ngVLA MEMO #28
HOST GALAXIES AND RELATIVISTIC EJECTA OF COMPACT BINARY MERGERS IN THE ngVLA ERA
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ABSTRACT
We present the results of a community study aimed at exploring some of the scientific opportunities that the next generation Very Large Array (ngVLA) could open in the field of multi-messenger time-domain astronomy. We focus on compact binary mergers, golden astrophysical targets of ground-based gravitational wave (GW) detectors such as advanced LIGO. A decade from now, a large number of these mergers is likely to be discovered by a world-wide network of GW detectors. This will enable the identification of host galaxies, either directly through detection of electromagnetic (EM) counterparts, or indirectly by probing potential anisotropies in the spatial distribution of mergers. Identifying the host galaxy population of GW mergers would provide a way to constrain the efficiency of various binary neutron star (NS) or black hole (BH) formation scenarios, and the merger timescale distributions as linked to merger rates in early- and late-type galaxies. We discuss how a radio array with ≈ 10× the sensitivity of the current Karl G. Jansky VLA and ≈ 10× the resolution, would enable resolved radio continuum studies of binary merger hosts, probing regions of the galaxy undergoing star formation (which can be heavily obscured by dust and gas), AGN components, and mapping the offset distribution of the mergers with respect to the host galaxy light. For compact binary mergers containing at least one NS and with associated EM counterparts, we show how the ngVLA would enable direct size measurements of the relativistic merger ejecta and probe, for the first time directly, their dynamics.

I. INTRODUCTION
The results summarized in this report follow a solicitation from the National Radio Astronomy Observatory to develop community-based studies for a future U.S.-led radio telescope, the ngVLA. Building on the scientific and technical legacy of the Jansky VLA and of the Atacama Large Millimeter Array (ALMA), the ngVLA will have ≈ 10× the collecting area of the Jansky VLA, operate at frequencies from 1 GHz (30 cm) to 116 GHz (2.6 mm) with up to 20 GHz of bandwidth, possess a compact core for high surface-brightness sensitivity, and extended baselines of at least hundreds of kilometers and ultimately across the continent to provide high-resolution imaging (Bolatto et al. 2017). As underlined by Bower et al. (2015), the ngVLA could bring transformational results by enabling the exploration of the dynamic radio sky with unprecedented sensitivity and resolution. Here we discuss two new scientific opportunities that would emerge in time-domain astrophysics if a facility like the ngVLA were to work in tandem with ground-based GW detectors:
1. Unraveling the physics behind the progenitors of BH-BH, NS-NS, and BH-NS mergers via host galaxy studies at radio wavelengths;
2. Enabling direct size measurements (and thus direct dynamics constraints) of relativistic ejecta from NS-NS and/or BH-NS mergers (with ngVLA plus VLBI stations).
In what follows, we briefly describe the scientific landscape expected to be realized when the ngVLA may become operational (Sec. 2). Then, we discuss radio studies of host galaxies of binary mergers (Sec. 3), and of relativistic ejecta (Sec. 4). Finally, in Sec. 5 we summarize and conclude.
We note that while this report was being submitted, the first NS-NS merger was discovered by the advanced LIGO and Virgo detectors, and found to be associated with an EM counterpart detected at all wavelengths (e.g., Abbott et al. 2017 [6]; and references therein). We have thus updated our discussion to briefly refer to GW170817 where relevant in the context of this study.

2. THE POST-2027 SCIENTIFIC LANDSCAPE
Our discussion of compact binary mergers and their relativistic ejecta in the ngVLA era is framed within the scientific landscape of a decade or more in the future. In light of the recent BBH detections by the advanced Laser Interferometer Gravitational-wave

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7 https://science.nrao.edu/facilities/vla
8 http://www.almaobservatory.org/en/home/
Fig. 1.— Figure adapted from the ngVLA project summary presentation by E. Murphy. See https://science.nrao.edu/futures/ngvla/documents-publications. The vertical dotted lines mark the frequencies relevant for this study. At these frequencies, the ngVLA collecting area is superior to that of SKA1 and ALMA.

