

NATIONAL RADIO ASTRONOMY OBSERVATORY  
GREEN BANK, WV

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Following are view-graphs that will be discussed by R. Norrod in GBT Specification Working Group Meeting of 7/13/89.

R. Norrod  
July 13, 1989

- amplitude and phase control of the aperture illumination by subreflector shaping
- spillover past the subreflector is directed toward a cold sky
- low spillover past the paraboloid toward the ground for high elevation angles
- large depth of focus and field of view.

Some disadvantages are also apparent:

- greater blockage, particularly in small antennas (less than 100 wavelength apertures)
- higher sidelobes near the main beam
- not readily adaptable to use of poorly directional, frequency independent feeds

Given  $D =$   
 $F/D =$   
 $\text{Freq.} =$

(1) Hyperboloid Diameter

For Minimum Blockage

$$d = \sqrt{k \lambda F} \approx$$

\*  $k =$

use  $d =$

(2) Hyperboloid Focal Length

$$f = \frac{d}{2} (\cot \alpha + \cot \phi_0)$$

$$\phi_0 = 2 \tan^{-1} \frac{D}{4F}$$

$$\alpha = \quad ( \text{From Feed Design} )$$

$f =$

(3) Cassegrain Magnification

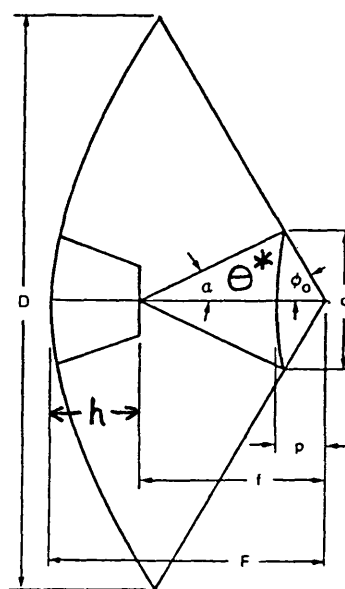
$$M = \frac{D}{4F} \cot \frac{\alpha}{2} =$$

(4) Hyperboloid Eccentricity

$$e = \frac{M+1}{M-1} =$$

(5) Hyperboloid Location

$$p = \frac{f}{2} \left( \frac{e-1}{e} \right) =$$



$D$  = Paraboloid Diameter  
 $F$  = Paraboloid Focal Length  
 $\phi_0$  = Paraboloid Half Angle

$d$  = Hyperboloid Diameter  
 $f$  = Hyperboloid Focal Length  
 $\alpha$  = Hyperboloid Half Angle

$M$  = Hyperboloid Magnification  
 $e$  = Hyperboloid Eccentricity  
 $p$  = Hyperboloid Location

$\lambda$  = Free space wavelength  
 $k$  = Feed beamwidth constant

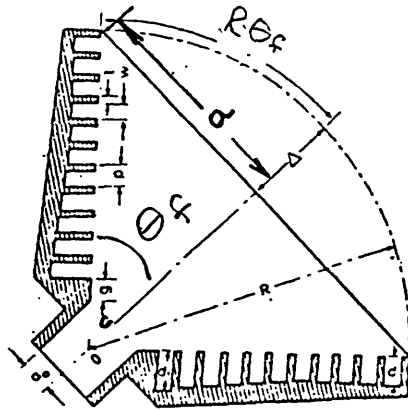
Fig. 3.33 Determination of Cassegrain geometry

\* " $k = 2$  for average feed with 10 dB taper."

FIGURE 1

Cassegrain Optics Design

Figures taken from Thomas, AP-26, p. 367f.



$$k \equiv \frac{2\pi}{\lambda}$$

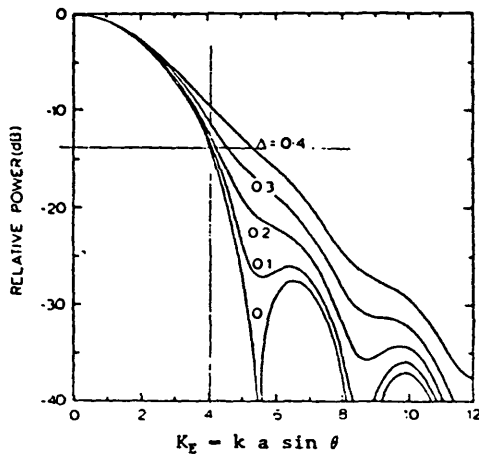


Fig. 2. Normalized radiation patterns for narrow-band corrugated horns where  $\theta$  is radiation angle relative to axial direction.

