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A DIRECTIONAL FILTER FOR LOCAL OSCILLATOR INJECTION IN A MILLIMETER-WAVE MIXER RADIOMETER

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ABSTRACT

The advent of mixer radiometers with large tuning ranges operating at a wavelength of three millimeters creates the need for a local oscillator injection scheme which will provide low signal power and local oscillator power losses over the entire operating range of the receiver. The purpose of this paper is to report on the development of a directional filter for use in an 80-120 GHz mixer radiometer. A unique use of the mode properties of a resonant ring filter allows a very wide tuning range (85-115 GHz LO) with little degradation in filter performance. The directional nature of the filter, together with the resonant characteristic, provides both low signal path loss (0.2 dB) and low local oscillator path loss (4 dB).

I. BACKGROUND

The proposed radiometer will tune continuously from 80 to 120 GHz (signal frequency) with an IF frequency of 4.75 GHz and an instantaneous bandwidth of 650 MHz. The first stage of the receiver is a broadband diode mixer with no RF tuning, allowing both the signal and image bands to be down converted to the IF. The entire front end and first IF amplifier will be cooled to 20° K to improve the noise performance. A method of supplying the local oscillator power to the mixer is required. The injection scheme must provide a low loss path for the signal and the image simultaneously and should provide a reasonable loss in the local oscillator path because of local oscillator power limitations. The injection scheme must cover the entire operating range of the receiver and, if tunable, must be adjustable remotely without opening the

dewar.

The traditional solution to the problem of local oscillator injection is presented in Figure 1. The directional coupler is chosen to provide the least signal loss due to coupling, consistent with available local oscillator power. A typical coupler for use in a 100 GHz receiver will have a -10 dB coupling factor and a mainline resistive loss of about 0.5 dB. The total signal power loss for this coupler is about 1 dB (0.55 dB coupling loss + 0.5 dB resistive loss), representing a significant decrease in receiver sensitivity. The local oscillator power loss is about 10 dB. The broadband nature of the coupling allows receiver operation over essentially the full waveguide band with no tuning required. The directional coupler represents an inexpensive, broadband solution to the problem of local oscillator injection; however, a solution yielding a lower signal path and local oscillator loss would be desirable. There exist several other techniques for injecting the local oscillator power, each with its attendant disadvantages.

II. RING FILTER

The proposed solution to the problem of local oscillator injection is presented in Figure 2. The injection filter is a 4-port device consisting of a traveling-wave resonant ring filter tuned to the local oscillator frequency and two directional couplers. The signal power is coupled from port 2 to port 3. The local oscillator power is coupled from port 1 to the resonant ring via one directional coupler and then to port 3 via the second directional coupler. The directional nature of the couplers prevents the flow of local oscillator power to ports 2 and 4, while the resonant ring prevents the coupling of signal power from port 2 to ports 1 and 4. Signal power loss is limited to resistive loss in the 2 to 3 path. There is virtually no signal loss due to coupling because of the resonant nature of the ring and the signal-local oscillator

frequency separation. Local oscillator power loss is limited to the resistive loss in the resonant ring. The resonant frequency of the ring filter is varied by altering the guide wavelength in the waveguide forming the ring. This directional filter represents a low loss solution to the problem of local oscillator injection.

The design of the traveling-wave filter is based largely on the work of Coale (1) and Tischer (2). The ring is formed by a circular section of rectangular waveguide (TE₁₀) which is closed upon itself to form a ring. The waveguide ring is split along the center line of the broad wall of the waveguide. This allows the broad dimension, and hence the guide wavelength in the ring, to be varied for tuning. Power is coupled into and out of the ring through two narrow-wall multi-hole couplers. For a ring of broad dimension <u>a</u> and mean circumferential length, L, the resonant wavelength, λ , is given approximately by (1):

$$\lambda_{\rm res} = \frac{1}{\sqrt{n^2/L^2 + 1/4a^2}}$$

where n represents the integer number of wavelengths around the ring at resonance. For a given guide width, a, there are an infinite number of resonances which will couple power from port 1 to port 3. The first few are shown in Figure 3. As we alter the guide width the "comb structure" representing the filter transmission modes moves along the frequency axis. One can operate the filter over any tuning range by increasing the ring waveguide width, a. There are three pertinent points to be noted.

The first point involves the restrictions which must be placed on the number of wavelengths, n, which one can fit around the ring. For a given guide wavelength there is a lower limit placed on the circumference of the ring, and

hence n, by the requirement that two directional couplers be realized along this circumference. The upper limit is placed on n by the minimum mode spacing requirements and loss considerations. The longer the guide, the greater the local oscillator power transmission loss and the smaller the mode spacing.

The second point involves the allowable range of the guide width, a. If the guide width is too narrow the guide wavelength becomes too long to be of use and the loss increases. As the guide width is increased to effect the tuning of the filter a gap appears between the ring halves. As the width of the gap increases, power is coupled through the gap, representing a loss, significantly lowering the cavity Q thereby increasing the transmission loss of the filter.

The third point involves the presence of more than one transmission frequency or mode. Multiple modes do not seriously affect the local oscillator to mixer coupling; however, if a mode were to fall in either the signal or image frequency band some power would be coupled from port 2 to port 4 representing a loss in the input path, decreasing the receiver sensitivity.

