# Laser Distance Measurements To The Elevation Bearing Support Weldments 

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March 14, 1997


#### Abstract

The GBT laser rangefinder system has the potential to provide accurate measurements of azimuth and vertical tilt of the telescope's elevation shaft. Distance measurements can be made from ranging stations around the telescope base, to reflecting optical targets located beneath the elevation bearing support weldments located at each end of the alidade structure. For any alidade azimuth, at least two ranging lines of sight are available on the right side of the alidade and two or more on the left side, to the bottom surface of each weldment. Retroreflectors located beneath the weldments, on a line parallel to the elevation shaft, could supply excellent position fiducial reference points on the weldments, if two right side and two left side range measurements can be made to each target. At best, the horizontal angle of the line between the target fiducial points could be measured within 1 arc-second, and the vertical tilt of this line to 2 arc-second. Position determination of these reference points would give good quality information on orientation and position of the telescope's elevation shaft.


Ball retroreflectors, which have the widest angular response of any available reflector, would have to be viewed near the limits of their response range to return signal to both right and left side rangefinders, if they were simply mounted statically beneath the weldments. More complex reflector arrangements could be used, to obtain adequate rangefinder return signal. Tradeoffs between quality of shaft location and reflector target configuration are discussed in this memo.

## 1 Introduction.

The mission of the GBT laser rangefinder system is to make measurements giving information about main reflector shape, telescope pointing and structural deformation and displacement. Ranging measurements of the positions of fiducial reference points rigidly attached to the telescope's alidade structure, near each of the elevation shaft bearings, could provide accurate
information on the orientation and position of the elevation shaft.

Twelve rangefinders are spaced at $30^{\circ}$ intervals around the telescope base, at 120 m distance from the pintle bearing. For any alidade azimuth, four or more ranging lines of sight are available to the bottom surface of each elevation bearing support weldment, at least two from each side of the telescope's plane of symmetry. If fiducial reference points can be fixed to the bottom surface of each weldment and ranged with four lines of sight, two from the right and two from the left, the coordinates of each fiducial point can be determined with sub-millimeter accuracy. The horizontal bearing angle of the line joining these points would be determined within one arc-second, and the vertical tilt of this line would be determined within two arc-seconds. The horizontal bearing offset angle and the vertical tilt offset angle of this line relative to the elevation axis of the telescope (which is the line between elevation bearing centers) should each remain nearly constant during telescope operation. It is proposed here that the offset of the line between weldment fiducial points and the elevation axis is sufficiently constant that this line between may be used to measure the elevation axis' spatial orientation, once the initial offset has been measured by surveying at some initial telescope elevation (e.g near the telescope rigging angle).

The two support weldments are massive platforms which support the elevation bearings of the telescope. The bottom surface of each weldment is a large horizontal plane area, designed to be 137.00 inches below the elevation axis (as measured perpendicular to the alidade track plane). Under varying loading of the telescope, when tipping structure elevation, wind loading, and temperature change, the change of orientation from the horizontal of the bottom surface of either weldment is expected to be less than 150 arc-seconds [1]. It can be demonstrated that changes of weldment surface orientation to the horizontal of this magnitude will not significantly degrade the measurement suggested above.

## 2 Range Distance Survey Models

In order to locate the center of a target retroreflector mounted beneath a bearing support weldment it will be necessary to range this target from stations both to the right and to the left of the telescope's plane of symmetry. For each target ball two stations to the left and two other stations to the right have direct lines of sight to the ball at any alidade azimuth. Figure 1 shows one of these lines of sight.

Typically, three target sight lines are not available to targets at both ends of the elevation shaft from stations on one side of the symmetry plane. One or both sub-weldment targets will have to be viewed from 2 stations right together with 2 stations left of that plane. However, the view angles of the stations from the subweldment retroreflectors, with respect to the downwards gravity vertical direction, are large. They are given in Table 1. The expected power return to a ranging station from a ball reflector at 100 to 150 meter range, for incidence angle of $72^{\circ}$ to the normal to the reflector aperture plane, is near one percent [2]. This level of return may be marginal for ranging measurements.

Actual ranging tests will have to be performed to determine whether power return is adequate for ranging at $72^{\circ}$ incidence at 150 meter range. If the tests are positive, then two ball targets can be mounted for ranging under the weldments, each with its aperture plane horizontal. The laser ranging lines of sight for this 2-ball configuration are shown schematically as configuration 1 in Figure 3. This ranging configuration is statically determinate. Survey modeling of this measurement arrangement (cf. Appendix II) indicates that the horizontal bearing of the line of ball centers should be measurable to $0.7^{\prime \prime} \mathrm{rms}$, vertical tilt of this line should be measurable to 2 ".

If the view angle is too large to get adequate laser power return the situation becomes more complicated. A target must be viewed at large angles from both the right and left halves of the telescope, with respect to the telescope's plane of symmetry. A single ball retroreflector aimed to look between $65^{\circ}$ and $75^{\circ}$ to the right has no responsivity to a laser beam incident from $65^{\circ}$ to $75^{\circ}$ left. A ball reflector aimed midway between right and left has inadequate response on both sides.

One possible solution would be to mount each of the retroreflector target balls in a mechanical latching toggle mount, which could allow the target to look alternately to the right and to the left. The ball would rotate its glance to either side. The axis of rotation would pass through the optical center of the target, which is the ball center of curvature; in that case, the stations on either side would still range to a fixed target point.

The price of this active reflector solution, compared to use of a fixed ball, is the need to design a moving mount and to supply power lines and position control signals to the targets.

Another possible solution might be to replace the single ball target under each weldment with a pair of closely spaced targets. The targets would be
mounted in a common housing at an accurately known separation and orientation relative to the bottom surface of the weldment. One reflector of the pair would be aimed approximately $70^{\circ}$ to the right, the other $70^{\circ}$ left, with appropriate baffling so the right-looking ball is ranged only by stations to the right and the left-looking ball is ranged only by stations to the left. The pairs of targets at the opposite ends of the elevation shaft could be aligned either perpendicular or parallel to the elevation axis of the telescope (Fig. 3).

This is a passive solution, and does not require power lines or control signals. However the ranging configuration now beomes statically indeterminate. Two stations ranging accurately on a target only restrain that target to lie on a circle. They do not fix the position of that target. Each ball center of a ball target pair at fixed separation is free to move on an arc of its circle, constrained only by the condition that a line segment of length equal to the ball center separation can be found connecting the circle arcs of the two ball centers. (The constraint geometry is discussed in more detail in Appendix I). Also, four ball targets are required instead of two.

Since a statically determinate trilateration is not generally available in here, it might appear that the separated ball pairs do not define unique target positions, so the employment of separated targets appears useless. This appearance is deceptive. Strong additional restraints on ball center positions are available in fact.

The weldment bottom surfaces will remain quite close to horizontal, for all operating conditions of the GBT. This means that the line of centers of the ball reflector pair at each end of the elevation axle will lie at a zenith angle (with respect to the direction of vertical at the pintle bearing) which is close to $90^{\circ}$. The line of centers of two balls at opposite ends of the elevation shaft will also lie at a zenith angle near $90^{\circ}$. By bounding the deviation from $90^{\circ}$ of the zenith angle of the line of centers of any two sub-weldment ball reflectors, one obtains a strong restraint on the Z-coordinate (which is defined to be $\perp$ to the alidade track) of each ball center. We note that zenith angles are not assumed to be $90^{\circ}$. We do however assume that their deviation from $90^{\circ}$ is known a-priori with a given standard deviation, in the model ranging surveys. We choose this a-priori standard deviation to be 300 arc-seconds. The structural tilts of the weldments are expected to be below 150 arc-seconds, in service. The ball centers can be mounted initially so that their Z-coordinates are the same within 1 mm . A 300 arc-second tilt in zenith angle between the centers of balls at opposite ends of the elevation axle would correspond to a 7.5 cm difference in elevation of the centers, which is a loose constraint in terms of directly restricting the ball heights.

Measurement model simulations were made using the Star*Net least squares survey adjustment program (Starplus Software Inc., Oakland, CA). The configurations 1-3 of Fig. 3 were modeled, with spacing of 52 meters between balls on opposite sides of the elevation axle. (This is not a critical spacing, simulations between 45 and 52 meters give similar results). Range station levelling was assumed to have standard error of 0.2 mm . The standard error of laser ranging distances was assumed to be 0.15 mm . The measurement configuration and lines of sight are shown in Fig. 4. Model adjustment files are given in Appendix II. The modeling results are summarized in Table 2.

Standard error of the horizontal bearing angle between opposite balls at the two ends of the elevation axle was 0.7 arc-second for the two ball configuration, 0.84 arc-second for the two ball pair configuration with each pair perpendicular to the elevation axis, and 1.3 arc-second for the four ball in-line configuration along a line paraxial to the elevation axis. Standard error of the vertical tilt angle between opposite axle end target centers was 2 arc-seconds for the first two configurations, and 3 arc-seconds for the in-line 4 -target configuration.

Configuration 1 was the strongest. Configuration 2 was slightly weaker, and configuration 3 was significantly weaker. If power return turns out to be too low for employment of configuration 1, then configuration 2 appears to be an acceptable alternative.


Figure 1. Bottom Surface Of An Elevation Bearing Support Weldment Viewed From A Rangefinder Station.


Figure 2. A Ball Retroreflector

# TABLE 1. View Angles Of Ranging Stations From The Ball Reflectors. 

Alidade Bearing: ..... $0^{\circ} \quad 10^{\circ}$
$20^{\circ} \quad 30^{\circ}$
Maximum Slant Range
To Reflector (meter): ..... $\begin{array}{llll}127.3 & 142.8 & 145.8 & 148.4\end{array}$
Minimum Slant Range $\begin{array}{llll}110.9 & 108.2 & 106.1 & 110.9\end{array}$
To Reflector (meter):
Maximum View Angle $69.0^{\circ} \quad 71.4^{\circ} \quad 71.8^{\circ} \quad 72.1^{\circ}$From Reflector:
Minimum View Angle ..... 65.8
$65.1^{\circ} \quad 64.6^{\circ}$ ..... $65.8^{\circ}$
From Reflector:

$\infty$


Figure 3. Bilateral Ranging Configurations Of Ball Retroreflectors.

