Student Lecture Notes - 1972

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CONTENTS

11.1 INTRODUCTION

11.1.1 Hydrogen Distribution and Kinematics

Hydrogen is the building material for stars and galaxies and a study of its distribution and kinematics in external galaxies is essential to understanding the dynamics and evolution of these objects. Much can be learned by comparing the overall or integral properties of different galaxies, but an understanding of the detailed distribution of neutral hydrogen in a galaxy can only be derived from a high resolution map.

The Magellanic Clouds were the first extragalactic objects observed in the λ21 cm line (Kerr, Hindman and Robinson, 1954). The large angular extent of these objects enabled a detailed map to be made of the neutral hydrogen density and velocity distribution across the Clouds. The aim of observations today is to make similarly detailed maps for ordinary spiral and irregular galaxies.

The story of mapping neutral hydrogen in external galaxies is one of a continuing quest for angular resolution, but we will first briefly review the classification and properties of the galaxies we will be talking about.

11.1.2 Classification Systems

Normal galaxies have been classified under several schemes. The Hubble (Sandage, 1961) classification, based on the morphological features visible on blue-sensitive plates, is perhaps the most widely used. This scheme, which divides spiral galaxies into three classes: Sa, Sb, Sc, depending on the openness of the spiral features, has been extended by Holmberg (1958)

and by de Vaucouleurs (1964), and has much to recommend it, in that it would seem to represent a real separation in terms of the evolutionary parameters (e.g. fractional hydrogen content) of the galaxies. This is not to say that the series is an evolutionary sequence. Indeed, unless there can be considerable accretion of mass by a galaxy it would appear impossible for evolution to take place along the series from the irregular and Sc galaxies (which, on average have the highest fractional hydrogen content) to the more massive Sa spirals and ellipticals.

Equivalent classifications under these morphological systems are set out in the introduction to de Vaucouleurs' (1964) Reference Catalogue of Bright Galaxies.

The Morgan (Yerkes) (1958, 1959) classification is a valuable complementary alternative to the Hubble classification. In this system the parameter a-k denotes increasing central concentration of light whilst the luminosity is progressively from A to K type stars (Morgan and Mayall 1957). Although the early type (Sa) spirals tend to have a higher degree of central condensation and the Hubble type correlates well with the integrated colour of galaxies (Holmberg 1958), there is not a one-to-one correspondence between the Hubble and Morgan classifications. A further classification system for late type spirals (Sc and Sb) is that of Van den Bergh (1960a, b), based on a strong correlation between the absolute luminosity and the degree of development of the spiral arms.

These classification systems are interrelated, but not exactly equivalent and each is useful in discussing the properties of spiral galaxies.

11.2 INTEGRAL PROPERTIES OF GALAXIES

The overall characteristics of a galaxy are determined by its, so-called, "integral properties," which include: the morphological form under some classification system, colour, total mass, luminosity, hydrogen mass, HII region abundance, radio continuum power, etc. By studying the correlations among these parameters we hope to learn something of the evolution of galaxies and the reasons for their different morphological forms.

Surveys of external galaxies in the λ21 cm line have been made by a number of authors and there are several excellent reviews of the integral properties of galaxies (e.g. Roberts 1969, 1967). We will merely note here some of the established trends of the integral properties.

11.2.1 The Data

a) Hydrogen Mass

The mass of neutral hydrogen in a galaxy is derived from its λ21 cm emission spectrum. The surface density (atom cm^{-2}) of hydrogen radiating in a 1 km sec^{-1} interval is given by

$$n_v = 1.823 \times 10^{18} T_s \tau_v \qquad 11.1$$

where T_s is the spin temperature of the gas and τ_v the optical depth (see for example the article by Kerr in Stars and Stellar Systems, Vol. 7). T_s is assumed, here, to be constant along the column of radiating gas. If the gas is optically thin ($T_B << T_s$) then the surface density is given by:

$$n = 1.823 \times 10^{18} \int_{\text{velocity}} T_B \, dV \qquad 11.2$$

and the total number of atoms N, is obtained by integrating the surface density across the galaxy:

$$N = 1.823 \times 10^{18} \int_{\text{galaxy}} dS \int_{\text{velocity}} T_B \, dV \qquad 11.3$$

An element of surface area dS, is related to the distance D by $dS = D^2 d\Omega$. Thus the number of atoms is proportional to D^2 and the integrated line flux is given by

$$N = 1.823 \times 10^{18} D^2 \iint T_B \, dV \, d\Omega, \qquad 11.4$$

or in convenient units:

$$M/M_\odot = 2.356 \times 10^5 D^2 \int S_v \, dV; \qquad 11.5$$

where D is in Mpc, S_v in flux units* and dV in km sec^{-1}.

The assumption of small optical depth may be invalid particularly where the velocity dispersion of the gas is small or the line of sight thickness is large due to high inclination of the galaxy. In this case the mass of neutral hydrogen derived above is a lower limit. Also, the variation of T_s (known to occur in our Galaxy) make the mass a lower limit from another point of view, as some of the hydrogen will be in cold clouds of substantial opacity. It is tacitly assumed that there is no interaction between radio continuum and line radiation. Epstein (1964) has considered this problem for different cases.

b) Total Masses

The masses of spiral galaxies are estimated by assuming that the galaxies are in rotational equilibrium.