The practical filter is limited in tuning range by the finite range of the guide width, a, and the limitations placed on the mode number, n. As an example consider the following design, based on the receiver requirements listed above. Consideration of the above points, in particular the third point, leads to the following choices for the ring parameters:

> n = 16 L = 3" a = .085" to .125" (.040" gap)

The tuning range of this filter will then be:

a = .085'' = .126''f = 93.7 GHza = .125'' = .150''f = 78.6 GHz

This represents a fractional tuning range of less than 20%, far short of the

40% (80-120 GHz) required for receiver operation. The gap of .040" would represent a large power loss, considerably affecting the transmission loss of the filter. The gap in the ring must be kept small.

One solution to this problem is to note that any of the resonances may be used. It is not necessary to move one resonance, as was done in the example above, to achieve the tuning range. It is necessary only to move the n^{th} resonance to the frequency location of the n+1 resonance. Since the entire comb moves, a large frequency range can be covered simply by choosing the proper mode and alterning the waveguide width to move that mode to the required frequency. In the example above, to move the n = 16 mode to the frequency of the n = 17 mode requires a change in guide width of .004 inches. This is a significant improvement in gap width. It is possible, using this technique, to construct a filter which has both low loss properties and a wide tuning range.

III. DESIGN

The first step in the design is the selection of the ring circumferential length, L, and the range of the ring guide width, <u>a</u>. The ring length is chosen to give the desired mode spacing consistent with coupler relizability. Care must be taken to assure that neither the image nor the signal band falls at the frequency of an adjacent mode. It is desirable to keep the ring as short as possible, in order to minimize loss. The ring waveguide width range, <u>Aa</u>, is chosen to give the tuning required to completely cover the region between the modes. Since the mode spacing and tuning rate are non-linear, care must be taken to assure that each mode covers its required range. It is desirable to choose values for <u>a</u> which yield a guide wavelength in a lower loss region of the guide attenuation curve.

The second step is the design of the couplers. It is usual to make the couplers identical. The following equation relates the transmission loss through the filter to the voltage coupling coefficient, C, and the loaded Q, Q_L, of the filter.

L (dB) = 20 log
$$\frac{1 - (1 - C^2) C^{-\alpha L}}{C^2 e^{-\alpha L/2}}$$

$$Q_{\rm L} \stackrel{\sim}{=} n\pi/C^2 10^{\rm Loss} (dB)/20$$

where α is the attenuation constant of the ring waveguide. The transmission loss of the filter is the more important of the two parameters in this case. Since we wish to minimize the local oscillator power loss the couplers will be designed accordingly. The accompanying decrease in the loaded Q is not a problem because of the high IF frequency. The coupler directivity requirement is determined from microwave circuit considerations for the case in question. The coupler is designed by any of the techniques presented in the literature.

IV. THE FILTER

The design of the filter proceeded as outlined above. To achieve a signal frequency range of 80-120 GHz the local oscillator must be tuned from about 85-115 GHz (LO above at the lower end and below at the upper end). A ring length of 3 inches was chosen to give the signal-LO-image relationship shown in Figure 4. Note that one mode has been allowed to fall between the LO (main mode) and the signal-image bands.

The couplers are chosen to each give a -10 dB coupling factor with a directivity in excess of 20 dB over the 85-115 GHz band, representing the best balance between loss and coupler relizability. The coupler design is based on the designs given by Levy (3). A Chebyshev tapered multi-hole array with circular apertures is chosen. Machining considerations dictate the use of the less efficient circular apertures. The coupling array is located in the very thin (.005 inch) common wall of the ring guide and signal/LO guides. The couplers are arranged symmetrically about the circular ring. Both couplers are mounted in the same half of the ring guide to allow for the tuning motion. The pertinent coupler dimensions are shown in Figure 5. Calculated coupler response is shown in Figures 5a and 5b.

The filter is fabricated of tellurium-copper, chosen because of its favorable machining characteristics. The filter is constructed in three pieces to allow for machining. The structure is aligned with steel guide pins. The rather odd waveguide pattern is chosen both for convenient final mounting considerations and to allow for relatively easy machining of the guides. The pattern is machined using an end mill equipped with a rotary table. The completed filter is gold plated for corrosion protection. Mechanical drawings and photographs of the filter are present in Appendix A.

The tuning of the filter presents special problems because of the high tuning sensitivity (600 GHz/inch) and the fact that the tuning must be accomplished at 20° Kelvin. The high tuning sensitivity leads to the use of a differential screw (400:1). The position of the screw is measured by a differential transformer, the core being connected to the high speed center screw of the differential pair. This type of position sensor gives the high resolution needed to measure the ring gap accurately and will operate at 20° Kelvin. A gear box is provided to interface the screw with the motor shaft in a convenient manner. Ball bearings are used throughout to minimize friction since no lubricant can be used. Careful choice of materials to minimize problems due to differential expansion is of the utmost importance.

Experience with the type of tuning mechanism described above leads to a decision to simplify the arrangement. While the above arrangement works adequately it is painfully slow. While the springs remove most of the backlash in the screw, stiction in the screw leads to a jerky tuning motion, making the tuning of the filter difficult in practice. An unexpected problem occurs when the servo fails. Since the servo remains on at all times any failure in the electronics causes the motor to drive the screw past the mechanical limits causing considerable damage to the tuning mechanism. In practice this has happened often enough to warrant attention. A step toward remedying these problems has been undertaken. Mechanical drawings and photographs of the tuning mechanism are present in Appendix B.