TABLE 2. Measurement Model Adjustment Standard Errors.
$\left.\begin{array}{llll} & \text { Configuration \#1 } & \text { Configuration \#2 } & \text { Configuration \#3 } \\ & \begin{array}{lll} & \\ & \text { One reflector ball at } \\ \text { each end of elevation } \\ \text { axle. }\end{array} & \begin{array}{l}\text { Two ball pairs, one } \\ \text { at each end of elev- } \\ \text { ation axle, line of }\end{array} & \begin{array}{l}\text { Four balls in-line, } \\ \text { two at each end of } \\ \text { each pair } \perp \text { to axle. }\end{array} \\ \text { elevation axle. }\end{array}\right]$


Figure 4. Ranging Measurement Sight Lines.

## 3 Possible Application To Telescope Pointing

GBT pointing will ultimately be done by observing a field of celestial radio sources, for calibration reference. Known source declinations and right ascensions will be converted to telescope horizon system azimuth and elevation local coordinates at time of observation. The corresponding telescope angle encoder azimuth and elevation readings at time of observation will then be fitted to a mathematical pointing model of the telescope. This model is a transformation which converts telescope horizon coordinates of an object to be observed to encoder setpoint values required to orient the telescope for observation of this object. The model contains a set of parameters, the pointing coefficients, which are obtained by some least squares procedure fitting the calibration source horizon coordinates to the encoder readouts at time of observation. After the pointing coefficients have been fitted, the observation measurement residuals are examined. If the residuals are acceptably low, the model is adopted as an algorithm to command the encoder output setpoints for driving the telescope to look at a celestial radio source. If the residuals are unacceptably large the model is modified and refitted, until the residuals are acceptable.

The pointing model is fitted initially and used subsequently for under telecope operating conditions which can be significantly different from those encountered during pointing model determination. The accepted model might not include all of the important variables encountered during telescope operations, for example thermal expansion gradients. In such a case the model might need correction.

Laser ranging is not ordinarily needed for telescope pointing, after a pointing model has been chosen, pointing coefficients fitted to a suitable field of celestial radio source objects have been obtained, and the model has been refined to the degree that the model's residuals are acceptably small.

However, in the early stages of telescope commisioning the telescope must acquire and track calibration sources before a pointing model has been fitted. During this time, the laser metrology system may be of aid in pointing the telescope. The horizontal bearing and vertical tilt angles of the mean axial line of ball target centers will likely be at small constant offset from the elevation axis defined by the line through elevation bearing centers. Shifts of the target mean line of centers are expected to be close to those of the elevation axis. The mean line of target centers can be an effective estimator for determination of elevation axis spatial orientation.

Certain motions of the antenna tipping structure and alidade, due to temperature gradients, and wind and gravity loading, can occur during telescope operation, which do not change the rotation of the antenna azimuth and elevation encoders, and are not sensed by these devices. These motions affect telescope pointing and they can be observed by laser ranging. Information about those motions, generated by laser ranging, and which supplements the angle encoder readout information, can be incorporated into the pointing command structure of the telescope.

## 4 Discussion

Survey modeling indicates that laser ranging of ball retroreflector targets under the GBT elevation bearing weldments could provide useful information to assist with pointing of the GBT. A structure weighing about forty to seventy pounds would have to be fastened rigidly beneath each weldment, and oriented precisely with respect to the bearing axis, upon installation. Installation mounts and procedures would have to be developed to do this. After installation of the targets, their initial positions would have to be surveyed, to determine the mean axial line of target centers relative to the bearing center defined elevation axis.

If the targets could be in place by early summer 1997, laser rangefinders could monitor structural deformations of the alidade and motions of the elevation axis during lifting of the heavy main reflector backup sections onto the box structure. The monitor information might be used to flag occurrence of possible hazard situations during the lifting.

Over a longer term, information on elevation axis orientation obtained by laser ranging can be collected and data based to allow the option of later analysis of elevation axis motions during telescope operation, for the purpose of improving the telescope pointing model and also for possible trend analysis to indicate long term changes in the telescope geometry and behavior.

## Bibliography

[1] Lee King. Private Note to D. Parker, February 27, 1997. Re: Elevation Bearing Measurements.
[2] M.A. Goldman. Ball Retroreflector Optics. GBT Memo 148. March 23, 1996.

## Appendix I. Concerning Static Determinism Of

## 4-Target Reflector Configurations.

Assume that laser ranging stations $L R_{1}$ and $L R_{2}$ are ranging ball retroreflector $A$ and stations $L R_{3}$ and $L R_{4}$ are ranging ball retroreflector $C$, which are mounted at the same end of the elevation axle. Assume that the true range of $A$ from $L R_{1}$ is $r_{1}$ and from $L R_{2}$ is $r_{2}$, and the true range of $C$ from $L R_{3}$ is $r_{3}$ and from $L R_{4}$ is $r_{4}$. Let $D_{12}$ be the distance between the scan points of stations $L R_{1}$ and $L R_{2}$, and $D_{34}$ be the distance between the scan points of stations $L R_{3}$ and $L R 4$. The scan centers of the four ranging stations lie close to a horizontal plane, to within a millimeter. The relevant geometry is shown in Fig. 5.

The center of ball $A$ is constrained to be one vertex of a triangle whose sides are $r_{1}, r_{2}$ and $D_{12}$, and whose other vertices are the scan centers of $L R_{1}$ and $L R_{2}$. The locus of all such points in space is a circle, $C_{A}$, lying in a plane $\perp$ to the line of scan centers of $L R_{1}$ and $L R_{2}$. The center point, $O_{12}$, of this circle lies on the line of scan centers $L R_{1}-L R_{2}$. Call $h_{12}$ the radius of this circle. Similarly the locus of possible positions of the center of ball reflector $C$ lies on a circle, $C_{C}$, of radius $h_{34}$, whose center, $O_{34}$, lies on the line of scan centers $L R_{3}-L R_{4}$, and whose plane is $\perp$ to the line $L R_{3}-L R_{4}$.

The centers of ball reflectors $A$ and $C$ are mounted at an accurately known distance $D_{A C}$ from one another. This constrains the line segment $\overline{A C}$ joining the centers of reflectors $A$ and $C$ to have its ends on the circles $C_{A}$ and $C_{C}$. The constraint that the reflector centers are at fixed distance $D_{A C}$ from one another constrains them to lie on bounded arcs of $C_{A}$ and $C_{C}$ but does not spatially fix the line segment $\overline{A C}$, which is free to slide within
a developable surface patch joining the bounded arcs.
The bounded arcs mentioned above are defined in the following manner. The locus of end points of line segments of length $D_{A C}$, whose nearer end lies at distance $h_{12}$ from $O_{12}$ is a closed hollow ball, $H B_{A}$, centered at $O_{12}$, whose inner radius is $h_{12}$ and whose outer radius is $h_{12}+D_{A C}$. The ball reflector center point $C$ must lie in the interior of or on the boundary spheres of $H B_{A}$. The point $C$ must also lie on the circle $C_{C}$, and also lie at positive elevation. The point $C$ is then constrained to lie on the arc which is the positive elevation intersection of circle $C_{C}$ with hollow ball $H B_{A}$. Similarly, the ball reflector center point $A$ must lie both on circle $C_{A}$ and within or on a hollow ball $H B_{C}$ whose inner radius is $h_{34}$ and outer radius is $h_{34}+D_{A C}$ and is centered at $O_{34}$.

The laser ranges $r_{1}$ to $r_{4}$ only constrain the reflector centers to lie on the arcs defined above. It does not fix them. If, however, a new geometric constraint is introduced independent of laser ranging, that line segment $\overline{A C}$ is horizontal, then there is a unique horizontal segment $\overline{A C}$ of length $D_{A C}$, at positive elevation, which joins circles $C_{A}$ and $C_{C}$. This additional constraint is sufficient to fix points $A$ and $C$. The constraint is obtained physically by the fact that the bottom weldment surfaces are nearly horizontal and the ball centers of nearby reflectors will mount at the same distance below their common weldment surface.

Similar considerations hold for balls $B$ and $D$, which mount at the other end of the elevation axle.


## Appendix II. Models Of Adjusted Laser Ranging Surveys.

Two models of laser ranging measurement of sub-weldment ball retroreflector positions are presented. One model is that of two reflectors, one under each weldment; the balls look directly downwards vertically; each reflector is ranged by four stations (configuration 1). This is a statically determinate model. The incidence angles to the balls, from the stations, lie between $65.8^{\circ}$ and $71.8^{\circ}$. If adequate laser return signal can be obtained, this will be an optimal measurement configuration.

The other model is that of two pair of balls under each weldment (configuration 2); the line of centers of the two balls on each end of the elevation axle is oriented perpendicular to the elevation axle, and is horizontal to 300 arc-seconds standard error. Input data for this model is laser range information supplemented by additional directional and angle restraints derived from the assumption that the reflectors are mounted on essentially horizontal weldment surfaces at nearly fixed position and orientation to one another. The ball centers are assumed to be precisely 0.25 meters apart. This distance is near to the smallest ball center spacing which allows the balls to be fixed rigidly in a common housing, with one ball facing right and the other facing left, and allows the housing to be mounted on a weldment so the line of ball centers is $\perp$ to the elevation axis.

STAR*NET Project: ELBEBALL

March 04, 1997 Version 5.3

This is a data file for preanalysis simulating a set of measurements from ground laser ranging stations to TWO cat's eye ball retroreflectors mounted approximately 101 inches below the upper weldment deck, one ball at each end of the elevation bearing. The pair of reflector balls will be represented by ball pairs at 10 degree azimuth increments clockwise (ABAIL moves Eastward), to simulate rotation of the alidade.

Ranging station scan point horizontal coordinates will be assumed known a-priori to a standard error of lmm. We use a free adjustment, assuming that no ground station scan points are fixed, but that the ground station distances to first and second nearest neighbor scan points are ranged on one another to 0.15 mm . THIS IS A FREE ADJUSIMENT, WITH NO FIXED RANGING STATION SCAN POINTS.

The Z-coordinate of each station scan point is assumed to be known a-priori to 0.20 mm standard error. (This is found by a levelling survey, with a small correction for earth curvature).