The line-of-sight velocity of some component of the galaxy, usually neutral hydrogen or ionized hydrogen, oxygen and nitrogen, can be measured

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* 1 flux unit = 10^{-26} W m^{-2} Hz^{-1}.

by the Doppler shift of its corresponding line emission. In the case of irregular galaxies (or for low resolution neutral hydrogen measurements) the mass of the galaxy can be estimated (e.g. Bottinelli et al. 1968) directly from the measured velocity disperison using the virial theorem (Chandrasekhar, 1942). More usually, for spiral galaxies, a rotation velocity is estimated as a function of radius and a mass derived from a model for the centrifugal equilibrium of the gas. The basic equation in either case is of the form $GM/R = 2V^2$ and the estimated mass scales linearly with assumed distance to the galaxy. As discussed in more detail in section 5 and 6 the neutral hydrogen data usually have poor angular resolution and the total mass must be derived from a model for the rotation curve whilst the optical data have high angular resolution and provide a detailed mass distribution, but only out to the limiting radius of the emission lines (e.g. Burbidge, Burbidge and Prendergast 1963). There is some difficulty, then, in comparing masses derived from optical and radio data.

c) Luminosity

The measured luminosity of a galaxy increases with the area of the photographic image integrated. The Holmberg (1958) system of luminosities and diameters of galaxies provides a well defined measurement down to a sky brightness limited isophote of $26^m.5$ per square sec arc. The measured luminosities and colours on the UBV system can be corrected for an average galactic extinction by -0.25 cosec(latitude) and for inclination of the observed galaxy. The absolute luminosity of a galaxy is usually quoted in units of the solar luminosity and of course scales as the square of the assumed distance.

d) Selection Effects

Observational requirements force a selection of galaxies which may affect the correlations described below. The neutral hydrogen measurements are biased towards the late type (Sc and Irr) galaxies and optical measurements of rotation curves tend to be of intrinsically bright galaxies. Neutral hydrogen has been reported (Robinson and Koehler 1965) in only one elliptical galaxy, NGC 4472, and we will confine ourselves in what follows to the spirals and irregulars.

11.2.2 Correlations

a) Mass-Luminosity

The masses and luminosities of spiral and irregular galaxies cover about four orders of magnitude and a plot of mass against luminosity (e.g., Roberts 1969) shows that the brighter galaxies are more massive. The mass-to-light ratio is approximately constant with one order of magnitude dispersion ($M/L \tilde{\sim} 4$ solar units $M_\odot/L_\odot$). There is no separation according to structural type in the mass-luminosity diagram, except in the case of the irregulars, which tend to be low mass, intrinsically faint systems. Without the irregulars the relationship between mass, luminosity and morphological type is not obvious.

b) Hydrogen Mass-Luminosity

The distance to an external galaxy is generally ill determined and distance independent parameters are of great value in establishing correlations between the integral properties of galaxies. The neutral hydrogen to luminosity ratio, M_H/L, is such a parameter and tends to be higher in the bluer, later type galaxies (e.g., Epstein 1964). The neutral hydrogen content is itself correlated with the luminosity and these two correlations probably signify

that star formation is proceeding rapidly in galaxies containing more hydrogen.

c) Fractional Hydrogen Content

A plot of neutral hydrogen mass versus total mass (e.g., Roberts 1969) again shows a correlation, but one which is highly dependent on the presence of the low mass irregular systems. There is a clear relationship between the fractional hydrogen content and the structural type. The HI content ranges from 1-2% hydrogen in the Sa spirals to over 30% in the irregular systems. This is the most striking relationship in the integral properties of galaxies and probably indicates that the early type spirals are more evolved than the late type spirals and irregulars.

d) Ionized Hydrogen

Except for the nearest galaxies, ionized hydrogen has only been discussed in terms of large HII regions. Sersic (1960) has made a survey of HII regions in 66 galaxies and finds that the mean size of the three largest HII regions increases progressively with neutral hydrogen content from the earlier types to the Sc^- galaxies and then decreases again in the dwarf Sc and irregulars. Hodge (1967) has catalogued the positions of HII regions in 66 galaxies and finds in an analysis of 25 of these (Hodge 1969) that the distribution of HII regions within a galaxy tends to be a function of the morphological type, possibly indicating a difference in the state, or rate of evolution, of the galaxies.

e) Radio Continuum

Normal spiral galaxies are sources of non-thermal radio continuum with flux densities of typically 0.1 to 1 flux units, at 408 MHz. The optical and radio luminosities of spiral galaxies are closely correlated and recent data

(Cameron 1971) has shown that this correlation is even stronger for the restricted set of galaxies of Morgan type f. The radio continuum power is better correlated with the van den Bergh and Morgan classifications than with the Hubble type. The correlation with the van den Bergh classification and hence with spiral arm development is particularly interesting in the light of recent maps of spiral galaxies (e.g., M31, Pooley 1969 and M51, Mathewson, et al. 1972) showing that spiral arms are sources of radio continuum emission.

11.3 MAPPING HI IN GALAXIES

11.3.1 Density Distribution

a) Extent of Distribution

The integral properties of galaxies have revealed several interesting correlations of total mass and hydrogen abundance with morphological type, but have not answered the question as to why the different morphological types exist. We can only hope to gain insight into this, and the question of evolution and star formation in galaxies, if we know more details of the structure and distribution of the different components of a galaxy. Particularly lacking in this respect is a detailed knowledge of the distribution of the neutral hydrogen, the most basic component of a galaxy. The mapping of neutral hydrogen in external galaxies allows us to find such things as:

i. The overall form of the HI distribution, how this compares with that of the total mass distribution and where the highest hydrogen concentrations are.

ii. The extent of the hydrogen distribution. Is it coextensive with the luminous population of a galaxy? How sharp are its boundaries?

iii. Neutral hydrogen wings, bridges between galaxies and companions or satellites with the same sort of relationship as the Magellanic Clouds are believed to have to the Milky Way.

b) Spiral Arms

The above questions can be answered with fairly limited resolution. With higher resolution we may comment further on whether the neutral hydrogen has the form of spiral arms and if these are coincident with the spiral arms defined by the bright HII regions or displaced from them.