Our understanding of the transient sky will also have been informed and shaped by the findings of several (upcoming or planned) synoptic optical surveys, such as e.g., the Zwicky Transient Facility (ZTF) and the Large Synoptic Survey Telescope (LSST). Particularly, when starting full operations in circa 2023 and for the following 10 years, the LSST will discover tens of thousands of astrophysical transients every night down to a limiting magnitude of $r \approx 24.7$ mag (LSST Science Collaboration et al. 2009). Thus, by the time the ngVLA will start operations, we expect to have a better census of the optical transient sky, including statistically significant samples ($\gtrsim 10$ objects) of rare and faint transients. Among other major EM facilities likely to be contributing observations at various wavelengths in the ngVLA era are ALMA, which will be observing in the mm, the Square Kilometer Array (SKA; e.g., DeBoer et al. 2009), and the Wide Field Infrared Survey Telescope (WFIRST) operating in the NIR-IR. The James Web Space Telescope (JWST) could also still (after its nominal mission duration) be providing sub-arcsecond resolution and unprecedented sensitivity from long-wavelength visible light to near/mid-infrared.

We stress that the ngVLA sensitivity (and resolution) will be optimal for the science topics described in this memo when compared to other radio facilities that we expect to be operational in the ngVLA era. Particularly, as shown in Fig. 1, we focus here on two topics that make use of the superior ngVLA (+VLBA) sensitivity and resolution at frequency ranges in between those for SKA1-MID ($\nu \lesssim 1$ GHz) and ALMA ($\nu \gtrsim 100$ GHz) will be the premier radio facilities.

As current EM follow-up efforts are demonstrating, spectroscopic and multi-wavelength observations of the zoo of optical transients populating the GW localization areas, and of their host galaxies, are going to be key to identifying and removing false positives, as well as breaking degeneracies in the physics behind potential EM counterparts (e.g., Abbott et al. 2016b; Bhalerao et al. 2016; Connaughton et al. 2016; Copperwheat et al. 2016; Cowperthwaite et al. 2016; Evans et al. 2016; Kasliwal et al. 2016).
RESOLVING THE HOST GALAXIES OF COMPACT BINARY MERGERS

GW observations of compact object binaries (NS-NS, BH-NS, or BH-BH) can constrain the properties of the compact object themselves, such as masses, spins, and merger rates. However, understanding their progenitors and formation channels (i.e., how do compact binary systems actually form and evolve) requires the identification of host galaxies, and more generally a detailed study of the merger environment.

A first constraint on the progenitors of compact binary mergers and their age distribution would be provided by the demographics of their host galaxies, since the distribution of merger timescales impacts the mix of early- and late-type hosts. Generally speaking, the smaller the merger delay, the stronger the connection with (recent) star formation (SF) rather than with stellar mass alone, and the larger the late-type fraction (e.g., Zheng & Ramirez-Ruiz 2007). A young cluster origin would also connect to late-type galaxies (e.g., O’Leary et al. 2007), while a globular cluster origin (e.g., Rodriguez et al. 2016) would connect to early-type galaxies. In the case of BH-BH mergers, a connection with AGN, which has been suggested in the context of formation via dynamical interactions, could also be tested via host studies (e.g., Bartos et al. 2017). Moreover, the dependence of the BH-BH merger efficiency on the metallicity may favor dwarf (low-metallicity) hosts and/or merging galaxies with bursts of SF at low metallicity in their assembly history. Overall, a detailed understanding of the galaxy “response function” for compact binaries (how often star forming gas of a given metallicity evolves into merging compact binaries) is likely to ultimately require broad-band datasets and the help of stellar population synthesis techniques (O’Shaughnessy et al. 2017).