A new tuning mechanism is illustrated in Appendix C. The motion necessary to tune the ring is provided by a cam driven by a gear box. All gears, as well as the cam yoke, are spring loaded to remove backlash. The mechanism provides the required tuning resolution without the use of screws. The cam provides a very smooth movement without the binding tendency inherent in the differential screw. Since the cam is cyclical there are no mechanical limits which can be exceeded, causing damage to the mechanism, as with the differential screw arrangement. The mechanism is designed to be directly interchangeable with the existing mechanism. Tests on the new unit are not complete at this time.

V. ANALYSIS

A computer program to evaluate the performance of the filter is included in Appendix D. The program computes the amount of power coupled from the local oscillator port to the other three ports. An effort has been made to use the most appropriate model for the directional coupler and ring. The program is partitioned in the form of subroutines to provide for ease of implementation.

In addition to the main routines several utility routines have been included since they are not widely available. The usage should be clear from the listing. A sample problem is included. A description of each subroutine follows.

The subroutine CPLR calculates the complex reflection and coupling coefficients for two transmission lines coupled together periodically. The program utilizes a rigorous 4-port network analysis, rather than the usual weak coupling analysis, to yield accurate estimates of coupling and directivity. The analysis takes into account the dispersive nature of the transmission lines, transmission line losses, and the infinite number of waves being coupled back and forth by the coupler. The coupling coefficients of the apertures are based on Bethe's small hole theory as modified by Cohn to consider aperture resonance phenomena and the finite thickness of the wall containing the apertures. Aperture interaction due to evanescent modes is not considered. The true electrical length of the coupler is calculated to allow improved estimates of the resonant frequencies and mode spacings of the ring resonator. The analysis is based on articles by Riblat (4) and Levy (5). It should be noted that the use of this program is not limited to the coupler in question but may be used for any coupled transmission line problem by insertion of the appropriate expressions for the coupling reactances.

The conventions used are illustrated in Figure 6. Consider a wave of amplitude a₁ incident on port 1. With all ports terminated in the characteristic impedance of the transmission line the waves emerging from the four ports are as follows:

> Port 1: $b_1 = R_0 a_1$ Port 2: $b_2 = KR a_1$ Port 3: $b_3 = KH a_1$ Port 4: $b_4 = T_{12} a_1$

where R_0 , T_{12} , KR, and KH are the complex reflection and coupling coefficients. Since the coupler is symmetrical and reciprocity holds, any port may be taken as the input with the same results. Therefore, the reflection coefficient, R_0 , for all ports is the same; the thru arm forward coupling, T_{12} , is the same as the thru arm reverse coupling, T_{21} , etc. An example of the application of these quantities for the coupler as it is excited in the filter is presented in Figure 7. The figure is self-explanatory.

The subroutine FILTER calculates the power delivered to each of the other three ports with a wave of unit amplitude entering port 1. All ports are assumed terminated in their characteristic impedance. The port numbering conventions are presented in Figure 2. The analysis considers waves traveling in both directions around the ring and resistive losses in the ring. A brief description of the method is presented.

The analysis is carried out in terms of the wave cascading matrix [R]. If the amplitudes of the incident waves are a_1 and a_2 and the amplitudes of outgoing waves are b_1 and b_2 as illustrated in Figure 8, then the waves are related as follows:

 $\begin{bmatrix} a_1 \\ b_1 \end{bmatrix} = \begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} b_2 \\ a_2 \end{bmatrix}$

The ring is divided into segments, each of which is characterized by its R-cascading matrix. Figure 9 illustrates the segmentation. The length of the coupler waveguides which are part of the ring is just the number of coupling holes times the hole spacing. The length of the waveguides which connect the two couplers to form the ring is half the balance necessary to make up the ring. Thus,

2 (# holes x hole spacing + length connecting guide) = L.

The upper directional filter is characterized as a 2-port with accompanying R matrix. This is allowed if we restrict incident waves to ports 1 and 2. The R matrix for this portion of the ring is:

$$\begin{bmatrix} a_1 \\ b_1 \end{bmatrix} = \frac{1}{T_{12}} \begin{bmatrix} 1 & -R_0 \\ \\ \\ R_0 & T_{12}^2 - R_0^2 \end{bmatrix} \begin{bmatrix} b_2 \\ \\ \\ a_2 \end{bmatrix}$$

where the quantities are defined as above.

The two sections of connecting waveguide are represented by:

$$\begin{bmatrix} a_1 \\ b_1 \end{bmatrix} = \begin{bmatrix} e^{\Gamma L} & 0 \\ 0 & e^{-\Gamma L} \end{bmatrix} \begin{bmatrix} b_2 \\ a_2 \end{bmatrix}$$

where $\Gamma = \alpha + j\beta$ is the complex propagation constant.