A detailed correlation can be made of the surface densities of the young O and B stars, the HII regions they excite and the neutral hydrogen from which they have been formed. This is a very important field, for in our Galaxy the situation is confused by the complex velocity-distance relationship. In an external galaxy one has an over-all view of the distribution of the different components.

11.3.2 Velocity Distribution

a) Line-of-Sight Velocity

Observations of neutral hydrogen are usually made with a multi-channel spectrometer so that the frequency or velocity distribution of the line radiation is also determined. Neutral hydrogen line radiation arises from a forbidden transition, and the low transition probability implies a small natural width of the line (5×10^{-16} Hz). The observed width of the line is therefore due to Doppler broadening (-4.74 kHz per km sec^{-1}) at the line rest frequency of 1420.4 MHz.

The line broadening is partly due to random and thermal motions in the gas, but is mainly due to larger scale motions of the gas. In a spiral galaxy the dominant motion is one of rotation, although expansion motions and other "peculiar" velocities are of great interest. The line-of-sight velocity of the neutral hydrogen in any portion of the galaxy can be measured as a Doppler shift and with sufficient angular and frequency resolution we observe different Doppler shifts across the face of the galaxy. The line-of-sight velocity is interpreted in terms of the rotation, expansion, and other velocities in the galaxy, which is assumed to have a plane rotating disk geometry.

b) Isovelocity Contours

The observed line-of-sight velocity, $u(r, \phi)$ of hydrogen with azimuthal coordinates (r, ϕ) in a plane galaxy inclined at an angle i to the plane of the sky, is given by:

$$u(r, \phi) = v_o + v(r, \phi) \sin i \cos \phi + w(r, \phi) \sin i \sin \phi + z(r, \phi) \cos i \quad 11.6$$

where v_o is the systemic velocity, $v(r, \phi)$ the tangential velocity (including both the rotation of the galaxy and "peculiar" streaming and random components), $w(r, \phi)$ a radial velocity in the plane of the galaxy and $z(r, \phi)$ a velocity out of the plane of the galaxy. A complete analysis of the kinematics of a galaxy should include all these effects. If the motion of the hydrogen in a galaxy is one of pure rotation then the lines of constant observed radial velocity will be the lines:

$$v(r) \cos \phi = \text{constant} \quad 11.7$$

A plot of $v(r)$ against radius r is called the rotation curve for the galaxy and typically has the form shown in Figure 1. For a rotation curve of this form, the lines of constant observed velocity (the isovelocity contours) will have the form shown in Figure 2. Where the rotation is solid body, i.e., $v(r) \alpha r$, the isovelocity contours are parallel to the minor axis of the galaxy. The region of solid body rotation is shown enclosed by the dashed line in Figure 2. Other systematic motions of the galaxy have characteristic isovelocity contours, for example, the addition of an expansion, $w(r) \alpha r$, gives isovelocity contours in the solid body region inclined at an angle to the minor axis. Closed isovelocity contours are produced by the region of the rotation curve where the rotation velocity is decreasing with radius.

c) Interpretation

From the velocity information we can investigate:

i. Rotation of the galaxy and the shape of the rotation curve,

ii. The total mass and a mass distribution for the galaxy,

iii. Angular momentum distribution,

iv. Velocity dispersion of the gas and hence an estimate of the thickness of the neutral hydrogen layer,

v. Peculiar velocities, expansion motions,

vi. Perturbations due to spiral arms, streaming motions, and density waves.

The above list has been compiled in order of increasing observational difficulty. Observation of the spiral arms and their perturbations requires the highest resolution and sensitivity and is the subject of current research.

The highest physical resolution so far obtained has been the observations of the Magellanic Clouds with the 210-foot Parkes dish where the half power beamwidth is equivalent to about 200 pc at the distance of the clouds. In order to obtain comparable resolution in the nearest spiral galaxies, an angular resolution of the order of 1 min arc is required and we must resort to aperture synthesis techniques. Aperture synthesis in general is discussed in chapter 10 and its application to spectral line work is discussed in Section 6 here, but let us first see what has been achieved with single dish measurements.

11.4 OBSERVATIONS WITH A SINGLE DISH

11.4.1 Observing Procedure

The radiometer system commonly used consists of a multichannel (or swept frequency) receiver, whose over-all bandwidth covers the range of velocities to be found in the observed galaxy and is centered on or near the systemic velocity of the galaxy. The receiver is frequency switched in order to establish a reference outside the hydrogen line or observations are made on and off the source to find a frequency baseline for the spectrum. Scans are made across the galaxy and the intensity in each frequency channel is recorded as a function of RA and declination. The sensitivity of the frequency channels may be calibrated by observing continuum sources or by injecting broad-band noise into the system. After calibrating the data, intensity versus frequency (or velocity) spectra may be drawn on a grid of points on the sky. These are the basic data. Integration under all the profiles yields a map of the hydrogen emission brightness temperature. Radio continuum emission from the galaxy may be subtracted, on the assumption of little interaction with the line radiation, by using channels outside the hydrogen line emission or by using an off-frequency observation.

Because the resolution is limited, the frequency profiles are usually single-peaked and it is an easy process to establish a velocity at the peak, median value, or leading edge of the profile. Thus a single velocity at each grid point can be derived and a map of isovelocity contours of the line-of-sight velocity can be plotted.

Most galaxies subtend only a few beam areas, but for the nearest galaxies there are many beam areas and the maps derived give beam-smoothed estimates of the overall hydrogen density and velocity distribution.

