^\circ/\text{SEC}}$$

@ 15.56 MPH

$$2 X_{0(1)} = 2 \frac{(1.5-1.0)}{.942 \times 10^{10}} \times 10,000 = 1.06 \times 10^{-6} \text{ RAD} = \underline{.22 \text{ ARC SEC}}$$

@ 0 MPH

$$2 X_{0(2)} = 2 \frac{(1.10-1)}{.942 \times 10^{10}} \times 51,644 = 1.10 \times 10^{-6} \text{ RAD} = \underline{.23 \text{ ARC SEC}}$$

@ 15.56 MPH

THESE ESTIMATED MINIMUM SMOOTH VELOCITIES AND DISCRETE STEP MOTIONS ARE BASED ON THE ASSUMPTION THAT THE STATIC (BREAK OUT) FRICTION LOSSES ARE 50% HIGHER THAN THE DYNAMIC LOSSES RELATIVE TO THE INHERENT AXIS FRICTION LOSSES ONLY. THIS IS CONSIDERED TO BE REALISTIC SINCE THE AVERAGE DIFFERENCE BETWEEN STATIC AND DYNAMIC EFFICIENCY OF A WELL DESIGNED GEAR BOX IS AROUND 4%.

THE STICK/SLIP MOTION IS CHARACTERIZED AS  $\frac{1}{2}$  CYCLE STEP FORWARD MOTION WHERE THE 2 STEP FREQUENCY SHOULD EQUAL THE LOCKED ROTOR RESONANT FREQUENCY OF THE SYSTEM :

$$f_{\text{STICK/SLIP (AZIM)}} = \left(\frac{1}{2}\right) \frac{7.42 \times 10^{-6}}{2 \times 5.95 \times 10^{-7}} = \underline{3.12 \text{ CPS}} \quad \left(\text{VS. } 3.11 \text{ LOCKED ROTOR FREQUENCY CALCULATED,}\right)$$

$$f_{\text{STICK/SLIP (ELEV)}} = \frac{1}{2} \frac{5.11 \times 10^{-6}}{1.06 \times 10^{-6}} = \underline{2.41 \text{ CPS}} \quad \left(\text{VS. } 2.41 \text{ LOCKED ROTOR FREQUENCY CALCULATED,}\right)$$

### STEPPING ACCELERATIONS :

$$\textcircled{a} \text{ AZ : } a_{\text{STEP}} = \frac{20,000}{43.8 \times 10^6} \cdot 5 = 2.28 \times 10^{-4} \frac{\text{RAD}}{\text{SEC}^2} = \underline{.013 \text{ }^\circ/\text{SEC}^2}$$

$$\textcircled{a} \text{ ELEV : } a_{\text{STEP}} = \frac{10,000}{41.18 \times 10^6} \cdot 5 = 1.214 \times 10^{-4} \frac{\text{RAD}}{\text{SEC}^2} = \underline{.007 \text{ }^\circ/\text{SEC}^2}$$



**NORTHERN PRECISION LABORATORIES, INC.**

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October 21, 1983

Systems Development Laboratories  
13372 Talle-Colina  
Poway, California 92064

Attention: Mr. Otto R. Heine

Reference: Telecon Heine/Nigro

Dear Mr. Heine:

Thank you for your interest in Northern Precision Laboratories' product line. Per our recent telephone conversation, enclosed please find copies of Northern Precision Laboratories' most recent Encoder and Drive literature. I have also enclosed a copy of a letter I previously sent to Mr. William Horn at National Radio Astronomy Observatory and some of our drawings which I feel may be of some assistance.

Should you have any questions or require additional information, please do not hesitate to contact me at your convenience.