Radio observations could contribute significantly to the above studies. Radio can probe the presence of AGNs in the hosts, and could thus help test the proposed formation scenario that connects (heavy) BH-BH mergers to dynamical interactions in dense stellar systems (including globular clusters and AGN, e.g., Bartos et al. 2017). More generally, radio continuum emission from galaxies traces the SF rate (SFR) during the last ~ 50 – 100 Myr (e.g., Murphy et al. 2011), and could thus help track the connection between mergers and recent SFR rate. In fact, due to the age-dust-metallicity degeneracy, the optical/UV emission alone is an unreliable measure of SFR in dusty galaxies. While the FIR is also an extinction free SFR tracer, and could provide more accurate estimates of SFR when combined with optical data, the ease with which SFRs can be measured is also to be taken into account. In this respect, ground-based extinction-free radio observations are advantageous compared to satellite-based FIR observations.

In addition to the host galaxy SFR (and type) as linked to the merger delay distribution, the study of sub-galactic environments (achievable via resolved multi-wavelength studies of the host galaxies) can be used to gain other clues to the progenitors of compact binary mergers. Resolved host galaxy studies of binary mergers with EM counterparts (and thus with accurate localizations) would first of all remove confusion between potential EM counterparts (especially those slowly-evolving radio transients predicted by some models of NS-NS merger ejecta, see e.g., Hotokezaka et al. 2016) and light from the host galaxy. Resolved studies would also allow us to assess the presence or absence of a spatial association with star formation or stellar mass, and potentially track an overall globular cluster distribution for a dominant population of dynamically formed binaries. Finally, the distribution of offsets between the birth and explosion sites, as determined by natal kicks, will be reflected in the fraction of “hostless” mergers (those whose projected locations will extend much beyond the visible extent of typical galaxies) and in the measured distribution of offsets of EM counterparts with respect to their host galaxy light (e.g., Belczynski et al. 2006; Behroozi et al. 2014 and references therein).

3.1. The short GRB host galaxy sample

To understand the role that ngVLA observations can play in the host galaxy study of compact binary mergers, here we consider the example of short GRBs. Because short GRBs are likely associated with cosmological mergers of compact binaries containing at least one NS and/or stellar-mass BHs, their host galaxies form a good sample to draw from in the context of compact binary mergers detectable by ground-based GW detectors.

First, we note that radio observations of the host galaxies of GRB 071227 and GRB 120804A provided clear evidence for SFRs at least an order of magnitude larger than those derived using optical data alone (Fig. 1; Guelbenzu et al. 2014), suggesting either a starburst origin or an AGN contribution. For instance, for the host of GRB 071227, Guelbenzu et al. (2014) find a SFR of $\approx 24 M_{\odot}/yr$ (Fig. 1), much in excess to the SFR of $\approx 0.6 M_{\odot}/yr$ estimated from the optical data alone (see Table 1). This supports our expectation that optical data alone, due to the age-dust-metallicity degeneracy, cannot reliably determine the host SFR for binary mergers detectable by ground-based GW detectors. The host galaxy NGC4993 of the recently detected binary NS merger
GW170817, associated with the short GRB 170817A, shows a radio SFR of \( \approx 0.1 \, M_\odot/\text{yr} \), approximately 10 times higher than the one estimated using the galaxy broad-band photometry, indicative of an AGN dominating the radio emission (Blanchard et al. 2017).