These three elements of the ring are now cascaded to yield a representation of the upper half of the ring as illustrated in Figure 10. The R matrix for the entire structure is:

$$\begin{bmatrix} a_1 \\ b_1 \end{bmatrix} = \frac{1}{T_{12}} \begin{bmatrix} e^{\Gamma L} & 0 \\ 0 & e^{-\Gamma L} \end{bmatrix} \begin{bmatrix} 1 & -R_0 \\ R_0 & T_{12}^2 - R_0^2 \end{bmatrix} \times \begin{bmatrix} e^{\Gamma L} & 0 \\ 0 & e^{-\Gamma L} \end{bmatrix} \begin{bmatrix} b_2 \\ a_2 \end{bmatrix}$$

The upper portion of the ring is interfaced with the lower portion using the conventions illustrated in Figure 11. With the coupler parameters as defined above the relations among the various waves are:

 $b_{1} = a_{1} R_{0} + a_{3} KH + a_{4} KR$ $b_{2} = a_{1} T_{12} + a_{3} KR + a_{4} KH$ $b_{3} = a_{1} KH + a_{3} R_{0} + a_{4} T_{12}$ $b_{4} = a_{1} KR + a_{3} T_{12} + a_{4} R_{0}$

We now define the matrix:

$$\begin{bmatrix} R_{11} & R_{12} \\ \\ R_{21} & R_{22} \end{bmatrix} = \frac{1}{T_{12}} \begin{bmatrix} e^{\Gamma L} & 0 \\ \\ 0 & e^{-\Gamma L} \end{bmatrix} \begin{bmatrix} 1 & -R_0 \\ \\ R_0 & T_{12}^2 - R_0^2 \end{bmatrix} \begin{bmatrix} e^{\Gamma L} & 0 \\ \\ 0 & e^{-\Gamma L} \end{bmatrix}$$

Then solving the following for ${\bf a}_3^{}$ and ${\bf a}_4^{}$

$$\begin{bmatrix} a_{3} \\ b_{3} \end{bmatrix} = \begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} b_{4} \\ a_{4} \end{bmatrix}$$

yields

$$a_{3} = (R_{21} - R_{22} R_{11}/R_{12}) b_{4} + \frac{R_{22}}{R_{12}} b_{3}$$
$$a_{4} = \frac{b_{3} - R_{11} b_{4}}{R_{12}}$$

which when substituted in the set of four simultaneous equations above yields in matrix form:

$$\begin{bmatrix} -a_{1}KR \\ -a_{1}KH \\ -a_{1}KH \\ -a_{1}T_{12} \\ -a_{1}R_{0} \end{bmatrix} = \begin{bmatrix} 0 & 0 & (R_{0}/R_{12} + R_{22} T_{12}/R_{12}) & \left\{ \left[T_{12} \left(R_{21} - \frac{R_{22}}{R_{12}} R_{11} \right) - \frac{R_{0}}{R_{12}} \right] - 1 \right\} \\ 0 & 0 & (R_{0} R_{22}/R_{12} + T_{12}/R_{12} - 1) & \left[R_{0} \left(R_{21} - \frac{R_{22}}{R_{12}} R_{11} \right) - \frac{T_{12}R_{11}}{R_{12}} \right] \\ 0 & -1 & \left(\frac{KR R_{22}}{R_{12}} + \frac{KH}{R_{12}} \right) & \left[KR \left(R_{21} - \frac{R_{22}}{R_{12}} R_{11} \right) - \frac{KH R_{11}}{R_{12}} \right] \\ -1 & 0 & \left(\frac{KH R_{22}}{R_{12}} + \frac{KR}{R_{12}} \right) & \left[KH \left(R_{21} - \frac{R_{22}}{R_{12}} R_{11} \right) - \frac{R_{11}}{R_{12}} KR \right] \end{bmatrix} \\ \begin{bmatrix} b_{1} \\ b_{2} \\ b_{3} \\ b_{4} \end{bmatrix}$$

This represents a set of four simultaneous equations in four unknowns. If we call the 4 x 4 matrix BFM, then

$$\begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \end{bmatrix} = \begin{bmatrix} BFM^{-1} \end{bmatrix} \begin{bmatrix} -a_1 & KR \\ -a_1 & KH \\ -a_1 & T_{12} \\ -a_1 & R_0 \end{bmatrix}$$

We now have an expression for the four waves necessary to completely characterize the filter. Waves b_3 and b_4 characterize the output side of the filter. Waves b_1 and b_2 characterize the input side of the filter. Output waves b_5 and b_6 can be found as follows: Waves b_3 and b_4 represent the waves at the exits of the input coupler. These waves are transformed around the ring to the input of the output coupler and then:

> $b_5 = a_4' KH + a_3' KR$ $b_6 = a_4' KR + a_3' KH$

where the primed quantities are the waves after transformation around the ring as described above. Waves b_1 and b_2 are the outward flowing waves in the input coupler main line.

The quantities used in the above analysis are complex; consequently the programs are written to handle complex expressions. Several mathematical functions such as the complex hyperbolic sine and a routine for the inversion of a complex matrix were not available on the system used by myself. The subroutines were written and are included. The methods used are straightforward. The matrix inversion is accomplished using the standard Gauss-Jordon pivoted method, with thanks to IBM. These routines are general and may be useful elsewhere. Plotting routines have not been included as they are very system dependent.

VI. RESULTS

The measured response of the filter at room temperature is presented in Figures 12 and 13. No measurements of the antenna port to mixer port loss is included due to the difficulty of measuring these small quantities accurately in this frequency range. The signal loss is about .3 dB. There is a slight improvement in local oscillator transmission loss when the filter is cooled to 20° Kelvin. The filter response agrees fairly well with the design. The discrepancies are thought to be due largely to inaccuracies in the coupler design and the uncertainty in the high frequency value of the skin depth. The overall response of the filter is considered to be very good, representing a significant improvement over other injection schemes.

