

North American ALMA Science Center



Interferometry Basics for ALMA Community Days

NAASC Memo #104

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ABSTRACT

These Interferometry Basics slides were included as part of the NA ALMA mm considerations presentation prepared by T. Hunter and C. Brogan. They include material from the NRAO Synthesis Imaging School, as well as from presentations of other ALMA Community Days, in particular the one at Caltech. The attached version is the presentation used in the ALMA Early Science Proposal Preparation Tutorial held in Charlottesville (Apr 26-27, 2011). Further updated versions of this presentation can be found at: https://sites.google.com/site/almacommunityoutreach/community-day-agendas/cde-powerpoint-slides.

Interferometry Basics and MM Observing Considerations



Nuria Marcelino North American ALMA Science Center

> Atacama Large Millimeter/submillimeter Array Expanded Very Large Array Robert C. Byrd Green Bank Telescope Very Long Baseline Array



Overview of Talk



- **Perspective:** Getting time on ALMA will be competitive!
 - The math: only ~600 hours for ES cycle 0
 at ~6 hours per project → ~100 projects split over the world
- Motivation: While ALMA is for everyone, a technical justification is required for each proposal, so you need to know some of the details of how the instrument works
- **Goal:** Do the best job you can to match your science to ALMA's capabilities





- Angular resolution
- Sensitivity
- Spectral resolution
- Image quality: UV coverage
- Source characteristics
- Calibration





- Angular resolution Single-dish: ~ λ / D
 - Interferometer: ~ λ / D_{max}

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Interferometers: the basics

- Interferometry: a method to 'synthesize' a large aperture by combining signals collected by separated small apertures
- An Interferometer measures the interference pattern produced by two apertures, which is related to the source brightness.
- The signals from all antennas are correlated, taking into account the distance (baseline) and time delay between pairs of antennas



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Interferometers: the basics





Interferometers: the basics





- Amplitude tells "how much" • of a certain frequency component
- Phase tells "where" this ۲ component is located





Visibility and Sky Brightness

For small fields of view: the complex visibility, V(u,v), is the 2D Fourier transform of the brightness on the sky, T(x,y)

$$V(u,v) = \int \int T(x,y) e^{2\pi i (ux+vy)} dx dy$$

 $T(x,y) = \int \int V(u,v) e^{-2\pi i (ux+vy)} du dv$

- u,v (wavelengths) are spatial frequencies in E-W and N-S directions, i.e. the baseline lengths
- x,y (rad) are angles in tangent plane relative to a reference position in the E-W and N-S directions









narrow features transform to wide features (and vice-versa)

2D Fourier Transforms



T(x,y)elliptical Gaussian



 $Amp{V(u,v)}$

elliptical Gaussian

Disk

NRAC



sharp edges result in many high spatial frequencies

Visibility: Amplitude and Phase ALMA



Visibility: Amplitude and Phase ALMA



Aperture Synthesis



- Sample V(u,v) at enough points to synthesis the equivalent large aperture of size (u_{max},v_{max})
 - I pair of telescopes \rightarrow I (u,v) sample at a time
 - N telescopes \rightarrow number of samples = N(N-1)/2 ("snapshot")
- A good image quality requires a good coverage of the uv plane
 - fill in (u,v) plane by making use of Earth rotation ("track")
 - reconfigure physical layout of N telescopes





RA offset (arcsec; J2000)

RA offset (arcsec; J2000)

(Image sequence taken from Summer School lecture by D.Wilner)

400

200

-200

-400

-400

NRAO

-200

0

 $u(k\lambda)$

200

400

v (kλ) 0

2 Antennas ß DEC offset (arcsec; J2000) 0

ŝ

5



0.5

0

-0.5

 $^{-5}$



0

RA offset (arcsec; J2000)



















7 Antennas



ALMA ES Proposal Preparation Tutorial Charlottesville, April 26, 2011 21







8 Antennas x 6 Samples





8 Antennas x 30 Samples





8 Antennas x 60 Samples





8 Antennas x 120 Samples





8 Antennas x 240 Samples



ALMA ES Proposal Preparation Tutorial Charlottesville, April 26, 2011



8 Antennas x 480 Samples



From Visibilities to Images



- Fourier transform of the measured V(u,v) to the image plane $\rightarrow T^{D}(x,y)$
- But difficult to do science on dirty image
- To determine (model of) T(x,y) we need to deconvolve b(x,y) from $T^{D}(x,y) \rightarrow$ "clean" image