Reflector ball point $X$ and $Y$ coordinates are assumed to be known only to 1 meter, a-priori, and are to be calculated from this survey model preanalysis. The ball Z-coordinate is assumed known, a-priori, to 0.30 m.
\# Each ball center $Z$ coordinate is assumed, a-priori, to be \# 1900" - 46" - 91" $-10^{\prime \prime}=1754^{\prime \prime}$ (44.526 meter) with 0.30 meter \# standard error.

The 2 ball centers are assumed, a-priori, to be 52 meter apart.

Ranges to ball centers are assumed measured to 0.15 mm standard error (0.006").

Each horizontal coordinate of ranging stations is assumed to have 1 mm std error, before station-to-station ranging.

EACH BAL工 IS ASSUMED TO SEE TWO RANGING STATIONS TO ITS RIGHT AND TWO STATIONS TO ITS LEFT.
\# enter laser ranging ground-Station scan point coordinates (meters)

| \# | POINT | X | Y | Z | Standard Error |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| \# |  | (EAST) | (NORTH) |  | $s(X)$ | $s(Y)$ | $s(Z)$ |
| C | ZY101 | 018.4894 | 118.5670 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY102 | 075.2958 | 093.4370 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY103 | 111.9268 | 043.2712 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY104 | 118.5670 | -018.4894 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY105 | 093.4374 | -075.2958 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY106 | 043.2712 | -111.9268 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY107 | -018.4894 | -118.5670 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY108 | -075.2958 | -093.4374 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY109 | -111.9268 | -043.2712 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY110 | -118.5670 | 018.4894 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY111 | -093.4374 | 075.2958 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY112 | -043.2712 | 111.9268 | 0.0 | 0.001 | 0.001 | 0.0002 |

\# ENTER ELEVATION BEARING BALL REFLECTOR COORDINATES (METERS)

| C | ABALLL1 | 00.0000 | 26.0000 | 45.7 | 1.0 | 1.0 | 0.3 |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| C | BBALLL1 | 00.0000 | -26.0000 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | ABALLL2 | 04.5149 | 25.6050 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | BBALLL2 | -04.5149 | -25.6050 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | ABALLS | 08.8925 | 24.4320 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | BBALLS | -08.8925 | -24.4320 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | ABALL4 | 13.0000 | 22.5167 | 45.7 | 1.0 | 1.0 | 0.3 |
| C | BBALL4 | -13.0000 | -22.5167 | 45.7 | 1.0 | 1.0 | 0.3 |

## \# <br> ENTER LASER RANGE TO BALL CENTER STD ERRORS <br> (METERS)

| ZY102-ABALL1 | 0.00015 |
| :--- | :--- |
| ZY103-ABALLI | 0.00015 |
| ZY111-ABALL1 | 0.00015 |
| ZY110-ABALLI | 0.00015 |
| ZY104-BBALLI | 0.00015 |
| ZY105-BBALL1 | 0.00015 |
| ZY108-BBALLI | 0.00015 |
| ZY109-BBALLI | 0.00015 |
|  |  |
|  |  |
| ZY103-ABALL2 | 0.00015 |
| ZY104-ABALL2 | 0.00015 |
| ZY110-ABALL2 | 0.00015 |
| ZY109-ABALL2 | 0.00015 |
| ZY105-BBALL2 | 0.00015 |
| ZY104-BBALL2 | 0.00015 |
| ZY108-BBALL2 | 0.00015 |
| ZY109-BBALL2 | 0.00015 |


| ZY103-ABALL3 | 0.00015 |
| :--- | :--- |
| ZY104-ABALL3 | 0.00015 |
| ZY110-ABALL3 | 0.00015 |
| ZY109-ABALL3 | 0.00015 |
| ZY105-BBALL3 | 0.00015 |
| ZY104-BBALL3 | 0.00015 |
| ZY108-BBALL3 | 0.00015 |
| ZY109-BBALL3 | 0.00015 |
|  |  |
| ZY104-ABALL4 | 0.00015 |
| ZY105-ABALL4 | 0.00015 |
| ZY109-ABALL4 | 0.00015 |
| ZY110-ABALL4 | 0.00015 |
| ZY104-BBALL4 | 0.00015 |
| ZY105-BBALL4 | 0.00015 |
| ZY109-BBALL4 | 0.00015 |
| ZY110-BBALL4 | 0.00015 |

ENTER ASSUMED RANGE STATION TO STATION DISTANCE STANDARD ERROR (METER)

| ZY111-ZY101 | 0.00015 |
| :--- | :--- |
| ZY112-ZY101 | 0.00015 |
| ZY112-ZY102 | 0.00015 |
| ZY101-ZY102 | 0.00015 |
| ZY101-ZY103 | 0.00015 |
| ZY102-ZY103 | 0.00015 |
| ZY102-ZY104 | 0.00015 |
| ZY103-ZY104 | 0.00015 |
| ZY103-ZY105 | 0.00015 |
| ZY104-ZY105 | 0.00015 |
| ZY104-ZY106 | 0.00015 |
| ZY105-ZY106 | 0.00015 |
| ZY105-ZY107 | 0.00015 |
| ZY106-ZY107 | 0.00015 |
| ZY106-ZY108 | 0.00015 |
| ZY107-ZY108 | 0.00015 |
| ZY107-ZY109 | 0.00015 |
| ZY108-ZY109 | 0.00015 |
| ZY108-ZY110 | 0.00015 |
| ZY109-ZY110 | 0.00015 |
| ZY109-ZY111 | 0.00015 |
| ZY110-ZY111 | 0.00015 |
| ZY110-ZY112 | 0.00015 |
| ZY111-ZY112 | 0.00015 |

ENTER DUMMY ASSUMED BALL TO BALL DISTANCE STANDARD ERROR OF 1 METER TO GET RELATIVE BEARING OUTPUT INFORMATION.

ABALL1-BBALL1 1.0
ABALL2-BBALL2 1.0
ABALL3-BBALL3 1.0
ABALL4-BBALL4 1.0


# STAR*NET Adjustment Program <br> Version 5.0444 <br> Copyright 1993 STARPLUS SOFTWARE, INC. <br> Licensed for Use by National Radio Astronomy Observatory Serial Number 20649 <br> Run Date : Tue Mar 04 1997 10:14:30 

Summary of Files Used

| Project Directory | C:\STAR |  |
| :--- | :--- | :--- |
| Input Data File | ELBEBRL.DAT |  |
| Output Listing (This File) | ELBEBRL.LST | (Version 5.3) |
| Coordinates | ELBEBRL.PTS |  |
| Project Parameters | ELBEBRL.PRJ |  |
| Error Log | ELBEBRL.ERR |  |
| Plot File | ELBEBRL.SPL |  |

Adjustment Options
STAR*NET Run Mode : Preanalysis
Type of Adjustment : 3D
Input Order for Coordinates : X,Y,Z
Coordinate System : LOCAL
Project Scale Factor : 1.00000000
Linear Units; Angular Units : Meters; DMS
Input Order for Angle Stations : At-From-To
Max Iterations; Convergence Limit : 50; 0.0001
Correct Zeniths for Curve \& Refract : No
Adjust 3D Obs for Vert Divergence : No
3D Data Input Mode : Slope/Zenith
Earth Radius : 6372161.544 Meters
Coefficient of Refraction : 0.070

Default Instrument Standard Error Settings

| Distances ( Constant ) | : | 0.0001000 | Meters |
| :---: | :---: | :---: | :---: |
| Distances ( PPM ) | : | 0.0000010 |  |
| Angles | : | 1.4140000 | Seconds |
| Directions | : | 1.0000000 | Seconds |
| Azimuth / Bearings | : | 2.0000000 | Seconds |
| Zeniths | : | 2.0000000 | Seconds |
| Elevation Differences ( Constant ) |  | 0.0001000 | Meters |
| Elevation Differences ( PPM ) |  | 0.0000010 |  |
| Centering Error Instrument |  | 0.0000100 | Meters |
| Centering Error Target |  | 0.0000100 | Meters |

Summary of Unadjusted Input Observations

Number of Stations (Meters) $=20$

| Partially Fixed | x | Y | 2 | Description |
| :---: | :---: | :---: | :---: | :---: |
|  | SE-X | SE-Y | SE-Z |  |
| ZY101 | 18.4894 | 118.5670 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY102 | 75.2958 | 93.4370 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY103 | 111.9268 | 43.2712 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY104 | 118.5670 | -18.4894 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY105 | 93.4374 | -75.2958 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY106 | 43.2712 | -111.9268 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY107 | -18.4894 | -118.5670 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY108 | -75.2958 | -93.4374 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY109 | -111.9268 | -43.2712 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY110 | -118.5670 | 18.4894 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| 2Y111 | -93.4374 | 75.2958 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY112 | -43.2712 | 111.9268 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ABALL1 | 0.0000 | 26.0000 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| BBALLI | 0.0000 | -26.0000 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| ABALL2 | 4.5149 | 25.6050 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| BBALL2 | -4.5149 | -25.6050 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| ABALL 3 | 8.8925 | 24.4320 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| BBALL3 | -8.8925 | -24.4320 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| ABALL4 | 13.0000 | 22.5167 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |
| BBALL4 | -13.0000 | -22.5167 | 45.7000 |  |
|  | 1.0000 | 1.0000 | 0.3000 |  |