The choice of the mode spacing together with the mode characteristics of the filter yield a filter without spurious modes. This property allows for ease of tuning. Mechanical limits prevent the filter from being tuned more than one mode spacing. This assures that at any operating frequency the filter need be tuned only to the closest mode without fear of reduced filter performance due to mode selection errors. In practice one need not be concerned with which mode he is operating on.

This injection filter represents an improved solution to the problem of local oscillator injection in millimeter wave radiometers. The filter gives excellent electrical and mechanical performance and can be implemented with moderate efforts, as compared to other schemes. In addition to use an an LO injection filter, this type of filter has many other uses. Filters of this type are currently in use in receivers of the NRAO at Kitt Peak, Arizona.

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REFERENCES

- Coale, F., Section 14.07, p. 881, <u>Microwave Filters, Impedance-Matching</u> <u>Networks, and Coupling Structures</u>, Matthaei, Young, and Jones. New York: McGraw Hill, 1964.
- (2) Tischer, F. J., "Resonance Properties of Ring Circuits", <u>IEEE Trans.</u>
 MTT-5, pp. 51-56, 1957.
- Levy, R., "Directional Couplers", <u>Advances in Microwaves</u>, Leo Young, editor, Vol. 1, pp. 115-209. New York: Academic Press, 1967.
- Riblet, H., "A Mathematical Theory of Directional Couplers", <u>Proc. of</u> the IRE, Vol. 35, pp. 1307-1313, November 1947.
- Levy, R., "Analysis and Synthesis of Waveguide Multiaperture Directional Couplers", IEEE Trans., MTT-16, pp. 995-1006, December 1968.







Figure 2: Resonant ring filter used for local oscillator injection.



SIGNAL & IMAGE BAND RELATIONSHIPS FIG. 4











Figure 7: Power flow in coupler.



Waveguide lengths are as in example.

.630 = 15 (holes) x .042 (hole) spacing

Figure 9: Segmentation of filter.



Figure 10: Representation of upper ring and coupler.









FIG. 13 - B

APPENDIX A

MECHANICAL DRAWINGS:

INJECTION FILTER

APPENDIX A



Photo 1: Injection Filter, Internal View.







APPENDIX B

MECHANICAL DRAWINGS:

DIFFERENTIAL SCREW AND GEAR BOX



Photo 1: Differential Screw and Cap Block.



Photo 2: Cavity with Differential Screw and Cap Block Attached.





Coupling holes: Set up Rotary table so the Zero Degree - 180° line is colinear with Reference & (See dwg.no. B2576M18 Hole Ref. &) then place holes on ,475 radius about Block &'s according to following table. Rotate block 180° and Repeat



DIAMETER	.018	.028	.034	.036	,036	,036	,036	.036	.036	.036	.036	.036	.034	.028	.018	RADIO ASTRONOMY SERVATORY
GLE	0"	0	0	0	0	0	0	0	0	0	0	0	0	0	0	NATIONAL
AN	55'	59	m	2	=	15	<u>6</u>	23	27	31	35	39	43	47	51	
	146°	151	159	162	167	172	177	182	187	192	197	202	207	212	217	

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D	0	N
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		~
S		6
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2		N
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DETAIL

TITLE: COUPLER





27. 61.14

APPENDIX C

MECHANICAL DRAWINGS:

PRECISION MOVER

APPENDIX C



Photo 1: Cavity with Precision Mover Attached.









APPENDIX D

COMPUTER PROGRAMS



FORTRAN	IV	V01C-03A MON 18-AFR-77 12:54:24 FAGE 001
0001		FRUCKAR DIRCOFFICIED FUERE STARFWHITHESTARFWHIT
0001		DIMENSION FWD(303) (RC03) (103) (103) (103) (RC03) (103) (103) (RC03)
0002		DIMENSION D(20)
0003		CUMMUN A, B, D, X, TH, LEN, N, ALPHA, K
0004		REAL K1,K2,K,LEN
0005		COMPLEX RO,T12,KR,KH
0006		READ 98+N
0007		READ 100, LEN
0008		READ 100, A
0009		READ 100, B
0010		READ 100,X
0011		READ 100,TH
0012		DO 99 I=1,N
0013	99	READ 100,D(I)
0014		ALFHA = .014576
0015		K = .862
0016	100	FORMAT (F6.4)
0017	98	FORMAT (12)
0018		DO 200 I = 1,501
0019		F(I) = I
0020		$F(I) = 85 \cdot E9 + 10 \cdot E7 * (F(I) - 1 \cdot)$
0021		CALL FILTER(F(I),FWD(I),REV(I))
0022	200	F(I) = F(I)/1.E9
0023		CALL SIMPLOT(F,FWD,501,0,'FRFD GH7','FWD DB',5.0)
0024		CALL SIMPLOT (F.REV.501.0. (FRED GH7(. (REV DB(.5.0)
0025		
0026		FND
		Let 1 L