Deconvolution



- Aims to find a **sensible** model of T(x,y) compatible with data without sidelobes
- Uses non-linear techniques to interpolate/extrapolate samples of V(u,v) into unsampled regions of the (u,v) plane
- Requires knowledge of beam shape and *a priori* assumptions about T(x,y)
- One of the most common algorithms in radio astronomy is the algorithm CLEAN (Hogbom 1974)





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Sensitivity calculator



https://almascience.nrao.edu/call-for-proposals/sensitivity-calculator

	Common Parameters									
A 6 ~	T_{sys}		Dec		00:00:00.000					
$\Delta S \propto -D$	$\left[n_p N(N-1) \Delta \nu \Delta t \right]^{1/2}$		Polarization		Dual		÷			
	= # polarizations = # antennas /= channel width		Observing Frequency		230.0 GHz		GHz 🛟			
п _р –			Bandwidth per Polarization		1.0 km/s		km/s 🛟			
N =			Water Vapour Column Density		Calculator Chooses		•	•		
Δν=			tau/Tsky	4	tau=0.136, Tsky=37.814 K					
Δt =	total time		Tsys		155.427 К					
	Individual Parameters									
		12m Arra	ay		7m Array 0			Total Power Array		
	Number of Antennas	16						1		
	Resolution1.0Sensitivity(rms)0.04802(equivalent to)1.22370		arcsec		÷	8.961831 arcsec		22.404577 arcsec		
			2 Ју 0 К		\$	Infinity	Jy 🛟	Infinity	Jy 🛟	
					÷	Infinity	K 🛟	Infinity	К	
	Integration Time 1.00000		0 min		+	0.00000	s 🗘	0.00000	s 🗘	
	Integration Time Unit Option Automatic									
	Calculate Integration Time Calculate Sensitivity									



Receiver Bands Available



3 mm

1.3 mm 0.87 mm

0.45 mm

- Only 4 of 8 bands are available for Early Science, all with dual linear polarization feeds
- Only 3 receiver bands can be "ready" at one • time (i.e. amplifiers powered on and stable temperature achieved). Required lead time to stabilize a new band is about 20 minutes.



- With configurations of \sim 125m and \sim 400m, approximately matched ٠ resolution is possible between Bands 3 and 7, or between Bands 6 and 9
- NRAC
- Matched resolution can be critical, for example to measure the SEDs of resolved sources.








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Correlator Modes, Spectral Resolution, Spectral Coverage - I

- Receivers are sensitive to two separate ranges of sky frequency: sidebands
- Each antenna has 4 digitizers which can each sample 2 GHz of bandwidth
- These 2 GHz chunks are termed **basebands**, and can be distributed among the sidebands (in ES: either all four in one, or two in both as shown below)





Correlator Modes, Spectral Resolution, Spectral Coverage - II ALMA



- In order to collect data, you need to set up a spectral window within one (or more) basebands.
- In Early Science, only 4 spectral windows are available, i.e. one per baseband, and all must have the same resolution and bandwidth
- **Note: exact spacing between sidebands and sideband widths vary from band to band – OT will show correct one for each band



Correlator Modes and Spectral						
Resolution Typical	Mode	Polari- zation	Bandwidth per baseband	Number of channels per	Channel Spacing (MHz)	Velocity width at 300 GHz
Durdoses:			(MHz)	baseband		(km/s)
рапросос. Г	7	Dual	1875	3840	0.488	0.48
Spectral scans	8	Dual	938	3840	0.244	0.24
	9	Dual	469	3840	0.122	0.12
Targeted imaging of moderately narrow lines: cold clouds / protoplanetary disks "Continuum" or broad lines	10	Dual	234	3840	0.061	0.06
	11	Dual	117	3840	0.0305	0.03
	12	Dual	58.6	3840	0.0153	0.015
	6	Single	58.6	7680	0.00763	0.008
	69	Dual	2000	128	15.625	15.6
	71	Single	2000	256	7.8125	7.8

- These numbers are per baseband (you can use up to 4 basebands)
- Usually want to have several channels across narrowest line
- Note that the resolution is ~ 2*channel width (Hanning)
 - The required spectral resolution typically needs to be justified as does the number of desired spectral windows



Correlator Setup line vs. continuum

Spectral line mode:



• "continuum mode": automatically place 4 spectral windows, with the largest bandwidth, across the sidebands



Band 3 (or 7)

Continuum mode:









Example: Spectral Lines in Band 9



- in Cycle 0, only one sideband per spectral window will be correlated
- for Band 9, there is full flexibility in that each baseband can be connected to either one or the other sideband
 - e.g. observe HD_2^+ at 691.66 GHz with one spectral window



• can place 3 additional windows in USB or LSB





• Band 9: 8 GHz continuum in a single side-band

Continuum placement in Band 9





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Image Quality

Sensitivity is not enough! Image quality also depends on UV coverage and density of UV samples

Image fidelity is improved when high density regions of UV coverage are well matched to source brightness distribution

→ The required DYNAMIC RANGE can be more important than sensitivity

→ALMA OT currently has no way to specify required image quality, but you can request more time in the Technical Justification

Does your setup need more time than is indicated by the time estimate?