Very truly yours,

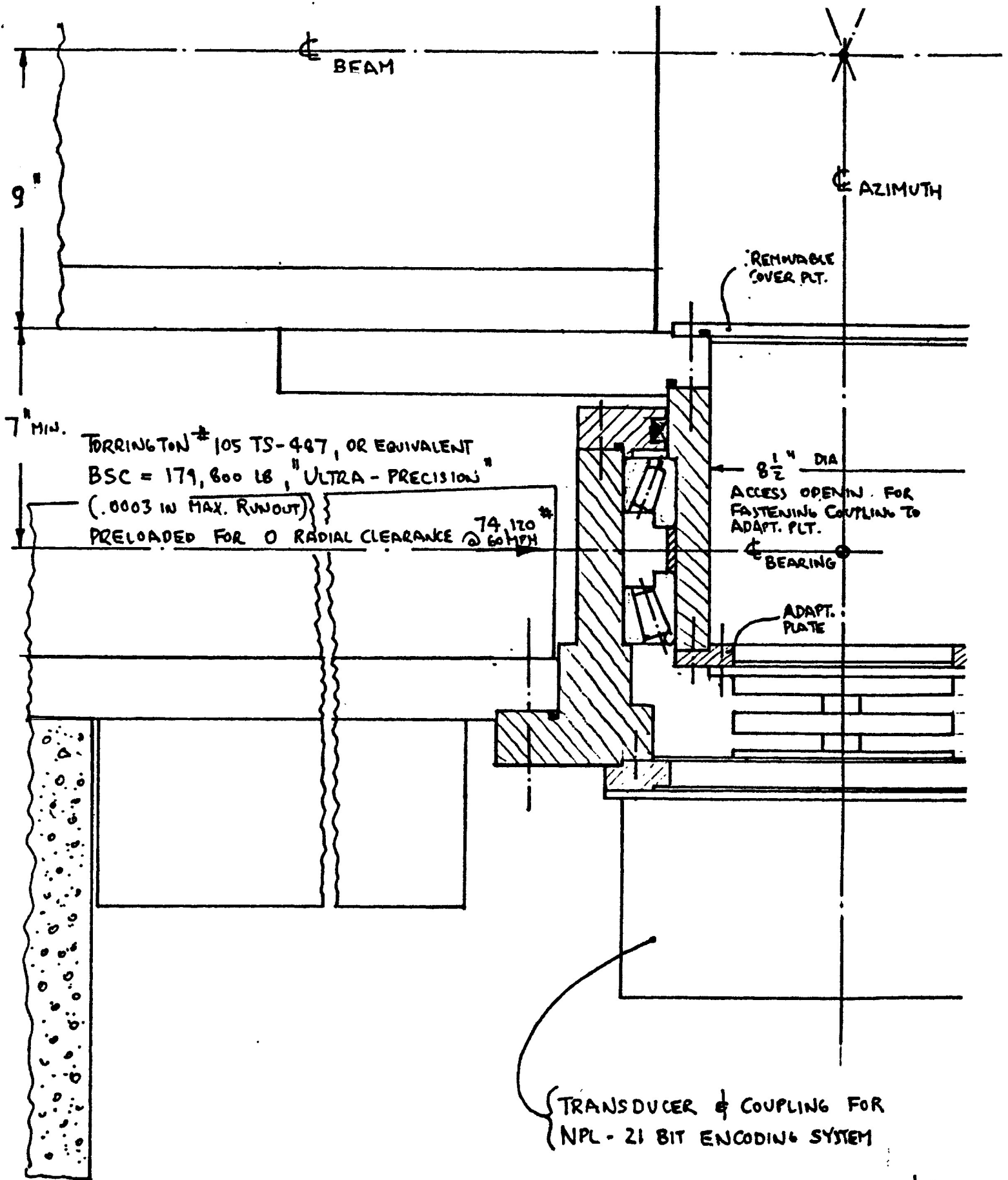
NORTHERN PRECISION LABORATORIES, INC.