### "Narrowband"

- 1) Select  $\Delta \leq 0.4$
- 2) Select  $K_E$  from Fig. 2 for desired edge taper-- e.g.,  $K_E = 4$  for -13 dB. Calculate:

$$a/\lambda = \frac{K_E}{2\pi \sin \theta^*}$$

- 3) From geometry,

$$\theta_f = 2 \tan^{-1} \left( \frac{\Delta \lambda}{a} \right)$$

and

$$\frac{R}{\lambda} = \frac{a}{\lambda \sin \theta_f}$$

$\theta^*$  = Subtended half angle of reflector.

Narrowband ( $\Delta \leq 0.4$ )

Wideband ( $\Delta \geq 0.75$ )

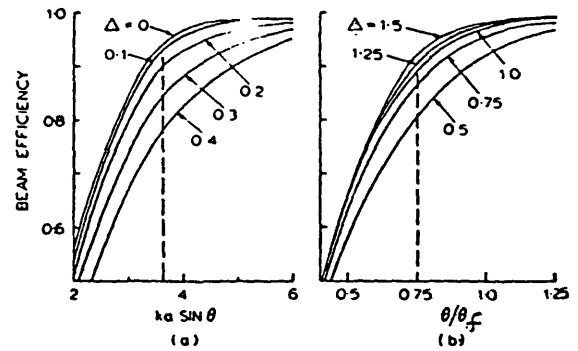


Fig. 4. Beam efficiencies for (a) narrow-band and (b) wide-band horns. Dashed line in both cases indicates horn parameters and beam efficiencies at -10-dB level of radiation patterns.

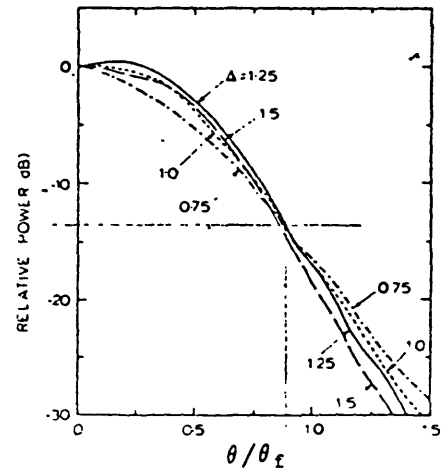


Fig. 6. Normalized radiation patterns for wide-band corrugated horns with  $\theta_0 < 70^\circ$ .

### "Wideband"

- 1) Select  $\Delta \geq 0.75$
- 2) Select  $\theta^*/\theta_f$  from Fig. 6 for desired edge taper. From this calculate  $\theta_f$ .

- 3) Then

$$a/\lambda = \frac{\Delta}{\tan \left( \frac{\theta_f}{2} \right)}$$

and

$$R/\lambda = \frac{a}{\lambda \sin \theta_f}$$

FIGURE 2  
Corrugated Horns

# Chronology of Proposed Designs

July 12, 1989

## Design 1: Technical Study Group Report (NLSRT #51) 4/18/89

F/D = 0.35                      d = 7 m                      h = 3.8 m (12.6')

Theta \* = 6.66

Wide-Band Feed :	Dia/Lambda = 21;	Length/Lambda = 71
Narrow-Band Feed:	Dia/Lambda = 11;	Length/Lambda = 64

Implications: Prime focus may be difficult; Fairly large feeds.

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## Design 2: Draft GBT Proposal (ca 5/15/89, unpublished)

F/D = 0.30                      d = 10 m                      h = 5 m (16.4')

Theta \* = 11.73

Wide-Band Feed :	Dia/Lambda = 12;	Length/Lambda = 23
Narrow-Band Feed:	Dia/Lambda = 6;	Length/Lambda = 21

Implications: Prime focus difficult; Fairly small feeds.