While currently most of the cosmological short GRB host galaxies remain undetected in the radio, a sensitive array like the ngVLA will be able to resolve short GRB-like hosts within the LIGO horizon distance. To show this, in Table 1 we collected the (optical/UV) SFR and optical sizes of short GRB hosts available in the literature. We use the measured SFR to calculate the expected host galaxy luminosity at 1.4 GHz via the Murphy et al. (2011) SFR-to-non-thermal radio emission calibration relation:

\[
\left( \frac{\text{SFR}_{1.4\,\text{GHz}}}{M_\odot/\text{yr}} \right) = 6.35 \times 10^{-29} \left( \frac{L_{1.4\,\text{GHz}}}{\text{erg s}^{-1}\text{Hz}^{-1}} \right).
\]

To estimate the corresponding luminosity at the lowest ngVLA frequency of \( \approx 3 \, \text{GHz} \), we extrapolate from the 1.4 GHz luminosity using a spectral index of \( \approx -0.75 \) (as appropriate for non-thermal galaxy emission). The results are reported in Table 1, together with the corresponding expected radio flux densities at \( z = 0.1 \) (the advanced LIGO horizon distance). We then use the effective galaxy radius \( r_e \) from optical/IR observations as FWHM size of the galaxy at radio wavelengths. This is justified by the fact that radio emission from local galaxies is typically observed to be more concentrated than in the optical. Specifically, using the Condon et al. (2002) sample, we estimate an average ratio of \( \approx 0.5 \) between the FWHM of the radio galaxies in the NVSS catalog (FWHM \( \approx 45'' \)) and the size of their blue diameter. The smaller concentration of the radio emission in star forming galaxies has also been confirmed in the GOODS-N Jansky VLA sample by comparing effective radii of the 10 GHz emission with effective radii derived from HST/WFC3 observations (Murphy et al. 2017). With the expected radio flux and expected radio size in hand, we thus calculate the expected brightness temperature as:

\[
T = 0.32 \times 10^{23} \frac{\lambda^2}{\theta^2} S,
\]

where \( \lambda \) is the observed wavelength, \( \theta \) is the FWHM radio size, and \( S \) is the flux density at the considered wavelength (\( \lambda \approx 10 \, \text{cm} \) for observations at 3 GHz). Our results are reported in the last column of Table 1, and also plotted in Fig. 2. The ngVLA will reach a surface brightness sensitivity of \( \approx 0.0823 \, \text{K} \) (\( \approx 0.18 \, \text{K} \)) in 1 hr with \( \approx 1'' \) (\( \approx 0.1'' \)) resolution at 3 GHz, thus resolving most of these hosts at \( z \lesssim 0.1 \). We stress that the current VLA in its A configuration, would offer a comparable resolution of \( \approx 1'' \) at 3 GHz, but with a worse surface brightness sensitivity in 1 hr of \( \approx 0.6 \, \text{K} \). Only two of the host galaxies in Table 1 have a brightness temperature larger than \( \approx 3 \times 0.6 \, \text{K} = 1.8 \, \text{K} \), thus resolved studies of most short GRB-like host galaxies within the advanced LIGO horizon would be inaccessible to the Jansky VLA (for reasonable integration times, see the blue horizontal line in Fig. 2) and require a more sensitive array like the ngVLA.
TABLE 1

<table>
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<th>GRB</th>
<th>z</th>
<th>SFR</th>
<th>( r_{cz} )</th>
<th>( r_e )</th>
<th>FWHM (_{2.5%} )</th>
<th>( L_{3\text{GHz}} )</th>
<th>( F_{3\text{GHz}} )</th>
<th>( T )</th>
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<td>0.65</td>
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<tr>
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<td>15</td>
<td>1.0</td>
</tr>
<tr>
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</tr>
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</tr>
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<td>1.7</td>
<td>1.5 \times 10^{10}</td>
<td>59</td>
<td>2.8</td>
</tr>
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</table>

Fig. 3.— Predictions for the radio brightness temperature of NS-Ns and BH-NS binary merger host galaxies located with the advanced LIGO horizon distance \((z \leq 0.1)\). These predictions are based on our current knowledge of short GRB hosts (see Table 1). The ngVLA will reach a surface brightness sensitivity of \(\approx 0.0823 \text{ K} \) in 1 hr with \(= 1''\) resolution at 3 GHz, thus resolving most of these hosts at \(z \leq 0.1\) (red dotted line). We note that resolved studies of most short GRB-like host galaxies within the advanced LIGO horizon are inaccessible to the Jansky VLA for reasonable integration times (blue dashed line).