Number of Distance Observations (Meters) $=60$

| $\because r o m$ | To | Obs Dist | StdErr | HI | HT | Flags |
| :--- | :--- | :--- | :--- | ---: | ---: | :---: |
| YY102 | ABALL1 | 110.9310 | 0.0001 | 0.000 | 0.000 | S |
| AY103 | ABALL1 | 122.1245 | 0.0001 | 0.000 | 0.000 | $S$ |
| $\because Y 111$ | ABALL1 | 115.1048 | 0.0001 | 0.000 | 0.000 | $S$ |
| $\because Y 110$ | ABALL1 | 127.2911 | 0.0001 | 0.000 | 0.000 | $S$ |
| Y104 | BBALL1 | 127.2911 | 0.0001 | 0.000 | 0.000 | $S$ |
| $\because 105$ | BBALL1 | 115.1048 | 0.0001 | 0.000 | 0.000 | $S$ |


| ZY108 | BBALLI | 110.9313 | 0.0001 | 0.000 | 0.000 | S |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZY109 | BBALLI | 122.1245 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALL2 | 118.0589 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALL2 | 130.5400 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | ABALL2 | 131.4849 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ABALL2 | 142.7974 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALI2 | 118.9635 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | BBALL2 | 131.4849 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | BBALL2 | 108.1650 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | BBALI2 | 118.0589 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALI 3 | 114.2780 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALI 3 | 126.3299 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | ABALI 3 | 135.5350 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ABALI 3 | 145.8407 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALI 3 | 123.0732 | 0.0001 | 0.000 | 0.000 | 5 |
| ZY104 | BBALL 3 | 135.5350 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | BBALL 3 | 106.1114 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | BBALL 3 | 114.2780 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALL4 | 122.1245 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ABALL4 | 134.6327 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ABALL4 | 148.4023 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | ABALL4 | 139.3362 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | BBALL4 | 139.3362 | 0.0001 | 0.000 | 0.000 |  |
| ZY105 | BBALL4 | 127.2912 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | BBALL4 | 110.9313 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | BBALL4 | 122.1245 | 0.0001 | 0.000 | 0.000 | S |
| ZY111 | ZY101 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY112 | ZY101 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY112 | ZY102 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY101 | ZY102 | 62.1167 | 0.0001 | 0.000 | 0.000 | S |
| ZY101 | ZY103 | 120.0000 | 0.0001 | 0.000 | 0.000 |  |
| ZY102 | ZY103 | 62.1163 | 0.0001 | 0.000 | 0.000 |  |
| ZY102 | ZY104 | 119.9996 | 0.0001 | 0.000 | 0.000 |  |
| ZY103 | ZY104 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ZY105 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ZY105 | 62.1165 | 0.0001 | 0.000 | 0.000 |  |
| ZY104 | ZY106 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ZY106 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ZY107 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY106 | ZY107 | 62.1165 | 0.0001 | 0.000 | 0.000 |  |
| ZY106 | ZY108 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY107 | ZY108 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY107 | ZY109 | 120.0000 | 0.0001 | 0.000 | 0.000 |  |
| ZY108 | ZY109 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | ZY110 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ZY110 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ZY111 | 120.0000 | 0.0001 | 0.000 | 0.000 |  |
| ZY110 | ZY111 | 62.1165 | 0.0001 | 0.000 | 0.000 |  |
| ZY110 | ZY112 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY111 | ZY112 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ABALLI | BBALLI | 52.0000 | 0.0001 | 0.000 | 0.000 |  |
| ABALL2 | BBALL2 | 52.0000 | 0.0001 | 0.000 | 0.000 |  |
| ABALL 3 | BBALL3 | 52.0000 | 0.0001 | 0.000 | 0.000 |  |
| ABALL4 | BBALL4 | 52.0001 | 0.0001 | 0.000 | 0.000 | S |


|  | To | Bearing | Distance | Relative |  | DistPrec (PPM) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | BgErr | DisErr |  |
| ZY102 | ABALL1 | S48-09-05.39W | 101.0802 | 0.64 | 0.0002 | (DM) |
| ZY103 | ABALL1 | S81-13-40.76W | 113.2515 | 0.65 | 0.0002 | 1 |
| ZY111 | ABALLI | S62-11-05.00E | 105.6439 | 0.63 | 0.0002 | 1 |
| ZY110 | ABALLI | N86-22-31.64E | 118.8046 | 0.63 | 0.0002 | 1 |
| ZY104 | BBALLI | S86-22-31.64W | 118.8046 | 0.63 | 0.0001 | 1 |
| ZY105 | BBALL1 | N62-11-05.00W | 105.6439 | 0.63 | 0.0002 | 1 |
| ZY108 | BBALL1 | N48-09-04.78E | 101.0805 | 0.64 | 0.0002 | 1 |
| ZY109 | BBALLI | N81-13-40.76E | 113.2515 | 0.64 | 0.0001 | 1 |
| ZY103 | ABALL2 | S80-39-36.34W | 108.8550 | 0.67 | 0.0002 | 1 |
| ZY104 | ABALL2 | N68-51-45.67W | 122.2792 | 0.62 | 0.0002 | 1 |
| ZY110 | ABALL2 | N86-41-28.70E | 123.2874 | 0.64 | 0.0001 | 1 |
| ZY109 | ABALL2 | N59-23-43.24E | 135.2871 | 0.60 | 0.0002 | 1 |
| ZY105 | BBALL2 | N63-06-05.42W | 109.8355 | 0.62 | 0.0002 | 1 |
| ZY104 | BBALL2 | S86-41-28.70W | 123.2874 | 0.63 | 0.0001 | 1 |
| ZY108 | BBALL2 | N46-13-06.88E | 98.0366 | 0.65 | 0.0002 | 1 |
| ZY109 | BBALL2 | N80-39-36.34E | 108.8550 | 0.67 | 0.0001 | 1 |
| ZY103 | ABALL3 | S79-38-17.78W | 104.7425 | 0.68 | 0.0002 | 1 |
| ZY104 | ABALL3 | N68-37-37.13W | 117.7741 | 0.63 | 0.0002 | 1 |
| ZY110 | ABALL3 | N87-19-50.18E | 127.5980 | 0.63 | 0.0001 | 1 |
| ZY109 | ABALL3 | N60-44-06.54E | 138.4956 | 0.60 | 0.0001 | 1 |
| ZY105 | BBALL3 | N63-34-12.01W | 114.2739 | 0.61 | 0.0002 | 1 |
| ZY104 | BBALL3 | S87-19-50.18W | 127.5980 | 0.62 | 0.0001 | 1 |
| ZY108 | BBALL3 | N43-53-56.77E | 95.7661 | 0.66 | 0.0002 | 1 |
| ZY109 | BBALL3 | N79-38-17.78E | 104.7425 | 0.68 | 0.0001 | 1 |
| ZY104 | ABALL 4 | N68-46-19.21W | 113.2515 | 0.67 | 0.0002 | 1 |
| ZY105 | ABALL4 | N3 9-25-57.44W | 126.6391 | 0.60 | 0.0002 | 1 |
| ZY109 | ABALL4 | N62-13-41.48E | 141.1905 | 0.60 | 0.0002 | 1 |
| ZY110 | ABALL4 | N88-14-48.15E | 131.6286 | 0.64 | 0.0001 | 1 |
| ZY104 | BBALL 4 | S88-14-48.15W | 131.6286 | 0.64 | 0.0001 | 0 |
| zY105 | BBALL4 | N63-37-28.46W | 118.8047 | 0.64 | 0.0001 | 1 |
| ZY109 | BBALL4 | N78-09-04.99E | 101.0805 | 0.70 | 0.0002 | 1 |
| 2Y110 | BBALL4 | S68-46-19.21E | 113.2515 | 0.69 | 0.0001 | 1 |
| ZY111 | ZY101 | N68-51-48.11E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY112 | ZY101 | N83-51-48.27E | 62.1165 | 0.88 | 0.0001 | 1 |
| ZY112 | ZY102 | S81-08-11.26E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY101 | ZY102 | S66-08-10.94E | 62.1167 | 1.04 | 0.0001 | 1 |
| ZY101 | ZY103 | S51-08-12.00E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY102 | ZY103 | S36-08-12.73E | 62.1163 | 0.72 | 0.0001 | 1 |
| ZY102 | ZY104 | S21-08-12.13E | 119.9996 | 0.59 | 0.0001 | 0 |
| ZY103 | ZY104 | S06-08-11.73E | 62.1165 | 0.73 | 0.0001 | 1 |
| ZY103 | ZY105 | S08-51-48.06W | 120.0000 | 0.59 | 0.0001 | 0 |
| ZY104 | ZY105 | S23-51-47.84W | 62.1165 | 0.65 | 0.0001 | 1 |
| ZY104 | ZY106 | S38-51-48.00W | 120.0000 | 0.65 | 0.0001 | 0 |
| ZY105 | ZY106 | S53-51-48.06W | 62.1166 | 1.02 | 0.0001 | 1 |
| ZY105 | ZY107 | S68-51-48.11W | 120.0000 | 0.66 | 0.0001 | 0 |
| ZY106 | ZY107 | S83-51-48.27W | 62.1165 | 0.85 | 0.0001 | 1 |
| ZY106 | ZY108 | N81-08-11.94W | 120.0000 | 0.66 | 0.0001 | 0 |
| ZY107 | ZY108 | N66-08-12.16W | 62.1165 | 1.01 | 0.0001 | 1 |
| ZY107 | ZY109 | N51-08-12.00W | 120.0000 | 0.65 | 0.0001 | 0 |
| ZY108 | ZY109 | N36-08-11.94W | 62.1166 | 0.67 | 0.0001 | 1 |
| ZY108 | ZY110 | N21-08-11.89W | 120.0000 | 0.59 | 0.0001 | 0 |
| ZY109 | ZY110 | N06-08-11.73W | 62.1165 | 0.69 | 0.0001 | 1 |
| ZY109 | ZY111 | N08-51-48.06E | 120.0000 | 0.58 | 0.0001 | 0 |


| ZY110 | ZY111 | N23-51-47.84E | 62.1165 | 0.71 | 0.0001 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ZY110 | ZY112 | N3 8-51-48.00E | 120.0000 | 0.68 | 0.0001 |
| ZY111 | ZY112 | N53-51-48.06E | 62.1166 | 1.03 | 0.0001 |
| ABALII | BBALII | S00-00-00.00E | 52.0000 | 0.68 | 0.0001 |
| ABALI2 | BBALI2 | S10-00-00.37W | 52.0000 | 0.63 | 0.0001 |
| ABALL3 | BBALI3 | S19-59-59.85W | 52.0000 | 0.66 | 0.0001 |
| ABALL4 | BBALI4 | S29-59-59.84W | 52.0001 | 0.63 | 0.0001 |