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## Design 3: GBT Proposal 6/15/89

F/D = 0.42                      d = 8 m                      h = 0 m

Theta \* = 5.74

Wide-Band Feed :	Dia/Lambda = 24;	Length/Lambda = 96
Narrow-Band Feed:	Dia/Lambda = 13;	Length/Lambda = 86

Implications: Cassegrain pushed to 3 - 5 GHz. Feeds large.

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## Design 4: Fisher-Napier-Thompson Small Sub-reflector

F/D = 0.42                      d = 4 m                      h = 5 m

Theta \* = 3.19

Wide-Band Feed :	Dia/Lambda = 43;	Length/Lambda = 310
Narrow-Band Feed:	Dia/Lambda = 23;	Length/Lambda = 278

Implications: Cassegrain difficult. Many feeds required.

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Other examples in R. Norrod report of 7/12/89 to be released as NLSRT memo.

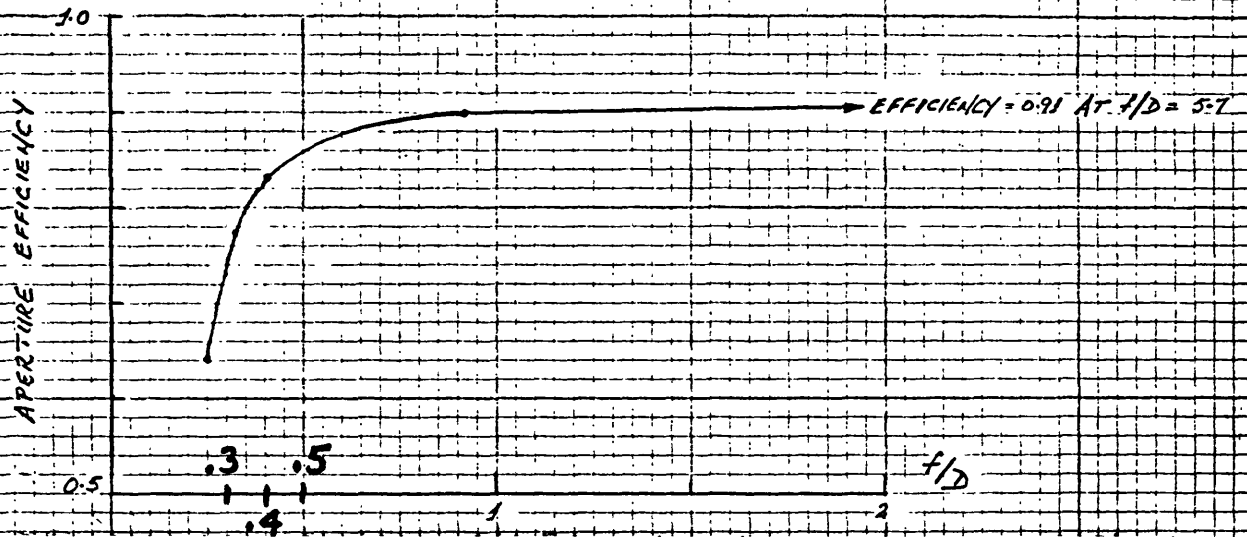
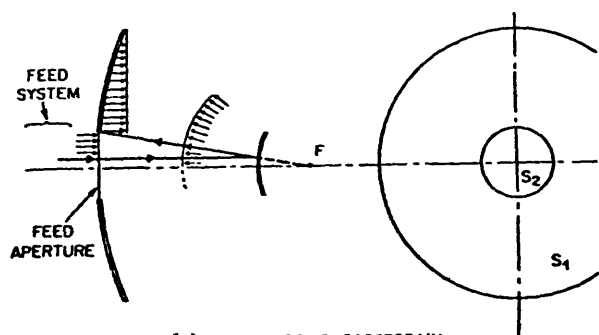
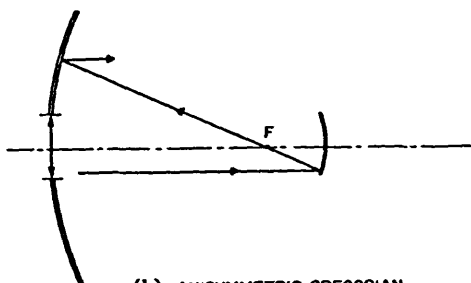


Fig. 1. Theoretical aperture efficiency of a paraboloid reflector antenna with a dual hybrid-mode feed at the prime focus. Data are taken from Fig. 13 of Minnett and Thomas (1968).