11.4.2 Magellanic Clouds

As already mentioned, the observations of the Magellanic Clouds with the Parkes 210-foot dish have the highest physical resolution so far attained. The Magellanic Clouds cover some 800 square degrees of sky and, at a distance of $\approx$ 50 kpc, are the nearest extragalactic objects to our own Galaxy. A low resolution ($2\overset{\circ}{.}2$ beamwidth) HI survey (Hindman, Kerr and McGee 1963) showed that the Large and Small Clouds are embedded in the same HI envelope. The total HI mass of the system is some 1.5×10^9 $M_\odot$; 5.4×10^8 $M_\odot$ associated with the LMC and 4.8×10^8 $M_\odot$ with the SMC.

The 210-foot survey of the LMC (McGee and Milton 1966) revealed 52 HI complexes of mean HI mass 4×10^6 $M_\odot$ and diameter 575 pc ($\approx$ 1 HI atom/cc). The HI complexes are closely associated (in position and velocity) with HII regions and OB stars, but do not correlate with the stellar clusters.

Of 90 large catalogued HII regions by Henize (1956), 61 are closely associated with the HI complexes. The super-giant OB stars with measured velocities also have a high correlation in position and velocity with the HI complexes.

From an analysis of the rotation of the LMC and the position and velocity distribution of the population I objects, McGee and Milton proposed a spiral structure for the LMC. The total mass derived from rotational and random motions is greater than 6×10^9 $M_\odot$ giving the LMC a fractional hydrogen content of 5-9%. The 1410 MHz radio continuum also correlates well with the integrated hydrogen contours.

The neutral hydrogen distribution in the SMC is rather smooth with three major concentrations reaching peak brightness temperatures of 150, 110 and 100 K merging into a high level background. This smooth distribution

is in striking contrast to the clumpy distribution in the LMC. The most interesting feature of the 210-foot survey (Hindman 1967) is the presence of what would appear to be three massive (1 to 2 x 10^7 $M_\odot$) expanding neutral hydrogen shells of diameter 1 to 2 kpc, which could be the result of supernova explosions. The SMC is also thought to be rotating, but is only slightly flattened. The estimated mass is 1.5 x 10^9 $M_\odot$ with some 30% neutral hydrogen. As in the LMC there is a correlation between the distribution of neutral hydrogen and the bright stars. About half of the catalogued HII regions (Henize 1956) are located in the vicinity of the three major gas concentrations.

11.4.3 Nearby Spiral Galaxies

Although the Magellanic clouds are closest and allow the most detailed comparison of optical and radio features, it is important to also observe the external spiral galaxies which more closely resemble the Milky Way. Our Galaxy is thought to have a morphological form somewhere between that of M31 and M33, (see Burke, 1967, in IAU symposium No. 31). Both of these galaxies have been mapped with 10 min arc resolution, equivalent to 2 kpc at a distance of 680 kpc. At this resolution the most prominent feature of the HI distribution of M31 is a deficiency of hydrogen in the central regions, with the peak hydrogen distribution in the form of a broad ring at a radius of 50 min arc (Roberts 1966, Gottesman and Davies, 1970). The OB star associations, HII regions and radio continuum emission are all closely correlated with the ridge of neutral hydrogen, all of which suggests that star formation is proceeding at maximum rate where the neutral hydrogen density is highest, (see 11.7.5). There are several possibilities for the deficit of neutral hydrogen in the central regions of M31 (a feature it has in common with our Galaxy and several other external galaxies, see 11.7.4).

A rotation curve has been derived out to 150 min arc from the center of M31. The computed mass distribution gives an almost constant M/L (mass-to-light) ratio (= 11.9 $M_\odot/L_\odot$) over the entire galaxy. The total mass within 150 min arc is some $2 \times 10^{11} M_\odot$ giving M31 a fractional hydrogen content of 2% - typical for an Sb galaxy. There is a marked asymmetry in the isovelocity contours of adjacent quadrants of the galaxy and the rotation curves derived separately for the north and south of the galaxy differ in the central regions by some 30 km s^{-1}. These asymmetries have been interpreted as a tilt in the plane of the galaxy of some 10° and could be caused by the tidal effect of the companion galaxies M32 and NGC 205 in a similar way to the suggested influence of the Magellanic Clouds on the Milky Way (Avner and King 1967).

M33 is an Sc galaxy and has the second largest angular size in the northern hemisphere. At an assumed distance of 720 kpc it lies some 190 kpc from M31. Observations with a 10 min arc resolution (Gordon 1971) reveal a neutral hydrogen distribution with the same overall dimensions as the Holmberg optical size (83 x 53 min arc). The neutral hydrogen distribution is asymmetric with a major concentration in the south preceding quadrant and a 10% central depression. At the extreme ends of the major axis are two companions or wings of the galaxy which have a very different position angle to that of the main body of the galaxy. These wings contain 10% of the total HI mass. The computed rotation curve is rather flat-topped and the derived total mass within 60 min arc of the center is 2.3×10^{10} $M_\odot$. The neutral hydrogen mass is some 7% of this total. The velocities in the wings do not follow those predicted by the rotation curve and a consistent interpretation is that the wings are stable gaseous companions gravitationally bound to M33 rather like the Magellanic Clouds are to our galaxy. M33 is discussed in greater detail in section 11.7.1.

11.4.4 Galaxies with Smaller Angular Diameters

With more distant galaxies, where the beam size is comparable with the angular diameter of the galaxy, it is still possible to measure the line profile and estimate the mass of neutral hydrogen. The velocity width of the profile allows an estimate of the rotation or random velocities within the galaxy and, with the usual assumption of gravitational equilibrium, the mass of the galaxy may be estimated.