Michael P. Nigro  
Product Development

MPN:nls

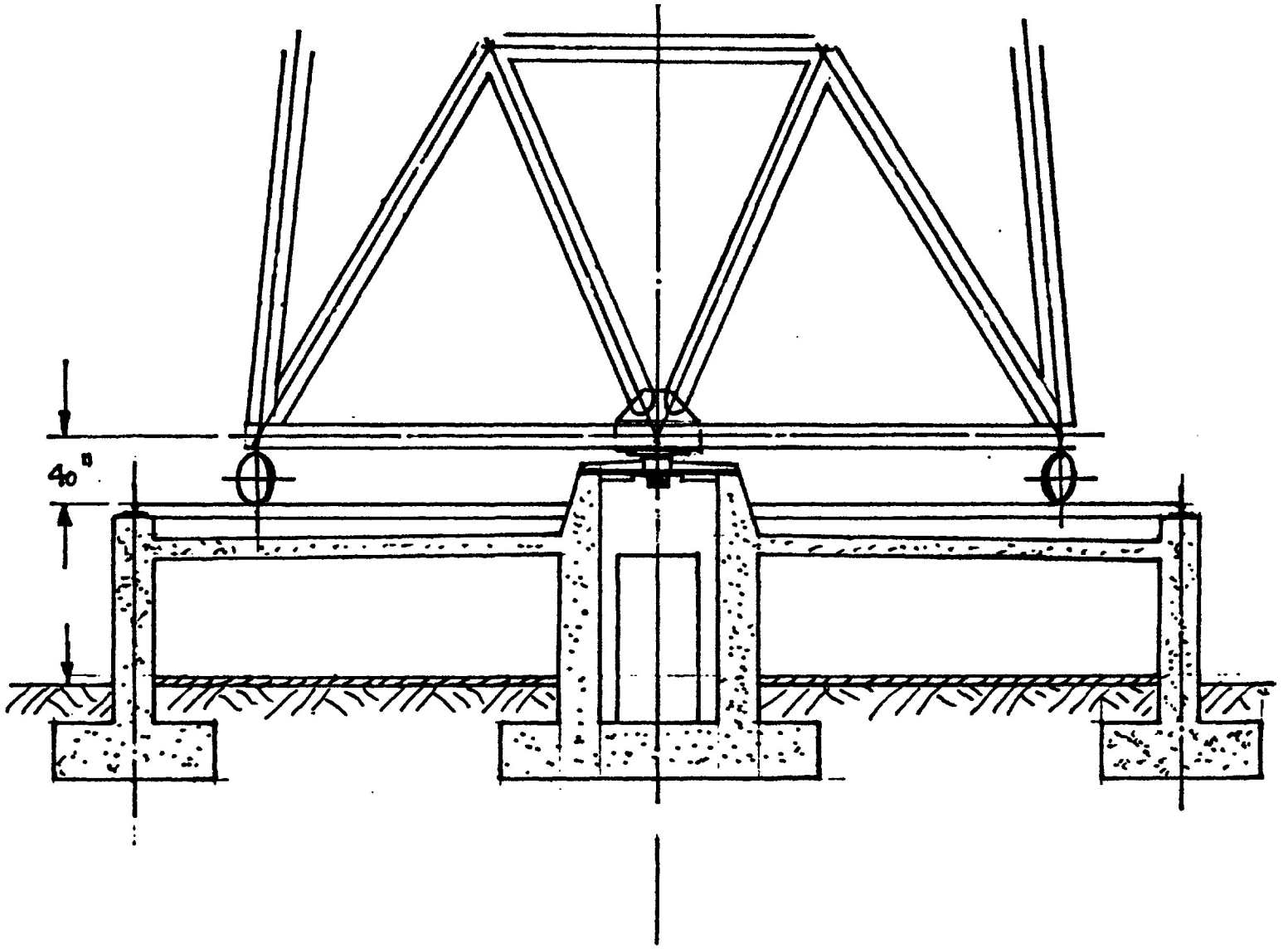
Encls. Catalogs 82900, 78900,  
Model 25 10HP SCR Servo Amplifier  
Drawings 801404-1, 801342-1,  
801342-2, 801908  
Copy of NRAO Letter 8/31/83