FORTE	AN IV C*DEC	V01C-03A MON 18-AFR-77 12:54:27 FAGE 001 K,FILT FAGE 001
0001		SUBROUTINE FILTER(F,FWD,REV)
	С	
		COMPUTES FOWARD (MIXER) AND REVERSE (ANTENNA) COUPLED POWER FOR RESONANT RING INJECTION FILTER VS FREQUENCY. F = FREQUENCY IN GHZ FWD = FOWARD COUPLED POWER (DB) REV = REVERSE COUPLED POWER (DB)
		***NOTE - COMMON STATEMENT MUST AFFEAR IN CALLING ROUTINE
0002	C	COMMON A, B, D, X, TH, LEN, N, ALFHA, K
0003		DIMENSION D(20)
0004		DIMENSION T(2,2),R(2,2),TRM(2,2),TRIF(2,2),BFM(4,4),L(4),M(4)
0005 0006 0007 0008		REAL LEN,LAM,LAMG,K COMFLEX RO,T12,T,R,TRM,TRIF,BFM,R11,R12,R21,R22, L,M,R5,R6 COMFLEX KR,KH,DET CALL CPLR(F,R0,T12,KR,KH)
0009		LAM = 1.18E10/F
0010		LAMG = LAM/SQRT(1LAM* $*2/4./A**2$)
0011		BETA = 6.283185/LAMG
0012		$T(1+1) = CEXF(N*CMFLX(ALFHA+BETA))$ $T(2+2) = 1 \cdot (T(1+1))$
0013		T(1,2) = 0.
0015		T(2,1) = T(1,2)
0016		R(1,1) = 1./T12
0017		R(1,2) = -R0/T12
0018		R(2,1) = R0/T12
0019		$R(2_{2}2) = (T12*T12-R0*R0)/T12$
0020		CALL UMPT(K)I)(KM)2)2)2) CALL CMPY(T.TPM.TPTP.2.2.2)
0022		R11 = TRIP(1,2)
0023		R12 = TRIP(1,1)
0024		R21 = TRIF(2,2)
0025		R22 = TRIF(2,1)
0026		10 101 11 = 1,4
0027	101	DO IOI J = 1,4 BEM(11,1) = (0, 0, 1)
0029		BFM(3,2) = (-1,0,0)
0030		BFM(4,1) = (-1,0,)
0031		BFM(1,3) = RO/R12+R22*T12/R12
0032		BFM(1,4) = T12*(R21-R22*R11/R12)-R0*R11/R12-(1.,0.)
0033		BFM(2+3) = RU*R22/R12+112/R12+(1++0+) $RFM(2+4) = RU*(R21+R22*R14/R12+(1++0+))$
0035		BFM(3.3) = KR*R22/R12-KH/R12
0036		BFM(3,4) = KR*(R21-R22*R11/R12)-KH*R11/R12
0037		BFM(4,3) = KH*R22/R12+KR/R12
0038		BFM(4,4) = KH*(R21-R22*R11/R12)-R11*KR/R12
0039		CALL CMINV(BFM , 4, DET , L, M) L(1) = -KF
0010		

FORTRAN	IV	V01C-03A MON 18-APR-77 12:54:27	F÷GE	002
0041		$L(Z) = -T_1 Q$		
0042				
0043		L(4) = -RU		
0044		CALL CMFY(BFM,L,M,4,4,1)		
0045		M(3) = M(3)/T(1,1)		
0046		M(4) = M(4)/T(1,1)		
0047		R5 = M(4) * KH + M(3) * KR		
0048		R6 = M(4) * KR + M(3) * KH		
0049		REV = 10.*ALOG10(CABS(R5)**2)		
0050		FWD = 10.*ALOG10(CABS(R6)**2)		
0051		RETURN		
0052		END		

FORTRA	N IV C*DECK	V01C-03A MON 18-APR-77 12:54:35 (,CCOSH	PAGE 001
	C		
	С	COMPLEX HYPERBOLIC COSINE	
	С	X = COMPLEX ARGUMENT	
	С	***NOTE - CCOSH MUST APPEAR IN COMPLEX STATEMENT IN	CALLING PRGM
	С		
	С		
	С		
	С		
0001		COMPLEX FUNCTION CCOSH(X)	
0002		COMPLEX X,A,B	
0003		A = CEXF(X)	
0004		B=1./A	
0005		CCOSH =(A+B)/(2.,0.)	
0006		RETURN	
0007		END	