When the hydrogen distribution subtends 2 or 3 beamwidths, an estimate of the large scale HI distribution may be made and compared with the optical features. An example of this sort of observation is the work done by the Meudon group with the Nançay radio telescope. This instrument has a beamwidth of 4 min arc E-W by $\csc$ 24 min arc N-S at λ21 cms which allows an estimate of the E-W hydrogen distribution. Using this instrument, Bottinelli (1971) finds that the hydrogen distribution is asymmetrical with respect to the optical distribution in about 40% of the galaxies observed. The ratio of the neutral hydrogen diameter to optical diameter (measured on the Holmberg (1958) system) is observed to be a function of the morphological type, increasing towards the later type galaxies. This characteristic gives a mean HI surface density independent of the galactic type. Details of the neutral hydrogen distribution may be deduced through a model-fitting procedure and Bottinelli finds that a ring-like model for the HI distribution (as in M31) is consistent with about 30% of the galaxies observed, and that the neutral hydrogen seems to be more strongly concentrated towards the center in the early type galaxies.

11.4.5 Model Fitting

a) HI Distribution and Rotation Curve

The technique of taking a model distribution for a source and smoothing it by the observing beam is well known. We can do rather better with line

observations as the distribution of HI in a particular velocity range is a function of both the density and velocity distribution of the gas. For a rotating galaxy with isovelocity contours as in Figure 2, observations in the different velocity channels are essentially of the regions delimited by the isovelocity contours. The shape of these is determined by the rotation curve and other motions in the galaxy. Profiles of brightness temperature versus velocity may be generated from a model for the rotation curve and the neutral hydrogen distribution. The generation of model profiles is usually performed with a digital computer and many input models can be tried. The HI distribution and rotation curve which give profiles which most resemble the observed profiles are to be preferred. The chief drawback to this procedure is that there must always be two multiparameter inputs: the rotation curve and the hydrogen distribution. These interact in the generation of the model profiles and it is usually possible to get a good fit to the observed profiles with more than one input model.

b) Minor Axis Profiles

The region radiating in a small velocity range about the systemic velocity of a rotating galaxy lies close to the minor axis (See Figure 2). In a direction orthogonal to the minor axis the region observed may be much narrower than the beamwidth. With limited resolution the shape of the hydrogen distribution in a small velocity range about the systemic velocity (viz. the minor axis profile) is often observed to be double peaked or flat topped. This observation has led to the suggestion (Roberts 1967) that the distribution of hydrogen along the minor axis is also double peaked and that a ring shaped distribution of hydrogen, as in M31, is a common feature of the HI distribution in external galaxies. Consideration of Figure 2 shows that the shape of the minor axis profile is a function of both the distribution of

HI along the minor axis and the shape of the isovelocity contours defining the minor axis region observed.

In M31 the neutral hydrogen distribution along the minor axis is double-peaked in the integrated neutral hydrogen distribution as well as in a small velocity range centered on the systemic velocity and the description of the overall distribution of HI as a ring is a good one. M33 has a similar double-peaked minor axis profile in a small velocity range, but this is due to the shape of the isovelocity contours, and the HI distribution is really rather flat-topped. It remains to be seen from higher resolution observations whether a ring is a good general description of the neutral hydrogen distribution in external galaxies, (see section 7.3).

c) Mass Derivations

In many cases the internal motion of an external galaxy is well approximated by a rotation law, v(r) and if we assume that the rotating galaxy is in dynamic equilibrium under self-gravitation it is possible to derive a mass distribution from the rotation law. Several schemes have been used for calculating a mass distribution from the rotation curve. Most mass derivations based on optically measured rotation curves have used a mass model of the form of concentric spheroids developed by Burbidge, Burbidge and Prendergast (1959). The mass is calculated by fitting a polynomial to the rotation curve, and substituting this into the equation for the equilibrium of the concentric spheroids to derive the density as a function of radius. Use of a polynomial with more than 5 or 6 terms produces unrealistic oscillations in the rotation curve and the calculated mass distribution is not particularly sensitive to the number of terms in the polynomial used.

Many spiral galaxies are highly flattened and a variable density disk is a good model. Model rotation curves developed by Brandt and Belton (1962) have been much used in neutral hydrogen work as they may be inverted to give a mass distribution directly. The necessary functions are well tabulated (Brandt and Scheer, 1965). The Brandt curves are characterized by a maximum rotation velocity V_{max} at a radius R_{max}, also called the turnover radius. There is also a shape parameter n, which gives more sharply peaked rotation curves for larger values of n. The general equation is:

$$v(R) = \frac{V_{max} \times R/R_{max}}{[1/3 + 2/3\ (R/R_{max})^{n}]^{3/2n}} \qquad 11.8$$

The only physical feature of the Brandt curve is that, at large radii, the galaxy must appear as a point mass and the rotation velocity is then Keplerian. There is very little evidence from observations as to the nature of actual rotation curves beyond the turnover radius, but the Brandt curve is often a good fit up to this point and the derived mass within this radius compares well with masses derived by fitting concentric spheroids. The total mass derived by extrapolating the observed rotation curve along the best fitting Brandt curve is, however, much larger, and we have the rather unsatisfactory result that most of the mass of the galaxy lies beyond the observed region. Fitting a rotation curve model to a number of galaxies does offer a convenient and standard way of comparing the mass and derived quantities of these galaxies, but some care must be exercised in interpreting the results. The best procedure seems to be to quote a mass out to some standard radius such as the Holmberg (1958) radius. The angular momentum distribution may also be derived from the fitted density distribution and this is of interest with respect to theories

of galaxy formation from a condensing cloud of gas. The Brandt curve is characterized by only three parameters: R_{max}, V_{max}, and the shape parameter n. Since the angular momentum scales as $R_{max}^2 V_{max}^3$ and the mass as $R_{max} V_{max}^2$, we must guard against comparing any two parameters such as mass and angular momentum derived by fitting Brandt curve as they will be mathematically correlated, independent of any real physical correlation between mass and angular momentum. Indeed, in the absence of real correlation between mass and angular momentum a graph of $R_{max}^2 V_{max}^3$ versus $R_{max} V_{max}^2$ has a slope determined by the relative dispersion in the distributions of R_{max} and V_{max}. Measurements of angular momentum are also rather unsatisfactory as most of the angular momentum lies beyond the observed rotation curve.