NS-NS and BH-NS mergers are thought to produce, in addition to GW in-spiral signals, EM (and, specifically, synchrotron radio) emission associated with outflows with significant kinetic energies. This prediction has been proven accurate by GW170817, a NS-NS merger associated with emission of EM radiation at all wavelengths (e.g. Abbott et al. 2017; Evans et al. 2017; Hallinan et al. 2017; Kasliwal et al. 2017; Troja et al. 2017; Valenti et al. 2017 and references therein). In what follows, we show that the ngVLA with its superior sensitivity could probe, for the first time directly, the early-time dynamics of relativistic ejecta from NS-NS and BH-NS mergers located within the distance horizon of ground-based GW detectors. Resolving the radio remnant of a relativistic ejecta requires VLBI techniques. So far, given the large cosmological distances of most GRBs detected via purely EM observations, this has been attempted only for the brightest long GRBs (\(\gamma\)-ray transients associated with massive star collapse), and limited to long timescales after the explosion (so as to give time to the ejecta to expand). Direct imaging of the relativistically ejecta associated with BH-NS or NS-NS producing short GRBs, which generally have lower luminosities and dimmer radio afterglows compared to long GRBs, has not been within the reach of current radio arrays, and represents the only direct way to map the speed distribution of merger ejecta and test the predictions of dynamic ejecta models.

Broadly speaking, three major classes of radio counterparts are thought to exist (e.g., Hotokezaka et al. 2016; Lazzati et al. 2017): (i) counterparts associated with sub-relativistic merger ejecta producing radio remnants on timescales of a few years; (ii) ultra-relativistic jets that produce short GRBs and (on-axis) radio afterglows in the direction of the jet (evolving on timescales of a few days), and/or orphan-radio afterglows extending over wider angles (evolving on timescales of weeks); (iii) mildly-relativistic “cocoons” whose emission may be more isotropic and whose brightness would depend on the amount of energy imparted to it by the jet. Here, we consider scenario (ii) and focus on the case in which the observer is located on-axis with an ultra-relativistic jet launched during the merger. Other emission processes and geometries may be possible, but this example gives a good order of magnitude estimate of what is possible with the VLBI capabilities of ngVLA. In this case, detailed calculations for the predicted surface brightness of the radio counterpart exist (e.g. Granot et al. 1999). According to these predictions, the image of a short
Fig. 4.— Left: Figure adapted from Granot et al. (1999). We show the expected image of a GRB afterglow for $\phi = 10$ where $\nu_m$ is the time-evolving characteristic synchrotron frequency of electrons located just behind the shock front on the line of sight (see text). This image has been created by smoothing the corresponding $\phi = 10$ image presented in Granot et al. (1999). Larger values of $\phi$ represent a higher observing frequency or a later observing time (since $\nu_m \propto t^{-3/2}$). The image is brighter near the edge and dimmer near the center, and the contrast is higher at larger values of $\phi$. Right: Simulation of a 2.3 hr-long ngVLA observation of the radio remnant of a relativistic ejecta from a BH-NS/NS-NS merger at $d_L \approx 150 \text{Mpc}$, with realistic parameter values of $E_{\text{iso}} \approx 1.7 \times 10^{50} \text{erg}$, $\epsilon_e = 0.1$, $\epsilon_B = 0.01$, $n = 0.01 \text{cm}^{-3}$. We have used the model image shown in the left panel, assumed an ngVLA configuration as shown in Fig. 5 (left panel) with the addition of VLBI stations, and added noise level compatible with current estimates of expected ngVLA performance at 30 GHz (see Fig. 5, right panel).

GRB afterglow would to be ring-like: brighter near the edge and dimmer near the center, with the contrast between the edge and the center of the image increasing (and the width of the ring decreasing) at higher frequencies for a given observing time (see Fig. 4, left, and Granot et al. 1999).