Effects of UV Coverage







- Angular resolution
- Sensitivity
- Spectral resolution
- Image quality: UV coverage
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Sky coverage available



- ALMA is at a latitude of -23 degrees → Southern sky!
- Antenna elevation limit is technically 3 degrees
- But in practice, atmospheric opacity will cause significant degradation with lower elevation

 most severe at higher frequencies

Maximum length of observation for Northern sources (hrs)

	Dec	Elev > 15°	Elev > 20°	Elev > 30°
	+50	2.5	-	-
>	+40	5.8	4.3	-
	+30	7.3	6.3	3.9
	+20	8.4	7.5	5.7

Note: This table does not account for shadowing, which further impedes low elevation observations in compact configurations.



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Maximum Angular Scale



Band	Frequency	Primary	Maximum Angular Scale (")	
	(GHz)	beam (")	Compact	Extended
3	84-116	72 - 52	20	10
6	211-275	29 - 22	9	4.5
7	275-373	22 - 16	6	3
9	602-720	10 - 8.5	3	1.5

- Smooth structures larger than MAS are completely resolved out
- Begin to lose total recovered flux for objects on the order of half MAS

→ Need additional observations with a single-dish or a more compact array with smaller antennas



Sensitivity and Brightness Temperature



• There will be a factor of 10 difference in brightness temperature sensitivity between the 2 configurations offered in Early Science. Very important to take into account for resolved sources.

The conversion from brightness temperature T to flux S_v with synthesized beam solid angle Ω_s is

$$S_{\nu} = \frac{2 \nu^2 k T}{c^2} \Omega_s.$$

An alternate formula that is often useful is

$$\begin{pmatrix} \frac{T}{1K} \end{pmatrix} = \left(\frac{S_{\nu}}{1 \text{ Jy beam}^{-1}} \right) \left[13.6 \left(\frac{300 \text{ GHz}}{\nu} \right)^2 \left(\frac{1''}{\theta_{max}} \right) \left(\frac{1''}{\theta_{min}} \right) \right]$$

Example: I minute integration at 230 GHz with I km/sec channels:

Configuration	Angular resolution	Flux density Sensitivity	Brightness sensitivity
125 m	3"	32 mJy/beam	0.09 K
400 m	1"		0.82 K



 \rightarrow It is harder to detect extended line emission at high angular resolution !



- Angular resolution
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Observatory Default Calibration

- Need to measure and remove the (time-dependent and frequency-dependent) atmospheric and instrumental variations.
- Set calibration to system-defined calibration unless you have very specific requirements for calibration (which then must be explained in the Technical Justification). Defaults include (suitable calibrators are chosen at observation time):
 - I. Pointing, focus, and delay calibration
 - 2. Phase and amplitude gain calibration
 - 3. Absolute flux calibration
 - 4. Bandpass calibration
 - 5. System Temperature calibration
 - 6. Water-vapor radiometry correction

Spectral Spat	ial Calibration Setup Parameters Catalog			
Select calibration setup. If "system" is selected, the ALMA system will select default calibrators.				
Goal Calibrators				
Select <i>User-defined calibration</i> to choose your own calibrators, or <i>Sy</i> automatically select the calibrators to be observed.				
System-defined calibration				
 User-defined calibration 				



Future Capabilities



- Better sensitivity and image fidelity:
 - Imaging fidelity ~10x better, Sensitivity > 3x better
 - Fantastic "snapshot" uv-coverage (50 x 12m antennas = 1225 baselines)
- Higher angular resolution:
- baselines ~15km, matched beams possible in all bands
- Better imaging of resolved objects and mosaics
 - TPA: four additional 12m antennas with subreflector nutators
 - ACA: Atacama Compact configuration 12 x 7m antennas
 - "On-the-Fly" mosaics: quickly cover larger areas of sky
- More receiver bands: 4, 8, 10 (2mm, 0.7mm, 0.35mm)
- Polarization: magnetic fields and very high dynamic range imaging
- "Mixed" correlator modes (simultaneous wide & narrow, see A&A 462, 801)
- ALMA development program → studies just beginning