See NLSRT Memos #59 (Fisher)  
and #62 (Thompson) for  
discussion



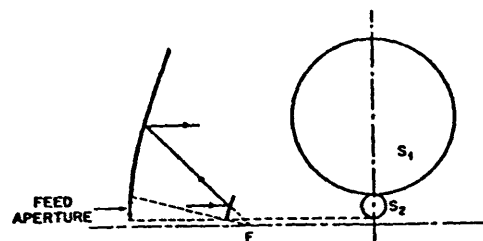
(a) AXISYMMETRIC CASSEGRAIN



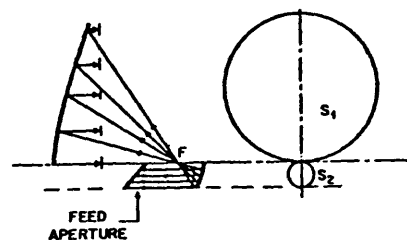
(b) AXISYMMETRIC GREGORIAN

Conventional axially symmetrical antennas of Cassegrainian and Gregorian type.

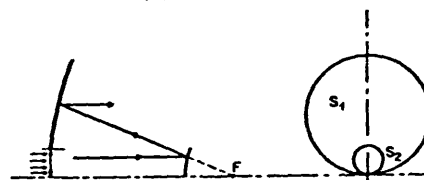
Figure 4-1



(a) OFFSET CASSEGRAIN



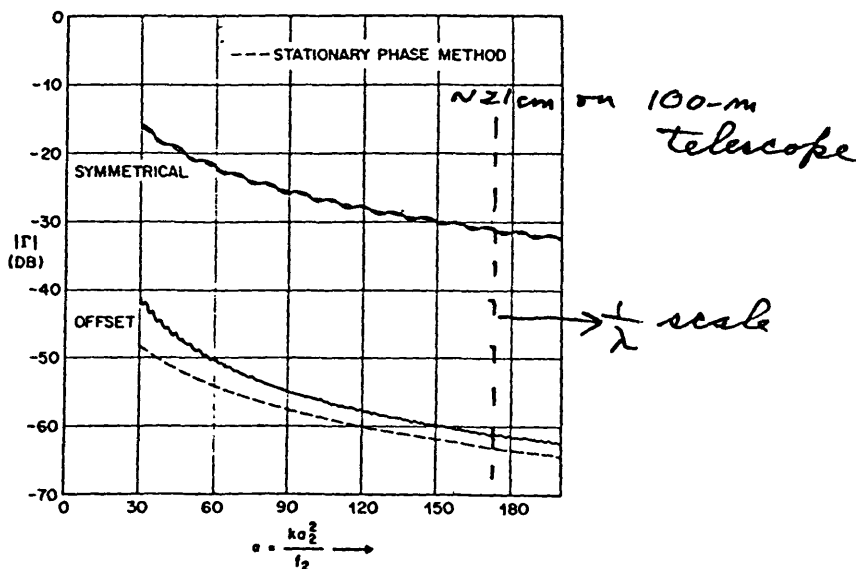
(b) BISECTED GREGORIAN



(c) BISECTED CASSEGRAIN

(a) Cassegrainian configuration without blockage. (b) Gregorian configuration without blockage. (c) Bisected Cassegrainian configuration with some blockage.

Figure 4-2



Reflection coefficients for cases of Figs. 1 and 2(c), assuming an illumination taper of 13 dB at edge of subreflector.