For those λ21 cm observations where there is insufficient angular resolution to measure the radius of maximum rotation velocity directly a mass may still be obtained by estimating V_{max} from the width of the profile and R_{max} from the optical size of the galaxy. Fig. 3b is a plot of R_{max}/a (where a is the Holmberg (1958) diameter) for 21 galaxies for which the rotation curves have been determined optically from long slit spectroscopy of HII regions. The ratio is not a function of the morphological type and the histogram is quite sharply peaked with $R_{max} \approx 0.1a$. If R_{max} cannot be measured, then we can estimate it as one-tenth a in order to obtain a mass estimate.

For irregular galaxies a mass may be estimated from the virial theorem (e.g. Volders and Hogbom 1961); the mass will be:

$$M = k \, \alpha \, V_{rms}^2 / G \qquad 11.9$$

where α is the diameter of the galaxy, G is the gravitational constant, V_{rms} is estimated from the width of the velocity profile and k is a constant

of order unity which depends upon an assumed model for the density and velocity distribution.

d) Non-circular Velocities

Non-circular velocities are apparent as departures of the isovelocity contours from symmetry about the major and minor axis. In particular we are interested in analyzing the isovelocity contours for expanding hydrogen and for streaming motions in the vicinity of spiral arms as predicted by the density wave theory (see Chapter 4 and also Lin, Yuan and Shu, 1968). Analysis of these effects may be made by fitting the isovelocity contours with a model rotation curve $V = V(r)$, and a set of parameters such as the systemic velocity, inclination, position angle and rotation center.

The fitting for $V(r)$ can take place over the whole plane of the galaxy, with a higher weight given to points near the major axis. Having obtained the best-fit rotation curve, model isovelocity contours can then be subtracted from the observed isovelocity contours to give the residual velocity field. Examination of the residuals then shows more clearly the systematic non-circular or "peculiar" velocities. It should be noted that the isovelocity contours and the residual velocity field are velocities weighted by the hydrogen distribution within the beam area and particular care must be exercised in interpreting the results. The effect of beam smoothing is to bias the measured velocity towards that of hydrogen concentractions within the beam. Two examples may be given:

i) A galaxy which is a few beamwidths in diameter and which has a steep rotation curve towards the center has isovelocity contours with a separation less than the observing beamwidth. Broad frequency profiles will be observed and the estimated rotation curve will have a smaller slope than the true curve.

ii) Suppose that the hydrogen distribution has the form of spiral arms with separation rather less than the observing beamwidth. Observations between the spiral arms where there is not much HI will give a beam-smoothed profile with a velocity biased towards that of the nearest spiral arm. There is usually a gradient in the rotation velocity and observations on the inner and outer edges of the spiral hydrogen concentration will yield velocities biased in opposite directions. This is just the sort of velocity perturbation we may be looking for due to streaming motions near spiral arms! Clearly, caution must be exercised in drawing conclusions from observed peculiar velocities.

11.5 INTERFEROMETRIC OBSERVATIONS

11.5.1 Position Profiles

An interferometer with a multichannel receiver is an inherently powerful tool for line observations, because the phase in each velocity channel contains information about the position of the source of radiation received in that velocity interval. A phase relationship over several channels can confirm a detection of a weak signal, whilst for stronger signals the phase gives the relative position in the sky of radiation received in each velocity channel. A plot of position versus velocity is often called a position profile.

11.5.2 Observations of External Galaxies

For a rotating galaxy, hydrogen radiating at different velocities will arise from regions of the galaxy (such as those in Figure 2) delimited by the isovelocity contours. If observations are made with an interferometer whose baseline has an orientation close to the position angle of the major axis of the galaxy, and whose length D is not so great that the hydrogen distribution is appreciably resolved (i.e., $a > \lambda/D$, where a is the diameter of the galaxy), then the interferometer phase in each velocity channel indicates the distance along the major axis of hydrogen radiating in that velocity interval. The position profile is then a plot of the centroid positions of the regions in Figure 2 weighted by the hydrogen distribution (and smeared by random velocities, the observing beam, and the velocity filter). The amplitude in each velocity channel is roughly the product of the hydrogen density multiplied by the area of these regions. Observations of a number of galaxies have been made in this manner at the Owens Valley Radio Observatory (Rogstad, Rougoor and Whiteoak 1967) (RRW). The amplitude-velocity and phase-velocity plots are a function

of both the hydrogen distribution and the rotation curve, and the position profile obtained is subject to various interpretations.

11.5.3 Interpretation

a) Rotation Curves

For a solid body rotation curve the isovelocity contours are everywhere parallel to the minor axis and the position profile along the major axis reproduces the shape of the beam smoothed rotation curve. For any other rotation curve, interpretation is more difficult and we must resort to model fitting. If the rotation velocity falls to small values at a large radius, as in Figure 1, then the isovelocity contours form small closed areas at the high velocities as in Figure 2. Provided that these closed regions occur well within the HI distribution, then the amplitude decreases at the velocity corresponding to the appearance of small closed regions in the isovelocity contours. The position indicated by the interferometer phase at this velocity gives an estimate of the "turnover radius" where the rotation velocity is a maximum. This was the original interpretation given to the position profiles by RRW. Through a model fitting procedure they deduced the turnover radius of the rotation curve and hence together with the rotation velocity the masses of the galaxies.

b) Hydrogen Distribution

The turnover radius deduced by RRW is, on average, a factor of two larger than rotation maxima measured by Burbidge, Burbidge and Prendergast and others by means of optical, long slit spectroscopy of HII regions (e.g. BBP 1963). This leads us to consider an alternative interpretation of the position profile in terms of the extent of the hydrogen distribution (Wright, 1971). If the rotation velocity does not decrease beyond the maximum as in

Figure 1 but instead remains at a high value, then the small closed regions to not appear in the isovelocity contours. The amplitude response then decreases at a velocity where there is not much hydrogen. The position profile at this velocity then tells us the extent of the hydrogen distribution.

c) Shape of HI Distribution and Rotation Curve

In either of the above interpretations, the position profile always gives us a lower limit to the extent of the hydrogen distribution and comparison of this radius with that of the total mass and HII region distribution shows that the HI distribution is much wider than either (see Fig. 3).