• mm VLBI, more receiver bands

• Higher data rates







www.almaobservatory.org

The Atacama Large Millimeter/submillimeter Array (ALMA), an international astronomy facility, is a partnership among Europe, Japan and North America, in cooperation with the Republic of Chile. ALMA is funded in Europe by the European Organization for Astronomical Research in the Southern Hemisphere, in Japan by the National Institutes of Natural Sciences (NINS) in cooperation with the Academia Sinica in Taiwan and in North America by the U.S. National Science Foundation (NSF) in cooperation with the National Research Council of Canada (NRC). ALMA construction and operations are led on behalf of Europe by ESO, on behalf of Japan by the National Radio Astronomical Observatory of Japan (NAOJ) and on behalf of North America by the National Radio Astronomy Observatory (NRAO), which is managed by Associated Universities, Inc. (AUI).







Visibility and Sky Brightness



- The Visibility is a complex quantity, which is the Fourier transform of the source Brightness
- Some simple and illustrative examples make use of 'delta functions' – sources of infinitely small extent, but finite total flux.





(from Summer School lecture by R. Perley)

Synthesized beam



Discrete sampling:
$$T'(x,y) = \iint W(u,v)V(u,v)e^{2\pi i(uv+vy)}dudv$$

The weighting function W(u,v) is 0 where V is not sampled

T'(x,y) is FT of the product of W and V, which is the convolution of the FT of V and W:

$$T'(x,y) = B(x,y) \otimes T(x,y)$$

$$B(x,y) = \iint W(u,v)e^{2\pi i(uv+vy)}dudv$$

B(x,y) is the synthesized beam, analogous of the point-spread function in an optical telescope.



(from CalTech CDE talk by A. Isella)

Weighting function



Measured flux:

$$T'(x,y) = B(x,y) \otimes T(x,y)$$

Synthesized beam:

$$B(x,y) = \iint W(u,v)e^{2\pi i(uv+vy)}dudv$$

You can change the angular resolution and sensitivity of the final image by changing the weighting function W(u,v)



(from CalTech CDE talk by A. Isella)

Weighting function



• "Natural" weighting: $W(u,v) = 1/\sigma^2(u,v)$, where $\sigma^2(u,v)$ is the noise variance of the (u,v) sample Advantage: gives the lowest noise in the final image, highlight extended

Advantage: gives the lowest noise in the final image, highlight extended structures.

Disadvantage: generally gives more weights to the short baseline (where there are more measurements of V) degrading the resolution

 "Uniform" weighting: W(u,v) is inversely proportional to the local density of (u,v) points. It generally gives more weights to the long baseline therefore leading to higher angular resolution.
 Advantage: better resolution and lower sidelobes
 Disadvantage: higher noise in the final map

• "**Robust**" (Briggs) weighting: W(u,v) depends on a given threshold value S, so that a large S gives natural weighting and a small S gives uniform weighting.



Mantage: continuous variation of the angular resolution.





 $u(k\lambda)$

- introduce weighting function W(u,v)

 $b(x,y)=FT^{-1}\{W(u,v)B(u,v)\}$

- W modifies sidelobes of dirty beam
 (W is also gridded for FFT)
- "Natural" weighting
 - $W(u,v) = I/\sigma^2(u,v)$ at points with data and zero elsewhere, where $\sigma^2(u,v)$ is the noise variance of the (u,v) sample
 - maximizes point source sensitivity (lowest rms in image)
 - generally more weight to short baselines (large spatial scales), degrades resolution



NRAO (from Summer School lecture by D.Wilner)

- "Uniform" weighting
 - W(u,v) is inversely proportional to local density of (u,v) points, so sum of weights in a (u,v) cell is a constant (or zero)
 - fills (u,v) plane more uniformly, so (outer) sidelobes are lower
 - gives more weight to long baselines and therefore higher angular resolution
 - degrades point source sensitivity (higher rms in image)
 - can be trouble with sparse sampling: cells with few data points have same weight as cells with many data points













- "Robust" (Briggs) weighting
 - variant of "uniform" that avoids giving too much weight to cell with low natural weight
 - implementations differ, e.g. S_N is natural weight of a cell, S_t is a threshold

$$W(u,v) = \frac{1}{\sqrt{1 + S_N^2 / S_{thresh}^2}}$$

- large threshold \rightarrow natural weighting
- small threshold \rightarrow uniform weighting
- an adjustable parameter that allows for continuous variation between highest angular resolution and optimal point source sensitivity