## Error Propagation

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==================
```

Station Coordinate Standard Deviations

Station
ZY101
ZY102
ZY103
ZY104
ZY105
ZY106
ZY107
ZY108
ZY109
ZY110
ZY111
ZY112
ABALL1
BBALL1
ABALL2
BBALL2
ABALL 3
BBALL3
ABALL4
BBALL4

Station
ZY101
ZY102
ZY103
ZY104
ZY105
ZY106
ZY107
ZY108
ZY109
ZY110
ZY111
ZY112
ABALL1
BBALL1
ABALL2
BBALL2
ABALL 3
BBALL 3
ABALL4
BBALL4

X

| 0.00041 | 0.00036 |
| :--- | :--- |
| 0.00039 | 0.00036 |
| 0.00034 | 0.00040 |
| 0.00032 | 0.00041 |
| 0.00036 | 0.00038 |
| 0.00040 | 0.00036 |
| 0.00041 | 0.00035 |
| 0.00038 | 0.00036 |
| 0.00033 | 0.00040 |
| 0.00033 | 0.00041 |
| 0.00037 | 0.00038 |
| 0.00040 | 0.00037 |
| 0.00031 | 0.00036 |
| 0.00031 | 0.00036 |
| 0.00031 | 0.00038 |
| 0.00031 | 0.00037 |
| 0.00031 | 0.00038 |
| 0.00031 | 0.00037 |
| 0.00031 | 0.00039 |
| 0.00031 | 0.00039 |

Z
0.00020
0.00020
0.00019
0.00019
0.00020
0.00020
0.00020
0.00020
0.00019
0.00019
0.00020
0.00020
0.00033
0.00029
0.00035
0.00030
0.00034
0.00030
0.00041
0.00028

Station Coordinate Error Ellipses Confidence Region $=95 \%$

| Semi-Major | Semi-Minor |  |
| :---: | :---: | :---: |
| Axis | Axis | Azimuth of <br> Major Axis |
| 0.00101 | 0.00087 | $102-29$ |
| 0.00102 | 0.00080 | $125-55$ |
| 0.00101 | 0.00080 | $157-04$ |
| 0.00101 | 0.00077 | $10-05$ |
| 0.00101 | 0.00078 | $41-15$ |
| 0.00101 | 0.00086 | $65-57$ |
| 0.00101 | 0.00086 | $101-45$ |
| 0.00101 | 0.00079 | $126-25$ |
| 0.00101 | 0.00077 | $157-20$ |
| 0.00101 | 0.00079 | $10-55$ |
| 0.00102 | 0.00079 | $41-34$ |
| 0.00101 | 0.00088 | $65-32$ |
| 0.00090 | 0.00075 | $172-18$ |
| 0.00089 | 0.00075 | $172-56$ |
| 0.00092 | 0.00074 | $171-09$ |
| 0.00092 | 0.00075 | $170-58$ |
| 0.00093 | 0.00074 | $169-55$ |
| 0.00092 | 0.00075 | $169-51$ |
| 0.00096 | 0.00075 | $178-52$ |
| 0.00095 | 0.00075 | $0-18$ |

\# M.A. Goldman

STAR*NET Project: ELBEBRL
March 04, 1997 Version 4.8

This is a data file for preanalysis simulating a set of measurements from certain ground laser ranging stations to TWO PAIRS of ball retroreflectors, each pair mounted approximately 101 inches below the alidade structure upper weldment deck at each end of the elevation bearing.

The pairs of elevation bearing balls will be represented by quadruples of balls at 10 degree azimuth increments clockwise (ABALI and CBALI move Eastward), to simulate rotation of the alidade.

The pair of balls mounted on a common fixture on each end of the elevation shaft is assumed to be fixtured so that the line of ball of ball centers will be oriented perpendicular to the shaft, to $1 / 12$ degree standard error (300 arc seconds).

A balls and $C$ balls are at one end of the elevation shaft. $B$ and $D$ balls are at the other end of the shaft. The $A$ and $D$ balls are viewed from one side of the elevation shaft (the left side as seen from the $A$ ball, looking along the elevation shaft). The $B$ and $C$ balls are viewed by stations on the other side of the elevation shaft.

Ranging station scan point horizontal coordinates will be assumed known a-priori to a standard error of lmm. We use a free adjustment, assuming that no ground station scan points are fixed, but that the ground station distances to first and second nearest neighbor scan points are ranged on one another to 0.15 mm . THIS IS A FREE ADJUSTMENT, WITH NO FIXED RANGING STATION SCAN POINTS.

The Z-coordinate of each station scan point is assumed to be known a-priori to 0.20 mm standard error. (This is found by a levelling survey, with a small correction for earth curvature).

Each ball center $Z$ coordinate is assumed, a-priori, to be 1900" - 46" - 91" $-10^{\prime \prime}=1754^{\prime \prime}$ (44.526 meter), with 0.30 meter standard error.
$A$ and B Balls are assumed a-priori to be 52 meter apart. C and D Balls are assumed a-priori to be 52 meter apart.

The distance between the $A$ and $C$ balls is assumed to be 0.25 meters and measured accurately in the laboratory to 50 um. This is a distance fixed by their mounting on a common fixture for installation under the weldment. The distance is also 0.25 meter between the $B$ and $D$ balls, measured to 50 um.

The quadruplet of balls corresponding to a particular alidade azimuth will be called ABA工I(n), BBA工L(n), CBAIL(n), DBALI(n).

Version 4.4. THIS MODEL ASSUMES A STANDARD ERROR OF 0.20 MM ON THE Z-COORDINATE OF EACH RANGING STATION.

Ball ranges are assumed measured to 150 um standard error (0.006").

In this model we use the fact that the balls almost lie in a horizontal plane, and can assume that their zenith angles (viewed from one another) to vertical are nearly 90 degrees. (We assume $1 / 12$ degree Standard Error).

We assume that we can oxient the ball mounting fixtures during installation on the alidade so the angles $B-A-C$ and $A-B-D$ are known (by proper orientational setting during installation and subsequent measurement) to a standard error of $1 / 12$ degree.

These angles should be each be set to 90 degrees on installation. That is, the ball lines $A B$ and $A C$, and $A B$ and $B D$ should cross at 90 degrees.

ENTER LASER RANGING GROUND-STATION SCAN POINT COORDINATES
(METERS)

| \# | POINT | $\begin{gathered} \mathbf{X} \\ (E A S T) \end{gathered}$ | $\begin{gathered} \mathbf{Y} \\ \text { (NORTH) } \end{gathered}$ | Z | Standard Exror |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \# |  |  |  |  | S (X) | $s$ (Y) | s (Z) |
| C | ZY101 | 018.4894 | 118.5670 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY102 | 075.2958 | 093.4370 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY103 | 111.9268 | 043.2712 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY104 | 118.5670 | -018.4894 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY105 | 093.4374 | -075.2958 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY106 | 043.2712 | -111.9268 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY107 | -018.4894 | -118.5670 | 0.0 | 0.001 | 0.001 | $!$ |
| C | ZY108 | -075.2958 | -093.4374 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY109 | -111.9268 | -043.2712 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY110 | -118.5670 | 018.4894 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY111 | -093.4374 | 075.2958 | 0.0 | 0.001 | 0.001 | 0.0002 |
| C | ZY112 | -043.2712 | 111.9268 | 0.0 | 0.001 | 0.001 | 0.0002 |

\# ENTER ELEVATION BEARING BALL REFLECTOR COORDINATES (METERS)

| C | ABALLI | 00.1250 | 26.0000 | 44.526 | 1.0 | 1.0 | 1.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C | CBALII | -00.1250 | 26.0000 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | BBALL1 | -00.1250 | -26.0000 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | DBALII | 00.1250 | -26.0000 | 44.526 | 1. 0 | 1.0 | 1.0 |
| C | ABALL2 | 04.63795 | 25.58330 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | CBALI2 | 04.39175 | 25.62671 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | BBALL2 | -04.63795 | -25.58330 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | DBALL2 | -04.39175 | -25.62671 | 44.526 | 1.0 | 1.0 | 1.0 |


| C | ABALI3 | 09.00999 | 24.38926 | 44.526 | 1.0 | 1.0 | 1.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C | CBALI3 | 08.77506 | 24.47476 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | BBALI3 | －09．00999 | －24．38926 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | DBALI3 | －08．77506 | －24．47476 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | ABALL 4 | 13.10825 | 22.45416 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | CBALI4 | 12.89175 | 22.57916 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | BBALL4 | －13．10825 | －22．45416 | 44.526 | 1.0 | 1.0 | 1.0 |