Following Granot et al. (1999), we write the characteristic synchrotron frequency of electrons located just behind the relativistic shock on the line of sight as:

$$\nu_m \approx 1.3 \times 10^9 \text{Hz} \sqrt{1+z} \left(\frac{\epsilon_B}{0.01}\right)^{1/2} \left(\frac{\epsilon_e}{0.1}\right)^2 \left(\frac{E_{\text{iso}}}{3 \times 10^{50} \text{erg}}\right)^{1/2} \left(\frac{t}{7 \text{d}}\right)^{-3/2},$$

where $\epsilon_e$ and $\epsilon_B$ denote the fraction of energy going into accelerating relativistic electrons and amplifying magnetic fields (with typical values of $\epsilon_e \approx 0.1$ and $\epsilon_B \approx 0.01$), and $E_{\text{iso}}$ is the isotropic-equivalent kinetic energy of the ejecta. We note that $E_{\text{iso}} \approx 1.7 \times 10^{50} \text{erg}$ corresponds to a true jet energy of $E_j \approx 2 \times 10^{49}(\theta_j/30 \text{deg})^2 \text{erg}$, where $\theta_j$ is the jet half-opening angle. The synchrotron emission spectrum peaks at a frequency which, for a typical value of the power-law index of the electron energy
distribution of \( p \approx 2.5 \), is \( \approx 1.88 \times \nu_m \) (Granot et al. 1999):

\[
y_p \approx 2.4 \times 10^9 \text{Hz} \sqrt{1 + z} \left( \frac{\epsilon_8}{0.01} \right)^{1/2} \left( \frac{\epsilon_9}{0.1} \right)^{3/2} \left( \frac{E_{\text{iso}}}{1.7 \times 10^{50} \text{erg}} \right)^{1/8} \left( \frac{t}{7 \text{d}} \right)^{-3/2}.
\]

(4)

For a merger ejecta located within the advanced LIGO horizon distance \( (z \leq 0.1) \), we can approximate the total flux received by an on-axis observer at \( \nu \approx 30 \text{GHz} \) and \( t \approx 7 \text{d} \) as:

\[
F_{\nu} \approx 0.33 \text{mJy} \left( 1 + z \right)^{11/8} \left( \frac{\epsilon_8}{0.01} \right)^{7/8} \left( \frac{\epsilon_9}{0.1} \right)^{3/2} \left( \frac{E_{\text{iso}}}{1.7 \times 10^{50} \text{erg}} \right)^{11/8} \left( \frac{n}{0.01} \right)^{1/2} \left( \frac{d_1}{150 \text{Mpc}} \right)^{-2} \left( \frac{\nu}{30 \text{GHz}} \right)^{-3/4} \left( \frac{t}{7 \text{d}} \right)^{-9/8},
\]

(5)

where \( n \) denotes the density of the ISM in units of \( \text{cm}^{-3} \). The above flux is distributed as shown in Figure 3 (left panel), with an observed outer radius of the ring equal to Granot et al. (1999):

\[
R_{\text{max}} \approx 1.4 \times 10^{17} \text{cm} \left( \frac{E_{\text{iso}}}{1.7 \times 10^{50} \text{erg}} \right)^{1/8} \left( \frac{n}{0.01} \right)^{-1/8} \left( \frac{t}{(1 + z)7 \text{d}} \right)^{5/8}.
\]

(6)

Thus, for a source located at 150 Mpc, the outer angular diameter of the relativistic ejecta image can be estimated as:

\[
D_{\text{max},150 \text{Mpc}} \approx 0.13 \text{mas} \left( \frac{E_{\text{iso}}}{1.7 \times 10^{50} \text{erg}} \right)^{1/8} \left( \frac{n}{0.01} \right)^{-1/8} \left( \frac{t}{7 \text{d}} \right)^{5/8}.
\]