We can use the disagreement between the optically derived rotation maximum and that deduced from the first interpretaiton to invert the argument as follows: If the first explanation is not correct, then the rotation velocity cannot fall to a low value as in Figure 1, but must remain at a high velocity within the extent of the hydrogen distribution. This is quite consistent with observed rotation curves (see section 7), which are indeed rather flat-topped.

11.6 APERTURE SYNTHESIS OBSERVATIONS

11.6.1 Observational Requirements

a) Angular Resolution

Model fitting of low resolution maps or of simple interferometer observations is clearly inadequate to analyze the details of the HI distribution and kinematics in spiral galaxies. Aspects concerning the spiral structure can only be investigated when we have obtained a map of the neutral hydrogen distribution with a resolution comparable to the angular separation of the luminous spiral arms. In the nearest galaxies this is of the order of 1 min arc and such resolution can only at present be obtained by the use of aperture synthesis techniques. Aperture synthesis observations of external galaxies are currently being made at 4 observatories. The instruments being used are the Cambridge Half-Mile telescope in England (Baldwin et al. 1971), the 12-element Westerbork Synthesis Radio Telescope (Brouw 1971) in the Netherlands, the 2-element interferometer at the Owens Valley Radio Observatory, and the 3-element interferometer at the National Radio Astronomy Observatory in the United States.

Observations are usually made with the telescopes at each of several separations at which the telescopes track the source over a range of hour angle. Maps of the sky brightness are computed from a Fourier inversion of the recorded data. This is the method of earth rotation synthesis. (See Chapter 10). The maximum angular resolution is determined by the largest interferometer baseline D, used in the aperture synthesis. The synthesized beam subtends a solid angle $(\lambda/D)^2$ cosec δ, where δ is the declination of the source.

If observations are made with interferometer baselines at intervals d to a maximum D, then a grating sidelobe response occurs at an angle λ/d in

RA and $(\lambda/d) \times \cos \delta$ in declination. The area of sky which can be mapped without ambiguity from grating side lobes is $(\lambda/d)^2$ cosec δ. The baseline interval d should be sufficiently small that this area includes the extent of the neutral hydrogen radiating in any velocity channel, otherwise the synthesized map will be confused by grating sidelobes. There is no point, however, in making d much smaller than the diameter of the antennas since the reception pattern of these then limits the area of sky which can be mapped.

b) Frequency Resolution

Observations of spiral galaxies show that the greatest range of velocities expected is about $\pm$ 300 km sec^{-1}, and it is desirable that a multi-channel receiver should cover the whole of this range. The maximum useful resolution in velocity is dependent on the angular size of the synthesized beam, since in general the line-of-sight radial velocity varies in a systematic way across the galaxy. Near the center of the galaxy the area of the synthesized beam intersects many isovelocity contours (see Figure 2); a large range of velocities are present within one beam area and a high velocity resolution is not required. Further out in the galaxy, however, there is a small range of rotation velocities within one beam area and a higher resolution might be useful. Dispersion in the gas along the line-of-sight might be of order 10 km s^{-1} and this accordingly is a useful resolution. Thus a desirable minimum for a multichannel receiver is 60 channels each 10 km sec^{-1} wide, for each interferometer.

c) Sensitivity

Suppose that we spend equal times observing at each interferometer baseline at intervals d to a maximum D. The total integration time is proportional to D/d. The angular resolution obtained is proportional to

$\theta = \lambda/D$ so that for a given stepping interval d (which is determined by the angular extent of the hydrogen) the fluctuations in aerial temperature T_a are proportional to $\theta^{1/2}$. As a result of the aperture synthesis, only flux collected by the synthesized beam contributes to the effective aerial temperature of the source. The aerial temperature, T_a due to a source of uniform brightness temperature T_b, is obtained by multiplying T_b by the ratio of the synthesized beam area to the antenna beam area. Thus $T_a \approx T_b\theta^2$ and the sensitivity of the telescope to extended objects decreases with resolution as:

$$T_a/\Delta T_a \approx T_b\, \theta^{3/2} \qquad 11.10$$

This degrading of the signal-to-noise ratio with increasing resolution can be offset by spending a longer time at the larger aerial spacing and the reason for this requirement may be understood in terms of the increased rate of sampling of the u-v plane at the longer baselines (see Chapter 10). It does, however, mean that the sensitivity requirements may limit the resolution rather than the available baseline.

11.6.2 Correlation Receivers

The requirement for a large number of velocity channels has favored the use of cross-correlation receivers. The principle on which the cross-correlation receiver operates is that, for two random, time-varying signals, $V_1(t)$, $V_2(t)$, the cross correlation function,

$$\sigma(\tau) = \int V_1(t)\, V_2(t - \tau)\, dt \qquad 11.11$$

is the Fourier transform of the visibility spectrum $V_1(\omega)\, V_2(\omega)$ of the two signals. Here the signals $V_1(t)$ and $V_2(t)$ are the voltages from the two

telescopes forming the interferometer, and $V_1(\omega)\ V_2(\omega)$ is the cross-correlated spectrum at an angular frequency ω. The cross-correlation function is sampled over a range of delays $\pm\ \Delta T$, $\pm\ 2\Delta T$,...to a maximum delay $\pm$ T sec, and the visibility spectrum is obtained as the Fourier transform of the sampled cross-correlation function.