FORTR	AN IV	V01C-03A MON 18-AFR-77 12:54:37	FAGE 001
0001	0 + 1 - 1 - 0	SUBROUTINE CPLR(F,RO,T12,KR,KH)	
	С		
	с с с с с с с с с с с с	F = FREQUENCY OF COUFLER EVALUATION RO = REFLECTION COEFFICIENT AT ANY PORT OF COUPLER TERMINATED IN THE CHARACTERISTIC IMPEDANCE OF THE T12 = THROUGH ARM TRANSFER COEFFICIENT KR = REVERSE COUPLING COEFFICIENT KH = FOWARD COUPLING COEFFICIENT	(OTHER PORTS LINE)
	С	NOTE - RO, T12, KR, KH ARE COMPLEX	
	C	A = WAVEGUIDE WIDTH	
	C	D = DIAMETER OF COUPLING HOLF	
	C C C	X = DISTANCE FROM EDGE OF GUIDE TO CENTER OF COUPL TH = THICKNESS OF WALL CONTAINING COUPLING HOLE LEN = DISTANCE BETWEEN COUPLING HOLES	ING HOLE
	С	N = NUMBER OF COUPLING HOLES PER COUPLER	
	С	ALPHA = ATTENUATION CONSTANT OF WAVEGUIDE (NEPERS)	
	C		
	C		
	С		
0002		COMMON A, B, D, X, TH, LEN, N, ALPHA, A2	
0003		COMPLEX 1129KU9KK9KH9ML9GAMMA9CSINH9CCU5H	
0005		DIMENSION D(20) +M1(2+2) +M2(2+2) +M(2+2) +MT(2+2)	
0006		DIMENSION ME(2,2), MO(2,2), BZ(20), XX(20), BY(20), ML	(2,2)
0007		REAL LAM, LAMG, LEN, K1, K2	
0008		LAM = 1.18E10/F	
0009		LAMG = LAM/(SQRT(1LAM**2/4./A**2))	
0010		PU = 102 K = 19 N FOF = 1.18F10/1.305/D(K)	
0012		FOH = 1.18F10/1.705/D(K)	
0013		$A2 = (.065 \times D(K) + TH) / TH$	
0014		K1 = TAN(3.14159*F/2./FOH)/3.14159/F*2.*FOH	
		1*EXF(-6.28319*TH*A2/1.705/D(K)*SQRT(1F**2/FOH**2))
0015		K2 = TAN(3.14159*F/2./F0E)/3.14159/F*2.*F0E	
001/		1*EXF(-6,28319*/H*A2/1,305/U(K)*50K/(1,-F**2/FUE**2	
0010		YY(K)=12,54437*D(K)**3*(STN(3,14159*Y/A))**2/A/R/	H/D/LHN##2/124 Amg/A.
0018		$BZ(K) = -3.14159 \times LAMG \times D(K) \times 3 \times (COS(3.14159 \times X/A)) \times 2/$	A**3/8/6.
0019		BY(K) = BY(K) * K2	
0020		XX(K) = XX(K) * K1	
0021	102	BZ(K) = BZ(K) * K1	
0022		M1(1,1) = (1,0,0)	
0023		M1(2*1) = (0*0*)	
0025		M1(2*2) = (1**0*)	
0026		M2(1,1) = (1,0,0)	
0027		M2(1,2) = (0.,0.)	
0028		M2(2*1) = (0**0*)	
0029		M2(2,2) = (1,,0,)	
0030		GAMMA = CMPLX(ALPHA, 6, 283185/LAMG)	

FORTRAN	IV	V01C-03A MON 18-APR-77 12:54:37
0031		ML(1,1) = CCOSH(GAMMA*LEN/2)
0032		ML(1,2) = CSINH(GAMMA*LEN/2.)
0033		ML(2,1) = ML(1,2)
0034		ML(2,2) = ML(1,1)
0035		DO 103 K = 1.N
0036		ME(1,1) = (1,0,0)
0037		ME(1,2) = CMPLX(0,2,*XX(K))
0038		ME(2,1) = (0.,0.)
0039		ME(2,2) = (1.,0.)
0040		MO(1,1) = (1.,0.)
0041		MO(1,2) = (0,0,)
0042		MO(2,1) = CMPLX(0,2,*(BZ(K)+BY(K)))
0043		MO(2,2) = (1,0,)
0044		CALL CMPY(ML,ME,M,2,2,2)
0045		CALL CMFY(M,ML,ME,2,2,2)
0046		CALL CMPY(ML,MO,MT,2,2,2)
0047		CALL CMPY(MT,ML,MO,2,2,2)
0048		CALL CMPY(M1,ME,M,2,2,2)
0049		CALL CMFY(M2,M0,MT,2,2,2)
0050		$DO \ 104 \ I1 = 1,2$
0051		$DO \ 105 \ I2 = 1,2$
0052		M1(I1,I2) = M(I1,I2)
0053	105	M2(I1,I2) = MT(I1,I2)
0054	104	CONTINUE
0055	103	CONTINUE
0056		$10 \ 106 \ 11 = 1,2$
005/		$10 \ 107 \ 12 = 172$
0058		ME(I1,I2) = M(I1,I2)
0059	107	MO(11,12) = MI(11,12)
0060	106	CUNTINUE
0061		GAMMAU = (MU(1,1) - MU(2,2) + MU(1,2) - MU(2,1))
		1/(MU(1,1)+MU(1,2)+MU(2,1)+MU(2,2))
0062		GAMMAE = (ME(1,1) - ME(2,2) + ME(1,2) - ME(2,1))
		17(ME(1,1)+ME(1,2)+ME(2,1)+ME(2,2))
0063		TU = (2, j0,)/(MU(1, j1)+MU(1, j2)+MU(2, j1)+MU(2, j2))
0084		1E = (2**)(*)/(ME(1*1)+ME(1*2)+ME(2*1)+ME(2*2))
0065		$KH = (IE - IU)/(2 \cdot y U \cdot)$
0066		NK = (GAMMAE - GAMMAD) / (2 + y 0 +)
0067		RU = (UARRALTE)/(2 + yV +)
0000		$\frac{112}{\text{DETIDAL}} = \frac{10112772*70*7}{\text{DETIDAL}}$
0007		
0070		E NT