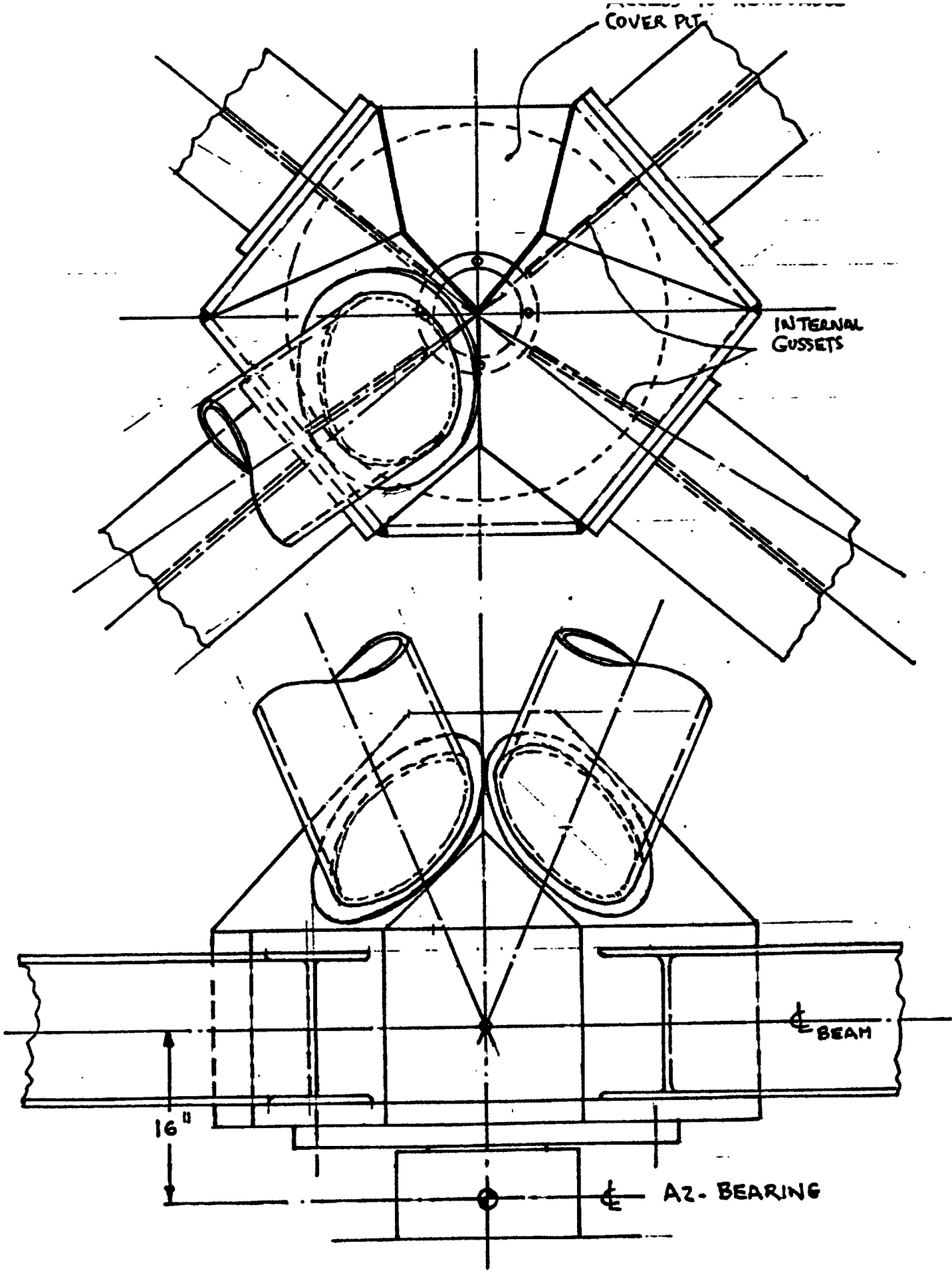


SCALE : 1/4

VLBA - AZIMUTH PINTLE BEARING



VLBA - AZIMUTH BEARING & TRACK



# Systems Development Laboratory

ENGINEERING CONSULTANTS

13372 CALLE COLINA

POWAY, CALIFORNIA 92064

(714) 485-5657

Mr. Anthony Tartaglio  
Sales Manager, Enclosed Drives  
PHILADELPHIA GEAR CORPORATION  
181 South Gulph Road  
King of Prussia, PA 19406

November 2, 1983

Dear Mr. Tartaglio:

Enclosed is a 1/4 scale sketch showing the preferred Azimuth Drive Arrangement for the VLBA Antenna, option # 4 as indicated in my letter of October 12. Please review this concept and let me know at your earliest convenience whether the VLA Elevation Drive Gear Box can be modified and mounted as shown on the sketch or whether the 30 inch diameter drive wheel would have to be provided with its own bearings?

I am assuming that the VLA Elevation Drive Gear Box Ratio could easily be reduced from the present 541:1 to 450:1 by changing the input stage ratio and that mounting the reducer overhead and at a slight incline would not be problematic.

At the present time I feel that utilizing the VLA Elevation Drive Gear Box for both the Elevation- and Azimuth Drives of the VLBA Antenna would be the most cost effective and practical solution in this case. Please concentrate your efforts on this concept and provide the information on options 1,2 and 3 at a later date. As mentioned before, the VLBA Elevation Drive Gear Boxes would be identical to the VLA Units with exception that the input speed would be raised to 2322 RPM and the maximum drive torque required would be 170,300 in-lb at 774 RPM.

Very truly yours,

SYSTEMS DEVELOPMENT LABORATORY

Otto R. Heine

cc.: William G. Horne, NRAO