- "Tapering"
 - apodize the (u,v) sampling by a Gaussian

$$W(u,v) = exp\left\{-\frac{(u^2+v^2)}{t^2}\right\}$$

t = tapering parameter (in $k\lambda$; arcsec)

- like smoothing in the image plane (convolution by a Gaussian)
- gives more weight to short baselines, degrades angular resolution
- degrades point source sensitivity but can improve sensitivity to extended structure
- could use elliptical Gaussian, other function
- limits to usefulness















Spectral Lines in the ALMA bands

http://www.splatalogue.net

(large subset also available in OT)

ΔΙ ΜΔ 🔜



Spectral lines in the ALMA bands



SMA spectrum of Arp 220 (Band 6) (Martin et al. 2011)



ALMA Calibration Device



Two-temperature load system (100C & ambient) maneuvered by robotic arm (shown in a Melco antenna below)



 $\tau = \tau_{o} \operatorname{sec}(el)$



Atmospheric phase fluctuations

- Variations in the amount of precipitable water vapor (PWV) cause phase fluctuations, which are worse at shorter wavelengths (higher frequencies), and result in:
 - Low coherence (loss of sensitivity)
 - Radio "seeing", typically 0.1-1" at 1 mm
 - Anomalous pointing offsets
 - Anomalous delay offsets

You can observe in apparently excellent submm weather (in terms of transparency) and still have terrible "seeing" i.e. phase stability.



Patches of air with different water vapor content (and hence index of refraction) affect the incoming wave front differently.



Phase correction methods



• Fast switching: used at the EVLA for high frequencies and will be used at ALMA. Choose cycle time, t_{cyc} , short enough to reduce ϕ_{rms} to an acceptable level. Calibrate in the normal way.

	Band 9 (690 GHz)	Band 7 (345 GHz)
50 antennas, 2 pol, 8 GHz, 1 minute, yields 1-sigma sensitivity:	1.94 mJy/beam	0.18 mJy/beam
Phase measurement on one baseline: with 1 pol, 2 GHz, 1 minute at 3-sigma requires source flux density:	F > 600 mJy	F > 54 mJy

- Traditional calibrators (quasars) are more scarce at high frequency
- But ALMA sensitivity is high, even on a per baseline basis
- Key will be calibrator surveys (probably starting with ATCA survey)



Phase correction methods



- Fast switching: used at the EVLA for high frequencies and will be used at ALMA. Choose cycle time, t_{cyc}, short enough to reduce φ_{rms} to an acceptable level. Calibrate in the normal way.
- **However**, the atmosphere often varies faster than the timescale of Fast Switching. The solution for ALMA is the WVR system.
- Water Vapor Radiometry (WVR) concept: measure the rapid fluctuations in T_B^{atm} with a radiometer at each antenna, then use these measurements to derive changes in water vapor column (w) and convert these into phase corrections using:

 $\Delta \varphi_{e} \thickapprox 12.6 \ \pi \ \Delta w \ / \ \lambda$




There are 4 "channels" flanking the peak of the 183 GHz water line

- Matching data from opposite sides are averaged
- Data taken every second, and are written to the ASDM (science data file)
- The four channels allow flexibility for avoiding saturation
- Next challenges are to perfect models for relating the WVR data to the correction for the data to reduce residual phase noise prior to performing the traditional calibration steps.



Tests of ALMA WVR System 600m baseline, Band 6, Mar 2011 (red=raw data, blue=corrected) 150 100 50 Phase Average 0 -50 -100-150 06:28:48.0 06:43:12.0 06:57:36.0 07:12:00.0 07:26:24.0 Time

NRAO

Phase correction methods



- Fast switching: used at the EVLA for high frequencies and will be used at ALMA. Choose cycle time, t_{cyc}, short enough to reduce φ_{rms} to an acceptable level. Calibrate in the normal way.
- Water Vapor Radiometry: measure rapid fluctuations in T_B^{atm} with a radiometer, then use these to derive changes in water vapor column (w) and convert these into phase corrections using: $\Delta \phi_e \approx 12.6\pi \Delta w/\lambda$
- Phase transfer: alternate observations at low frequency (calibrator) and high frequency (science target), and transfer scaled phase solutions from low to high frequency. Can be tricky, requires well characterized system due to differing electronics at the frequencies of interest.
- **Self-calibration**: possible for bright sources. Need S/N per baseline of a few on short times scales (typically a few seconds).