| C | DBALI4 | －12．89175 | －22．57916 | 44.526 | 1.0 | 1.0 | 1.0 |

ENTER LASER RANGE TO BALL CENTER STD ERRORS（METERS）

| ZY102－ABALIL | 0.00015 |
| :---: | :---: |
| ZY103－ABAL工1 | 0.00015 |
| ZY111－CBALL1 | 0.00015 |
| ZY110－CBALI1 | 0.00015 |
| ZY104－BBALII | 0.00015 |
| ZY105－BBALI | 0.00015 |
| ZY108－DBAL工1 | 0.00015 |
| ZY109－DBALII | 0.00015 |
| ZY103－ABALI2 | 0.00015 |
| ZY104－ABAL工2 | 0.00015 |
| ZY110－CBALL2 | 0.00015 |
| ZY109－CBAL工2 | 0.00015 |
| ZY106－BBALL2 | 0.00015 |
| ZY105－BBAL工2 | 0.00015 |
| ZY109－DBALI2 | 0.00015 |
| ZY108－DBALI2 | 0.00015 |
| ZY109－BBALI2 | 0.00015 |


| ZY103－ABAL工3 | 0.00015 |
| :---: | :---: |
| ZY104－ABALI3 | 0.00015 |
| ZY110－CBALI3 | 0.00015 |
| ZY109－CBALI3 | 0.00015 |
| ZY106－BBALI3 | 0.00015 |
| ZY105－BBALI3 | 0.00015 |
| ZY104－BBALL3 | 0.00015 |
| ZY108－DBALI3 | 0.00015 |
| ZY109－DBALI3 | 0.00015 |
| ZY103－ABALI4 | 0.00015 |
| ZY104－ABAL工4 | 0.00015 |
| ZY105－ABALI4 | 0.00015 |
| ZY109－CBALI4 | 0.00015 |
| ZY110－CBAL工4 | 0.00015 |
| ZY104－BBALL4 | 0.00015 |
| ZY105－BBALL4 | 0.00015 |
| ZY109－DBALL4 | 0.00015 |
| ZY110－DBALL4 | 0.00015 |
| ZY111－DBALL4 | 0.00015 |


| ZY111-ZY101 | 0.00015 |
| :--- | :--- |
| ZY112-ZY101 | 0.00015 |
| ZY112-ZY102 | 0.00015 |
| ZY101-ZY102 | 0.00015 |
| ZY101-ZY103 | 0.00015 |
| ZY102-ZY103 | 0.00015 |
| ZY102-ZY104 | 0.00015 |
| ZY103-ZY104 | 0.00015 |
| ZY103-ZY105 | 0.00015 |
| ZY104-ZY105 | 0.00015 |
| ZY104-ZY106 | 0.00015 |
| ZY105-ZY106 | 0.00015 |
| ZY105-ZY107 | 0.00015 |
| ZY106-ZY107 | 0.00015 |
| ZY106-ZY108 | 0.00015 |
| ZY107-ZY108 | 0.00015 |
| ZY107-ZY109 | 0.00015 |
| ZY108-ZY109 | 0.00015 |
| ZY108-ZY110 | 0.00015 |
| ZY109-ZY110 | 0.00015 |
| ZY109-ZY111 | 0.00015 |
| ZY110-ZY111 | 0.00015 |
| ZY110-ZY112 | 0.00015 |
| ZY111-ZY112 | 0.00015 |

ENTER ASSUMED BALL-TO-BALL DISTANCE STANDARD ERROR

| ABALLL1-BBALLI | 1.0 |
| :--- | :--- |
| CBALL1-DBALLI | 1.0 |
| ABALL1-CBALL1 | 0.00005 |
| BBALLL-DBALLL | 0.00005 |
|  |  |
| ABALL2-BBALL2 | 1.0 |
| CBALL2-DBALL2 | 1.0 |
| ABALL2-CBALL2 | 0.00005 |
| BBALL2-DBALL2 | 0.00005 |
| ABALL3-BBALL3 | 1.0 |
| CBALL3-DBALL3 | 1.0 |
| ABALL3-CBALL3 | 0.00005 |
| BBALL3-DBALL3 | 0.00005 |
|  |  |
| ABALL4-BBALL4 | 1.0 |
| CBALL4-DBALL4 | 1.0 |
| ABALL4-CBALL4 | 0.00005 |
| BBALL4-DBALL4 | 0.00005 |

DN DEALL1 00-00-00 0.01

BBALI 1

CBALL1

DN DE
DB CBALL2

DBALL1

BBALLL 2

CBALL2

DBALL2

ABALL 3
BBALL 3

BBALLI 3

CBALL3
DBALL 3
ABALL 3

ENTER ASSUMED INSTALLATION BALL (HORIZ.) ORIENTION ANGLE \& STD. ERROR

ABALLI
BBALII 00-00-00 0.01
CBALLI 270-00-00 300.0
\# Ref. station. Begin direction set.
\# Direction (D-M-S) and S.E. (Sec).
\# Assume 1/12 degree S.E.
\# End direction data set entry.

ABALL1 00-00-00 0.01
DBALL1 90-00-00 300.0 ABALLI 90-00-00 300.0

CBALLI 00-00-00 0.01
BBALLI 270-00-00 300.0

| ABALL2 |  |  |
| :--- | ---: | :--- |
| BBALL2 | $00-00-00$ | 0.01 |
| CBALL2 | $270-00-00$ | 300.0 |

ABALL2 00-00-00 0.01
DBALL2 90-00-00 300.0

DBALL2 00-00-00 0.01
ABALL2 $\quad 90-00-00 \quad 300.0$

CBALL2 00-00-00 0.01
BBALL2 270-00-00 300.0

CBALL3 270-00-00 300.0

АВАLL3 00-00-00 0.01
DBALL3 90-00-00 300.0

00-00-00
0.01 90-00-00 300.0

DB
DN
DN
DE

DB ABALL4
DN BBALL4 DN DE DB DN DN DE

DBALL3

BBALL4

> CBALL3 00-00-00 0.01

BBALL3 270-00-00 300.0

BBALL4 00-00-00 0.01
CBALL4 270-00-00 300.0

ABALL4 00-00-00 0.01
DBALL4 90-00-00 300.0

DB CBALL4

| DN | DBALL4 | $00-00-00$ | 0.01 |
| :--- | :--- | :--- | :--- |
| DN | ABALL4 | $90-00-00$ | $\mathbf{3 0 0 . 0}$ |

DE
DB DBALL4
DN
DN CBALL4

00-00-00 0.01
BBALL4 270-00-00 300.0

ENTER ASSUMED ZENITH ANGLE (D-M-S) \& STD. ERROR (SEC)

| ABALL1-BBALL1 | $90-00-00$ | 300.0 |
| :--- | :--- | :--- |
| ABALL1-CBALL1 | $90-00-00$ | 300.0 |
| CBALL1-DBALL1 | $90-00-00$ | 300.0 |
| BBALL1-DBALL1 | $90-00-00$ | 300.0 |
|  |  |  |
| ABALL2-BBALL2 | $90-00-00$ | 300.0 |
| ABALL2-CBALL2 | $90-00-00$ | 300.0 |
| CBALL2-DBALL2 | $90-00-00$ | 300.0 |
| BBALL2-DBALL2 | $90-00-00$ | 300.0 |

ABALL3-BBALL3
ABALL3-CBALL3
CBALL3-DBALL3
BBALL3-DBALL3

| $90-00-00$ | 300.0 |
| :--- | :--- |
| $90-00-00$ | 300.0 |
| $90-00-00$ | 300.0 |
| $90-00-00$ | 300.0 |

ABALL4-BBALL 4
90-00-00 300.0

| V | ABALL4-BBALL4 | $90-00-00$ | 300.0 |
| :--- | :--- | :--- | :--- |
| V | ABALL4-CBALL4 | $90-00-00$ | 300.0 |
| V | CBALL4-DBALL4 | $90-00-00$ | 300.0 |
| V | BBALL4-DBALL4 | $90-00-00$ | 300.0 |





Summary of Files Used

| Project Directory | C: \STAR |  |
| :--- | :--- | :--- |
| Input Data File |  |  |
| Output Listing (This File) | ELBEBRL.DAT |  |
| Coordinates | ELBEBRL.LST | (Version 4.8) |
| Project Parameters | ELBEBRL.PTS |  |
| Error Log | ELBEBRL.PRJ |  |
| Plot File | ELBEBRL.ERR |  |

Adjustment Options

| STAR*NET Run Mode | Preanalysis |
| :---: | :---: |
| Type of Adjustment | 3D |
| Input Order for Coordinates | X,Y, Z |
| Coordinate System | LOCAL |
| Project Scale Factor | : 1.00000000 |
| Linear Units; Angular Units | Meters; DMS |
| Input Order for Angle Stations | At-From-To |
| Max Iterations; Convergence Limit | 50; 0.0001 |
| Correct Zeniths for Curve \& Refract | No |
| Adjust 3D Obs for Vert Divergence | No |
| 3D Data Input Mode | Slope/Zenith |
| Earth Radius | : 6372161.544 Meters |
| Coefficient of Refraction | 0.070 |

Default Instrument Standard Error Settings
Distances ( Constant ) : 0.0001000 Meters
Distances ( PPM )
0.0000010

Angles
Directions
Azimuth / Bearings
1.4140000 Seconds

Zeniths
Elevation Differences ( Constant )
1.0000000 Seconds
2.0000000 Seconds
2.0000000 Seconds
0.0001000 Meters

Elevation Differences ( PPM )
0.0000010

Centering Error Instrument
0.0000100 Meters

Centering Error Target

|  | Summary of Unadjusted Input Observations <br>  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Number of Stations (Meters) $=28$ |  |  |  |
| Partially Fixed | X | Y | z | Description |
|  | SE-X | SE-Y | SE-Z |  |
| ZY101 | 18.4894 | 118.5670 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY102 | 75.2958 | 93.4370 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY103 | 111.9268 | 43.2712 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY104 | 118.5670 | -18.4894 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY105 | 93.4374 | -75.2958 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY106 | 43.2712 | -111.9268 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY107 | -18.4894 | -118.5670 | 0.0000 |  |
|  | 0.0010 | 0.0010 | FIXED |  |
| ZY108 | -75.2958 | -93.4374 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY109 | -111.9268 | -43.2712 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY110 | -118.5670 | 18.4894 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY111 | -93.4374 | 75.2958 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ZY112 | -43.2712 | 111.9268 | 0.0000 |  |
|  | 0.0010 | 0.0010 | 0.0002 |  |
| ABALLI | 0.1250 | 26.0000 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| CBALLI | -0.1250 | 26.0000 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| BBALL 1 | -0.1250 | -26.0000 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| DBALLI | 0.1250 | -26.0000 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| ABALL2 | 4.6380 | 25.5833 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| CBALL2 | 4.3918 | 25.6267 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| BBALL2 | -4.6380 | -25.5833 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| DBALL2 | -4.3918 | -25.6267 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| ABALL 3 | 9.0100 | 24.3893 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| CBALL 3 | 8.7751 | 24.4748 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| BBALL3 | -9.0100 | -24.3893 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| BBALL 3 | -8.7751 | -24.4748 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| ABALL 4 | 13.1083 | 22.4542 | 44.5260 |  |