(7)

We note that the above expressions for the radio frequencies, fluxes, and size of the radio remnant are valid for all time \( t \leq t_j \) where:

\[
t_j \approx 26 \text{d} \left( 1 + z \right) \left( \frac{E_j}{1.7 \times 10^{50} \text{erg}} \right)^{1/3} \left( \frac{n}{0.01} \right)^{-1/3} \left( \frac{\theta_j}{30 \text{deg}} \right)^2.
\]

(8)

In Figure 4, right panel, we show a simulation of a 2.3 hr-long ngVLA observation of the radio remnant of a relativistic ejecta from a BH-NS/NS-NS merger at \( d_1 \approx 150 \text{Mpc} \), with realistic parameter values of \( E_{\text{iso}} \approx 1.7 \times 10^{50} \text{erg}, \epsilon_9 = 0.1, \epsilon_8 = 0.01, n = 0.01 \text{cm}^{-3} \). We have used the model image shown in the left panel of Fig. 4, assumed an ngVLA configuration as shown in Fig. 5 (left panel) with the addition of VLBI stations with baselines up to \( \approx 3500 \text{km} \), and added noise level compatible with current estimates of expected ngVLA performance at 30 GHz (see Fig. 5, right panel). As evident from this Fig. 4 (right panel), with the ngVLA we will be able to measure sizes as small as \( \approx 11 \text{mas} \) at flux levels of order \( \approx 0.33 \text{mJy} \). We can compare this result with previous VLBI size measurements performed on the radio afterglows of long duration GRBs. Particularly, Taylor et al. (2004) reached similar size constraints in comparably long observations of GRB 030329 \( (z \approx 0.17) \) with VLBA plus other stations. However, GRB 030329 had fluxes \( \gtrsim 3 \text{mJy} \) in the \( 8 - 22 \text{GHz} \) range at the times at which these size constraints were obtained. Thus, our simulation shows that the ngVLA would enable size measurements comparable to those that have been achieved in the past for long GRBs (which are associated to the deaths of massive stars) using the VLA plus VLBI stations (with similar integration times), but for radio remnants \( \approx 10 \times \text{dimmer} \), which is key for probing NS-NS and BH-NS mergers - the golden multi-messenger sources whose radio size measurements have thus far remained outside the reach of current radio arrays.

5. SUMMARY AND CONCLUSION

We have investigated two new scientific opportunities that would emerge in time-domain astrophysics if a facility like the ngVLA were to work in tandem with ground-based GW detectors:

1. Unraveling the physics behind the progenitors of BH-BH, NS-NS, and BH-NS mergers via host galaxy studies at radio wavelengths;

2. Enabling direct size measurements (and thus direct dynamics constraints) of relativistic ejecta from NS-NS and/or BH-NS mergers (with ngVLA plus VLBI stations).

We have shown that:

1. The ngVLA, thanks to its improved surface brightness sensitivity at lower frequencies, can enable resolved studies of NS-NS and/or BH-NS mergers host galaxies within the advanced LIGO horizon distance. Based on current knowledge drawn from the short GRB host galaxy sample, these galaxies would otherwise remain largely inaccessible to the Jansky VLA (for realistic integration times).

2. The ngVLA+VLBI, thanks to its superior high frequency \( (\nu \approx 30 \text{GHz}) \) sensitivity at the longest baselines, can enable direct size measurements of relativistic ejecta from NS-NS and/or BH-NS mergers to a level \( (\approx 0.1 \text{mas}) \) comparable to what has been achieved in the past for long GRBs (using the VLA plus VLBI stations with similar integration times) but for radio remnants \( \approx 10 \times \text{dimmer} \), which is key for probing directly the currently unexplored dynamics of relativistic ejecta from binary NS of BH-NS mergers.

We finally stress that having the ngVLA be operated as a PI-driven array capable of fast response to GW triggers is fundamental to enabling the scientific results described in this memo.
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