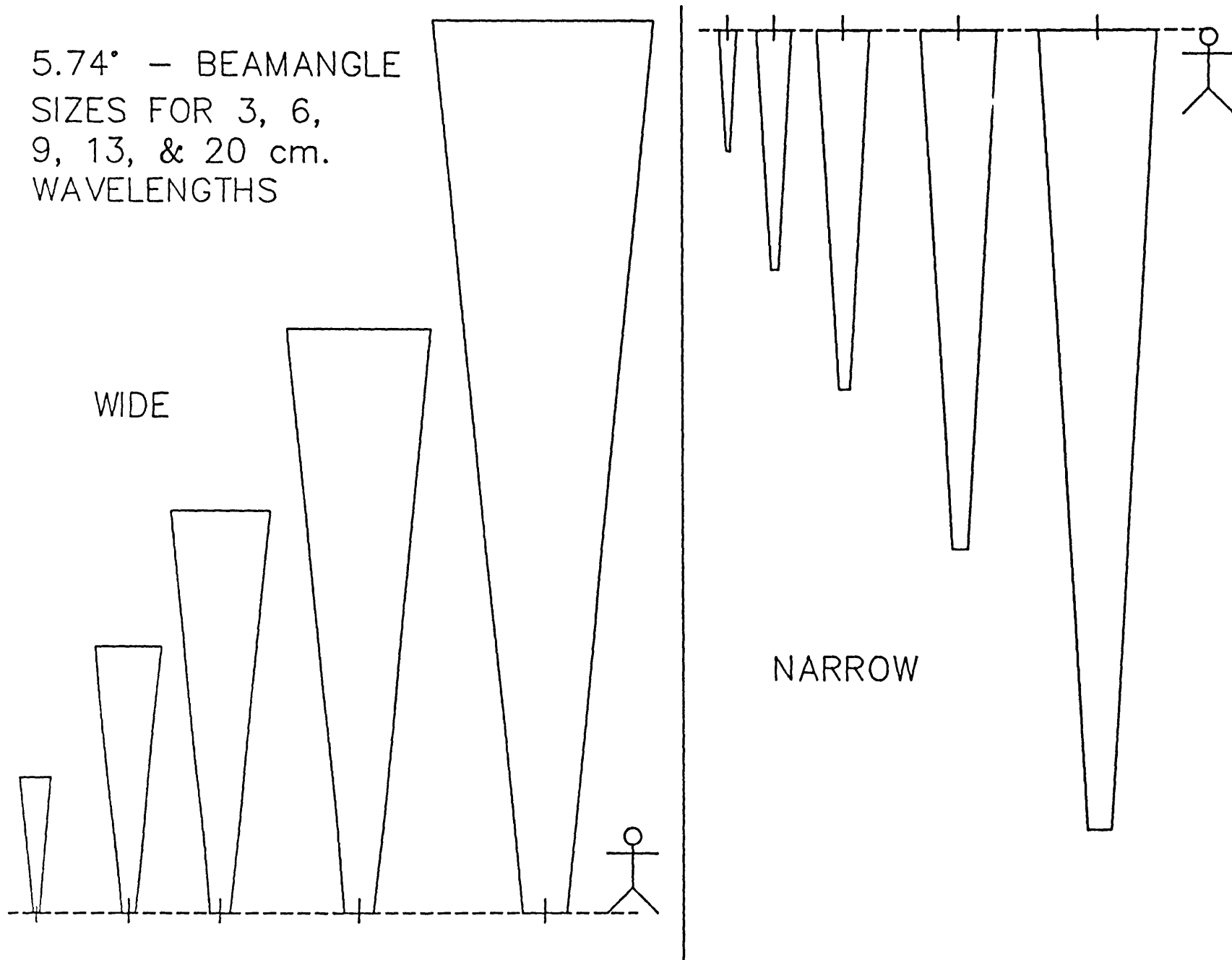
Figure 4-3

5.74° – BEAM ANGLE  
SIZES FOR 3, 6,  
9, 13, & 20 cm.  
WAVELENGTHS

WIDE

NARROW

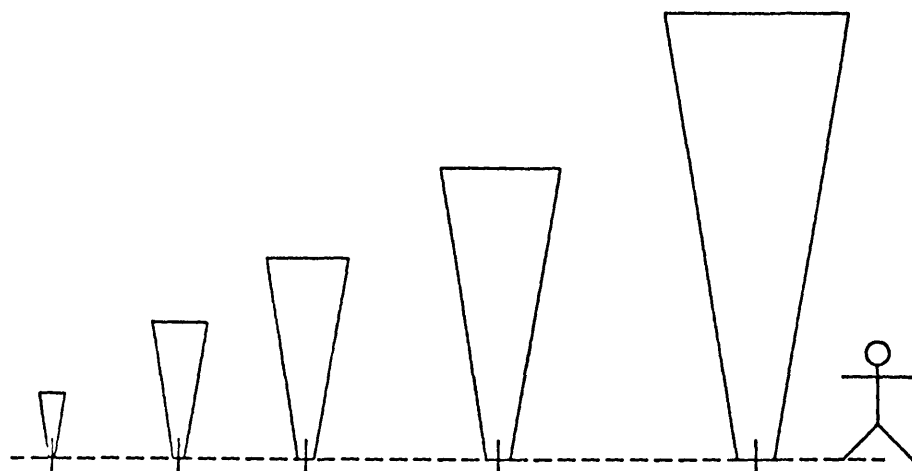
FIGURE 6



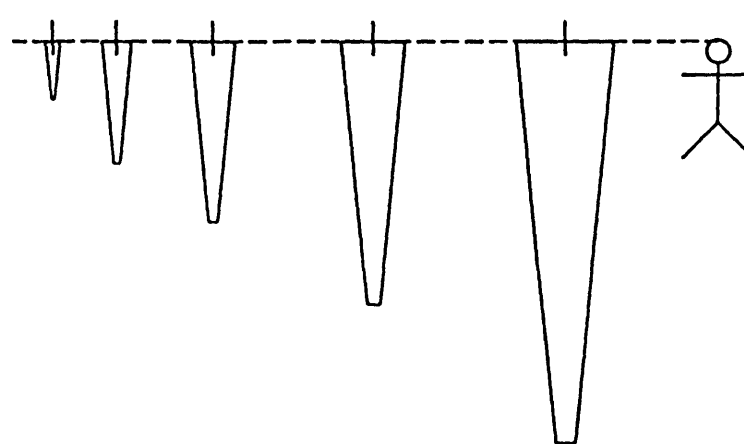
9.55° – BEAMANGLE  
SIZES FOR 3, 6,  
9, 13, & 20 cm.  
WAVELENGTHS

FIGURE 12

WIDE



NARROW





MEMBERS  
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# GBT OPTICS DESIGN

July 12, 1989

## Working Assumptions:

- 1) Attempt to maximize sensitivity over entire frequency range of antenna.
- 2) Design for nearly continuous frequency coverage from about 100 MHz to at least 45 GHz.
- 3) Must have capability to have multiple receivers on-line and "rapid" (automated if possible) switchover. Must include a "high use" weather independent frequency.
- 4) Must support VLBA observing to extent possible.

DRAFT AGENDA  
Optics Engineering Group  
Meeting 7/14/89

- 1) Goals
  - Short-term : Generate report with recommended optics configuration(s) for symmetrical antenna. Finish by Aug 10.
  - Long-term : ??
- 2) Fundamental Questions
  - F/D ?
  - Subreflector Diameter?
  - Location of secondary focus relative to vertex?
  - Receiver locations? How do we switch between receivers?
  - How do we cancel atmosphere?
- 3) Design Questions
  - How can we set physical limits on some of these parameters?
    - Strut blockage vs. F/D
    - Efficiency vs. F/D
    - Nutation of subreflector
    - Hiding or removal of subreflector
    - Feed diameter & length
    - Size of vertex cabin
  - Can we arrange optics to allow simultaneous observations at multiple frequencies?
- 4) Select a few cases to examine in detail
  - $F/D = 0.3$ ,  $d > 8$  m
  - $F/D = 0.42$ ,  $d > 8$  m
  - $F/D = 0.42$ ,  $d < 5$  m
  - Design similar to 12 meter antenna optics?
  - Beam waveguides?
  - Other exotic cases?
- 5) Miscellaneous
  - NRAO analysis software
  - Outside expertise
  - Communications within group