|  | 1.0000 | 1.0000 | 1.0000 |  |
| CBALL4 | 12.8918 | 22.5792 | 44.5260 |  |
|  |  | 37 |  |  |


|  |  | 1.0000 | 1.0000 | 1.0000 |
| :---: | :---: | :---: | :---: | :---: |
| BBALL 4 |  | -13.1083 | -22.4542 | 44.5260 |
|  |  | 1.0000 | 1.0000 | 1.0000 |
| DBALL4 |  | -12.8918 | -22.5792 | 44.5260 |
|  |  | 1.0000 | 1.0000 | 1.0000 |
|  |  | Number of Direction Observations $=32$ |  |  |
| From | To | Direction | StdErr |  |
| ABALLI | BBALLI | 180-16-31.65 | 0.08 |  |
| ABALLI | CBALLI | 270-00-00.00 | 300.45 |  |
| BBALLI | ABALLI | 0-16-31.65 | 0.08 |  |
| BBALLI | DBALLI | 90-00-00.00 | 300.45 |  |
| CBALLI | DBALLI | 179-43-28.35 | 0.08 |  |
| CBALL1 | ABALLI | 90-00-00.00 | 300.45 |  |
| DBALLI | CBALII | 359-43-28.35 | 0.08 |  |
| DBALL1 | BBALI 1 | 270-00-00.00 | 300.45 |  |
| ABALL2 | BBALL2 | 190-16-31.62 | 0.08 |  |
| ABALL2 | CBALL2 | 279-59-58.62 | 300.45 |  |
| BBALL 2 | ABALL2 | 10-16-31.62 | 0.08 |  |
| BBALL2 | DBALL2 | 99-59-58.62 | 300.45 |  |
| CBALL2 | DBALL2 | 189-43-28.33 | 0.08 |  |
| CBALL2 | ABALL2 | 99-59-58.62 | 300.45 |  |
| DBALL2 | CBALL2 | 9-43-28.33 | 0.08 |  |
| DBALL2 | BBALL2 | 279-59-58.62 | 300.45 |  |
| ABALL 3 | BBALL 3 | 200-16-31.67 | 0.08 |  |
| ABALL 3 | CBALL3 | 289-59-54.16 | 300.45 |  |
| BBALL 3 | ABALL 3 | 20-16-31.67 | 0.08 |  |
| BBALL 3 | DBALL 3 | 109-59-54.16 | 300.45 |  |
| CBALL3 | DBALL3 | 199-43-28.34 | 0.08 |  |
| CBALL 3 | ABALL 3 | 109-59-54.16 | 300.45 |  |
| DBALL3 | Cball 3 | 19-43-28.34 | 0.08 |  |
| DBALL 3 | BBALL3 | 289-59-54.16 | 300.45 |  |
| ABALL 4 | BBALL4 | 210-16-31.63 | 0.08 |  |
| ABALL 4 | CBALL4 | 300-00-02.62 | 300.45 |  |
| BBALL 4 | ABALL4 | 30-16-31.63 | 0.08 |  |
| BBALL 4 | DBALL 4 | 120-00-02.62 | 300.45 |  |
| CBALL4 | DBALL4 | 209-43-28.37 | 0.08 |  |
| CBALL4 | ABALL 4 | 120-00-02.62 | 300.45 |  |
| DBALL4 | CBALL 4 | 2.9-43-28.37 | 0.08 |  |
| DBALL4 | BBALL4 | 300-00-02.62 | 300.45 |  |

Number of Distance Observations (Meters) $=76$

| From | To | Obs Dist | StdErr | HI | HT | Flags |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZY102 | ABALII | 110.3674 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALI 1 | 121.5751 | 0.0001 | 0.000 | 0.000 | S |
| ZY111 | CBALI 1 | 114.5419 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | CBALI 1 | 126.7576 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | BBALI 1 | 126.9912 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALI 1 | 114.7456 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | DBALI 1 | 110.5381 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | DBAL工1 | 121.8050 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALL2 | 117.5003 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALI2 | 130.0184 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | CBALL2 | 130.9670 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | CBALI2 | 142.3358 | 0.0001 | 0.000 | 0.000 | S |
| ZY106 | BBAL工2 | 108.3192 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALI2 | 118.6283 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | DBALI2 | 117.7186 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | DBALL2 | 107.7415 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | BBALL2 | 117.5003 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALL3 | 113.7144 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALL3 | 125.7930 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | CBALL3 | 135.0348 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | CBALL3 | 145.3995 | 0.0001 | 0.000 | 0.000 | S |
| ZY106 | BBALI3 | 111.2596 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALL3 | 122.7579 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | BBALL3 | 135.2526 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | DBALI3 | 105.6571 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | DBALI3 | 113.9129 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ABALI4 | 110.3677 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ABALI4 | 121.5750 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ABALL4 | 134.1283 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | CBALI4 | 147.9814 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | CBALL4 | 138.8549 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | BBALL4 | 139.0563 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | BBALI4 | 126.9913 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | DBALL4 | 110.5381 | 0.0001 | 0.000 | 0.000 | S |
| ZY110 | DBALI4 | 121.8050 | 0.0001 | 0.000 | 0.000 | S |
| ZY111 | DBALL4 | 134.3491 | 0.0001 | 0.000 | 0.000 | S |
| ZY111 | ZY101 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY112 | ZY101 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY112 | ZY102 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY101 | ZY102 | 62.1167 | 0.0001 | 0.000 | 0.000 | S |
| ZY101 | ZY103 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY102 | ZY103 | 62.1163 | 0.0001 | 0.000 | 0.000 | S |
| ZY102 | ZY104 | 119.9996 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ZY104 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY103 | ZY105 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ZY105 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY104 | ZY106 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ZY106 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ZY105 | ZY107 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY106 | ZY107 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY106 | ZY108 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY107 | ZY108 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY107 | ZY109 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | ZY109 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ZY108 | ZY110 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ZY110 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| ZY109 | ZY111 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |


| ZY110 | ZY111 | 62.1165 | 0.0001 | 0.000 | 0.000 | S |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZY110 | ZY112 | 120.0000 | 0.0001 | 0.000 | 0.000 | S |
| zY111 | ZY112 | 62.1166 | 0.0001 | 0.000 | 0.000 | S |
| ABALII | BBALII | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| CBALII | DBALII | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| ABALII | CBALI 1 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| BBALLI | DBALLI | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| ABALL2 | BBALL 2 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| CBALL2 | DBALL2 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| ABALL2 | CBALI2 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| BBALL2 | DBALL2 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| ABALI 3 | BBALI 3 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| CBALL3 | DBALL 3 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| ABALL3 | CBALI 3 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| BBALI 3 | DBALL 3 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| ABALL4 | BBALI 4 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| CBALL4 | DBALL4 | 52.0006 | 0.0001 | 0.000 | 0.000 | S |
| ABALL4 | CBALL4 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |
| BBALL4 | DBALI4 | 0.2500 | 0.0001 | 0.000 | 0.000 | S |

From
ABALLI CBALLI BBALII ABALL2 ABALL2 CBALL2 BBALL2 ABALLL ABALLL 3 CBALLL BBALL3 ABALI4 ABALI4 CBALL 4 BBALL4


To BBALLI CBALLI DBALLI DBALLI BBALL2 CBALL2 DBALIL 2 DBALL2 BBALLL CBALL3 DBALLE DBALL 3 BBALL4 CBALL4 DBALL4 DBALL4

Number of Zenith Observations $=16$

| Obs Zenith | StdErr | HI | HT | FIags |