FORTRAN	IV	V01C-03A MON 18-APR-77 12:54:45
C*	DECH	<pre>CMPY</pre>
0001		SUBROUTINE CMPY(A,B,C,I,J,K)
С		MULTIFLIES COMPLEX MATRICES A*B = C
С		I = NUMBER OF ROWS IN A
С		J = NUMBER OF COLUMNS IN A
С		K = NUMBER OF COLUMNS IN B
0002		COMPLEX A,B,C
0003		DIMENSION A(I,J),B(J,K),C(I,K)
0004		DO 101 L=1,I
0005		DO 100 M = 1 K
0006	100	$C(L_{y}M) = (O_{y}O_{y})$
0007	101	CONTINUE
0008		DO 104 L = 1, I
0009		DO 103 M = $1, K$
0010		DO 102 N = 1, J
0011	102	$C(L,M) = C(L,M) + A(L,N) \times B(N,M)$
0012	103	CONTINUE
0013	104	CONTINUE
0014		RETURN
0015		END

PAGE 001

FORTR	AN I	V	VO1C-03A	MON 18-AFF	-77 12:54:43	7	PAGE 001
0001	C#1	ECN	SUBBOUTTNE CMT	NU(A.N.TI.I.	M		
0001	C		SOTITOOLITIKE OUT				
	C						
			INVERTS A COMP	LEX MATRIX	TO BE INVER	TED. MAT	RIX A IS WRITTEN
	C		OVER WITH THE	INVERSE OF	A.		
	L C		N = OKUER OF P	T OF WATEL			E TERTED FOR
	C		CTNCULADITY)	I OF MAINIZ		0+ 1141 D	
			SINGULANIII+7	V OF LENGTH			
			L - WURK MATET	V OF LENGT	1 14		
				TEC EVOCET		EV. N TC	THITEGEDWWW
	L C		***ALL QUANIII	IES EXCEPT	N ARE CONFLI	EV) N 10	INTEGERAAA
	C .						
	с С						
	C C						
0002	U		DIMENSION A(1)	,L(1),M(1)			
0003			COMPLEX A,BIG	A, HOLD, D			
0004			D = (1, 0, 0)				
0005			NK = -N				
0006			DO 80 K = 1,N				
0007			NK = NK + N				
0008			L(K) = K				
0009			M(K) = K				
0010			KK = NK + K				
0011			BIGA = A(KK)				
0012			$DO 20 J = K_{PN}$				
0013			$1Z = N \times (J - 1)$				
0015			$T_{1} = T_{7} + T_{7}$				
0016		10	IF(CABS(BIGA)-	CABS(A(IJ))) 15,20,20		
0017		15	BIGA = A(IJ)				
0018			L(K) = I				
0019			M(K) = J				
0020		20	CONTINUE				
0021			J = L(K)	OF			
0022		25	1F(J=K) 309309 KT = K=N	20			
0024		20	$T_{10} = 1 \cdot N$				
0025			KT = KT + N				
0026			HOLD = -A(KI)				
0027			JI = KI - K + J				
0028			A(KI) = A(JI)				
0029		30	A(JI) = HOLD				
0030		35	I = M(K)	70			
0031		70	1F(1-K) 45,45,	38			
0032		38	$Jr = N \pi (I - I)$				
0034			1K = NK + 1				
0035							
0036			HOLD = -A(JK)				
0037			A(JK) = A(JI)				
0038		40	A(JI) = HOLD				

FORTRAN	IV	V01C-03A MON 18-APR-77 12:54:47
0039	45	IF(CABS(BIGA)) 48,46,48
0040	46	$\Pi = (0 \cdot \cdot 0 \cdot)$
0041	40	
0042	48	10 00 I - INN 10/10/10/10/10/10/10/10/10/10/10/10/10/1
0043	50	TK NK T
0045	50	$\frac{1}{1} = \frac{1}{1} = \frac{1}$
0045	55	
0047	33	DO A5 I = 1.N
0048		IK = NK + I
0049		HOLD = A(IK)
0050		IJ = I-N
0051		10.65 J = 1.N
0052		IJ = IJ + N
0053		IF (I-K) 60,65,60
0054	60	IF(J-K) 62,65,62
0055	62	KJ = IJ - I + K
00.56		A(IJ) = HOLD*A(KJ)+A(IJ)
0057	65	CONTINUE
0058		KJ = K - N
0059		DO 75 J = 1.N
0060		KJ = KJ+N
0061		IF(J-K) 70,75,70
0062	70	A(KJ)=A(KJ)/BIGA
0063	75	CONTINUE
0064		D = D * BIGA
0065		A(KK) = (1.,0.)/BIGA
0066	80	CONTINUE
0067		K = N
8200	100	K = K - 1
0069	105	IF (K) 150,150,105
0070	105	I = L(N)
0071	100	17(1-17) 12091209100
0072	108	JU = N + (N - 1)
0073		JK = N + (1 - 1)
0075		
0076		$HO(T) = \Delta(1K')$
0077		II = IR+I
0078		A(JK) = -A(JT)
0079	110	A(JI) = HOLD
0080	120	J = M(K)
0081		IF(J-K) 100,100,125
0082	125	KI = K - N
0083		$DO 130 I = 1 \cdot N$
0084		KI = KI + N
0085		HOLD = A(KI)
0086		JI = KI - K + J
0087		A(KI) = -A(JI)
0088	130	A(JI) = HOLD
0089		GO TO 100
0090	150	RETURN
0091		END