| ---: | ---: | ---: | ---: | ---: |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |
| $90-00-00.00$ | 300.00 | 0.000 | 0.000 |  |

Adjusted Bearings and Horizontal Distances (Meters)

| From | To | Bearing | Distance | Relative |  | DistPrec (PPM) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | BgErr | DisErr |  |
| ZY102 | ABALLI | S48-06-15.05W | 100.9871 | 0.66 | 0.0002 | (2PM) |
| ZY103 | ABALLI | S81-13-06.01W | 113.1280 | 0.65 | 0.0002 | 1 |
| ZY111 | CBALLI | S62-09-10.99E | 105.5333 | 0.64 | 0.0002 | 1 |
| ZY110 | CBALLI | N86-22-17.90E | 118.6799 | 0.63 | 0.0002 | 1 |
| ZY104 | BBALLI | S86-22-45.34W | 118.9294 | 0.63 | 0.0001 | 1 |
| ZY105 | BBALLI | N62-12-58.76W | 105.7544 | 0.64 | 0.0002 | 1 |
| ZY108 | DBALLI | N48-11-54.80E | 101.1736 | 0.64 | 0.0002 | 1 |
| ZY109 | DBALLI | N81-14-15.44E | 113.3750 | 0.64 | 0.0001 | 1 |
| ZY103 | ABALL2 | S80-38-17.84W | 108.7371 | 0.69 | 0.0002 | 1 |
| ZY104 | ABALL2 | N68-51-04.92W | 122.1566 | 0.62 | 0.0002 | 1 |
| ZY110 | CBALL2 | N86-40-40.50E | 123.1657 | 0.64 | 0.0002 | 1 |
| ZY109 | CBALL2 | N59-21-39.07E | 135.1922 | 0.60 | 0.0002 | 1 |
| ZY106 | BBALL2 | N29-01-28.00W | 98.7446 | 0.62 | 0.0002 | 1 |
| ZY105 | BBALL2 | N63-07-13.55W | 109.9550 | 0.66 | 0.0001 | 1 |
| ZY109 | DBALL2 | N80-40-54.72E | 108.9730 | 0.65 | 0.0002 | 1 |
| ZY108 | DBALL2 | N46-16-38.97E | 98.1105 | 0.61 | 0.0002 | 2 |
| ZY109 | BBALL2 | N80-38-17.84E | 108.7371 | 0.66 | 0.0002 | 1 |
| ZY103 | AbALL3 | S79-36-13.24W | 104.6346 | 0.65 | 0.0002 | 1 |
| ZY104 | ABALL3 | N68-37-31.84W | 117.6491 | 0.59 | 0.0002 | 1 |
| 2Y110 | CBALL3 | N87-18-32.23E | 127.4826 | 0.62 | 0.0002 | 1 |
| ZY109 | CBALL3 | N60-41-45.40E | 138.4141 | 0.59 | 0.0002 | 1 |
| ZY106 | BBALL3 | N30-50-50.89W | 101.9615 | 0.57 | 0.0002 | 1 |
| ZY105 | BBALL3 | N63-34-37.29W | 114.3982 | 0.58 | 0.0002 | 1 |
| 2Y104 | BBALL3 | S87-21-07.97W | 127.7133 | 0.59 | 0.0001 | 1 |
| ZY108 | DBALL3 | N43-58-02.77E | 95.8168 | 0.63 | 0.0002 | 1 |
| ZY109 | DBALL3 | N79-40-22.08E | 104.8503 | 0.66 | 0.0002 | 1 |
| ZY103 | ABALL 4 | S78-06-14.58W | 100.9874 | 0.63 | 0.0002 | 1 |
| ZY104 | ABALL 4 | N68-46-54.03W | 113.1279 | 0.58 | 0.0002 | 1 |
| ZY105 | ABALL4 | N39-24-45.89W | 126.5220 | 0.56 | 0.0002 | 1 |
| ZY109 | CBALL4 | N62-11-06.99E | 141.1238 | 0.57 | 0.0001 | 1 |
| ZY110 | CBALL4 | N88-13-05.05E | 131.5224 | 0.59 | 0.0002 | 1 |
| ZY104 | BBALL4 | S88-16-31.21W | 131.7349 | 0.58 | 0.0001 | 1 |
| ZY105 | BBALL 4 | N63-37-14.69W | 118.9295 | 0.58 | 0.0001 | 1 |
| ZY109 | DBALL4 | N78-11-54.93E | 101.1736 | 0.60 | 0.0002 | 1 |
| ZY110 | DBALL4 | S68-45-44.59E | 113.3750 | 0.61 | 0.0002 | 1 |
| ZY111 | DBALL4 | S39-27-08.93E | 126.7561 | 0.59 | 0.0001 | 1 |
| ZY111 | ZY101 | N68-51-48.11E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY112 | ZY101 | N83-51-48.27E | 62.1165 | 0.88 | 0.0001 | 1 |
| ZY112 | ZY102 | S81-08-11.26E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY101 | ZY102 | S66-08-10.94E | 62.1167 | 1.03 | 0.0001 | 1 |
| ZY101 | ZY103 | S51-08-12.00E | 120.0000 | 0.68 | 0.0001 | 0 |
| ZY102 | ZY103 | S36-08-12.73E | 62.1163 | 0.72 | 0.0001 | 1 |
| ZY102 | ZY104 | S21-08-12.13E | 119.9996 | 0.57 | 0.0001 | 0 |
| ZY103 | ZY104 | S06-08-11.73E | 62.1165 | 0.68 | 0.0001 | 1 |
| ZY103 | ZY105 | S08-51-48.06W | 120.0000 | 0.57 | 0.0001 | 0 |
| ZY104 | ZY105 | S23-51-47.84W | 62.1165 | 0.64 | 0.0001 | 1 |
| ZY104 | ZY106 | S38-51-48.00W | 120.0000 | 0.55 | 0.0001 | 0 |
| ZY105 | ZY106 | S53-51-48.06W | 62.1166 | 0.67 | 0.0001 | 1 |
| ZY105 | ZY107 | S68-51-48.11W | 120.0000 | 0.60 | 0.0001 | 0 |
| ZY106 | ZY107 | S83-51-48.27W | 62.1165 | 0.83 | 0.0001 | 1 |
| ZY106 | ZY108 | N81-08-11.94W | 120.0000 | 0.56 | 0.0001 | 0 |
| ZY107 | ZY108 | N66-08-12.16W | 62.1165 | 0.84 | 0.0001 | 1 |
| ZY107 | ZY109 | N51-08-12.00W | 120.0000 | 0.61 | 0.0001 | 0 |


| ZY108 | 2Y109 | N36-08-11.94W | 62.1166 | 0.66 | 0.0001 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ZY108 | ZY110 | N21-08-11.89W | 120.0000 | 0.57 | 0.0001 | 0 |
| ZY109 | zY110 | N06-08-11.73W | 62.1165 | 0.66 | 0.0001 | 1 |
| ZY109 | zY111 | N08-51-48.06E | 120.0000 | 0.57 | 0.0001 | 0 |
| ZY110 | ZY111 | N23-51-47.84E | 62.1165 | 0.67 | 0.0001 | 1 |
| ZY110 | ZY112 | N38-51-48.00E | 120.0000 | 0.66 | 0.0001 | 0 |
| ZY111 | ZY112 | N53-51-48.06E | 62.1166 | 1.03 | 0.0001 | 1 |
| ABALLI | BBALLI | S00-16-31.65W | 52.0006 | 0.84 | 0.0001 | 1 |
| CBALLI | DBALLI | S00-16-31.65E | 52.0006 | 0.84 | 0.0001 | 1 |
| ABALLI | CBALLI | S90-00-00.00W | 0.2500 | 148.44 | 0.0001 | 403 |
| BBALLI | DBALLI | S90-00-00.00E | 0.2500 | 145.40 | 0.0001 | 403 |
| ABALL2 | BBALL2 | S10-16-31.62W | 52.0006 | 0.78 | 0.0001 | 1 |
| CBALI2 | DBALL2 | S09-43-28.33W | 52.0006 | 0.84 | 0.0001 | 1 |
| ABALL2 | CBALL2 | N80-00-01.38W | 0.2500 | 142.33 | 0.0001 | 403 |
| BBALL2 | DBALL2 | S80-00-01.38E | 0.2500 | 139.13 | 0.0001 | 370 |
| ABALL3 | BBALL3 | S20-16-31.67W | 52.0006 | 0.83 | 0.0001 | 1 |
| CBALL3 | DBALL3 | S19-43-28.34W | 52.0006 | 0.84 | 0.0001 | 1 |
| ABALL3 | CBALL3 | N70-00-05.84W | 0.2500 | 143.14 | 0.0001 | 402 |
| BBALL3 | DBALL3 | S70-00-05.84E | 0.2500 | 139.33 | 0.0001 | 400 |
| ABALL 4 | BBALL4 | S30-16-31.63W | 52.0006 | 0.82 | 0.0001 | 1 |
| CBALL 4 | DBALL4 | S29-43-28.37W | 52.0006 | 0.83 | 0.0001 | 1 |
| ABALL4 | CBALL4 | N59-59-57.38W | 0.2500 | 143.88 | 0.0001 | 401 |
| BBALL4 | DBALL4 | S59-59-57.38E | 0.2500 | 143.38 | 0.0001 | 402 |

Station Coordinate Standard Deviations

Station ZY101 ZY102 ZY103 ZY104 ZY105 ZY106 ZY107
ZY108
ZY109
ZY110
ZY111
ZY112
ABALLII
CBALLI
BBALLI
DBALLI
ABALLL 2
CBALLL 2
BBALL2
DBALL2
ABALL 3
CBALL 3
BBALL 3
DBALL3
ABALL4
CBALL4
BBALL4
DBALL4

Station
ZY101
ZY102
ZY103
ZY104
ZY105
ZY106
ZY107
ZY108
ZY109
ZY110
ZY111
ZY112
ABALLI
CBALLI
RBALLI LBALL1 ABALL2
X
0.00041
0.00039
0.00034
0.00031
0.00035
0.00040
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0.00032

| $\mathbf{Y}$ | $\mathbf{Z}$ |
| :---: | :---: |
| 0.00036 | 0.00020 |
| 0.00036 | 0.00020 |
| 0.00040 | 0.00019 |
| 0.00041 | 0.00019 |
| 0.00037 | 0.00019 |
| 0.00033 | 0.00019 |
| 0.00034 | 0.00000 |
| 0.00035 | 0.00019 |
| 0.00040 | 0.00019 |
| 0.00041 | 0.00019 |
| 0.00038 | 0.00020 |
| 0.00036 | 0.00020 |
| 0.00037 | 0.00038 |
| 0.00036 | 0.00039 |
| 0.00037 | 0.00033 |
| 0.00036 | 0.00033 |
| 0.00038 | 0.00040 |
| 0.00038 | 0.00041 |
| 0.00038 | 0.00033 |
| 0.00037 | 0.00039 |
| 0.00036 | 0.00040 |
| 0.00037 | 0.00041 |
| 0.00035 | 0.00036 |
| 0.00037 | 0.00034 |
| 0.00034 | 0.00038 |
| 0.00036 | 0.00039 |
| 0.00035 | 0.00033 |
| 0.00034 | 0.00031 |

Station Coordinate Error Ellipses Confidence Region $=95 \%$

| Semi-Major | Semi-Minor | Azimuth of <br> Axis |
| :---: | :---: | :---: |
| 0.00101 | 0.00087 | Major Axis |
| 0.00101 | 0.00080 | $101-30$ |
| 0.00101 | 0.00079 | $125-51$ |
| 0.00101 | 0.00075 | $157-13$ |
| 0.00101 | 0.00075 | $9-10$ |
| 0.00101 | 0.00077 | $39-01$ |
| 0.00101 | 0.00083 | $68-33$ |
| 0.00101 | 0.00076 | $99-27$ |
| 0.00101 | 0.00075 | $128-59$ |
| 0.00101 | 0.00078 | $157-52$ |
| 0.00101 | 0.00079 | $10-13$ |
| 0.00101 | 0.00086 | $42-26$ |
| 0.00090 | 0.00078 | $66-25$ |
| 0.00089 | 0.00078 | $171-48$ |
| 0.00089 | 0.00078 | $174-27$ |
| 0.00089 | 0.00078 | $174-00$ |
| 0.00093 | 0.00078 | $173-08$ |
|  |  | $174-45$ |

CBALL2
BBALL2
DBALL2
ABALLL
CBALLL
BBALL3
DBALL 3
ABALL4 CBALL4 BBALL4 DBALL4

| 0.00093 | 0.00077 | $170-29$ |
| :--- | ---: | ---: |
| 0.00093 | 0.00076 | $10-21$ |
| 0.00091 | 0.00079 | $8-54$ |
| 0.00088 | 0.00078 | $168-26$ |
| 0.00091 | 0.00077 | $169-36$ |
| 0.00087 | 0.00078 | $167-28$ |
| 0.00090 | 0.00078 | $173-52$ |
| 0.00084 | 0.00079 | $169-17$ |
| 0.00087 | 0.00077 | $169-53$ |
| 0.00085 | 0.00077 | $1-52$ |
| 0.00083 | 0.00078 | $5-44$ |

Elapsed Time $=00: 00: 02$