The maximum delay, T, determines the resolution of the synthesized frequency channel, $\frac{1}{2T}$ Hz, and the sampling interval ΔT, produces a grating response in frequency at an interval $\frac{1}{2\Delta T}$. The exact shape of the equivalent frequency-filter is the Fourier transform of the weighting applied to the cross-correlation function. If the latter is transformed with equal weight applied to each delay, then the equivalent frequency filters have a $(\sin \theta)/\theta$ response with a half-width of 1.2/2T Hz and 22% sidelobes. Both positive and negative delays must be sampled to determine the amplitude and phase of the interferometer and the correlation receiver is equivalent to a bank of $T/\Delta T$ adjacent frequency filters at intervals of 1/T Hz.

The cross-correlation may be achieved in practice either in an analogue device using physical delay steps or in a digital correlator. In the latter, simplified logic results if one-bit sampling of the correlation function is employed (so that only the sign of the sampled correlation function is recorded). This results in some loss in signal-to-noise ratio, but the visibility spectrum may be fully restored (Weinreb 1963), through the Van Flyck correction. While increasing the complexity of the data processing, as an extra Fourier transform must be computed, the correlation receiver has a number of advantages over a conventional filter bank receiver in that the relative sensitivity of the frequency channels is easily calibrated. A digital correlator has good stability essential for a good synthesis,

and the additional advantage that the bandwidth can be changed by simply changing the clock-rate which determines the sampling interval.

11.6.3 Data Reduction

a) Frequency Fourier Transform

If a correlation receiver has been used, then the first stage is a Fourier transform to recover the visibility spectrum of the signal. It should be noted that the shape of the frequency filters is under our control as we can apply a weighting function to the correlation function before computing the Fourier transform (this is equivalent to convolving the spectrum after the Fourier transform). Thus we can reduce the 22% frequency sidelobes associated with a uniform weighting function, at the expense of an increased half-width. The frequency Fourier transform is often made in an on-line computer which receives data directly from the correlator.

b) Calibrations

There are two basic calibrations in addition to the usual interferometer baseline and system gain and phase calibrations of a broadband interferometer (see Chapter 10). These are:

i) To determine the relative sensitivities of the frequency channels;

ii) To determine the sensitivity and system phase of the telescope as a function of frequency.

c) Spatial Fourier Transform

Each frequency channel may be separately Fourier inverted as for a broadband interferometer as discussed in chapter 10. The chief problem is the large quantity of data to be processed and the computation may take several hours even on the largest computers using fast Fourier transform techniques.

d) Presentation of the Data

The end product of the above processing is a series of maps of the hydrogen distribution in the different frequency channels. These maps form the basic data which can be considered as a three dimensional array with x, y, and frequency coordinates. The maps of frequency channels containing line emission may be combined to produce a map of the integrated line-emission, and a map of frequency spectra at a grid of points on the area of sky studied. A velocity (or profile width) can then be fitted to the frequency spectra and a map of isovelocity contours drawn across the source. There is obviously a considerable data-handling problem associates with mapping a 1 degree square of sky, say, with an angular resolution of 1 min arc at 60 different velocities, and the basic problem is presenting the information in a digestible form. It is to be expected that fairly exotic techniques will eventually be used in this final and most important stage of data reduction, namely in the interface between the data and the astronomer.

11.7 HIGH RESOLUTION MAPS

11.7.1 Observations of M33 with the Cambridge Half-Mile Telescope

a) Observations

The highest resolution observations of an external galaxy so far made using aperture synthesis techniques are those of M33 made with the Cambridge Half-Mile telescope (Wright, Warner and Baldwin 1972). This telescope consists of two 9m paraboloids on an east-west baseline and was designed as an aperture synthesis instrument for observing extended objects. The observations of M33 have an angular resolution of 1.5 min arc in RA and 3 min arc in declination, equivalent to a 300 x 600 pc area at the distance of M33 (690 kpc). (This compares with a linear resolution of 210 pc in the Magellanic Clouds using the Parkes 210-foot telescope). The velocity resolution of these data is 39 km s^{-1}, commensurate with the range of velocities expected within a 300 x 600 pc area over most of the galaxy. Observations were made at 59 interferometer baselines with telescope separations at 6m intervals to a maximum of 360m. The full baseline (720m or half-a-mile) was not used for reasons of sensitivity as discussed in the previous section. The data were obtained using an analogue cross-correlation receiver, and were processed much as described in the previous section. The basic data is in the form of nine maps of the HI distribution at 26 km s^{-1} intervals. These nine maps cover the range of velocities found in the neutral hydrogen of M33.

b) Integrated HI Brightness Distribution

For these observations the half-width of a velocity channel is larger than the velocity interval between the channels, and a simple addition of these

nine maps suffices to construct a map of the integrated hydrogen distribution in M33 (Figure 4). This map is of the surface brightness temperature of the hydrogen line integrated over the line profile.

If the galaxy is everywhere optically thin to the line radiation, then the map also represents the distribution of the HI surface density projected along the line of sight. The peak brightness temperature observed is 50 K but the distribution is in places unresolved in both angle and velocity so that the true brightness temperature may exceed 100 K and the line radiation may not be optically thin. Where the radiation is not optically thin, the brightness temperature gives only a lower limit to the surface density. There is no direct evidence of optically thick HI from absorption of continuum sources lying behind or in the disk of M33, and we can adopt as a working hypothesis that the line radiation is optically thin, so that the map of the integrated brightness temperature is also a map of the HI surface density.

c) Large-Scale Structure

The large-scale structure of the hydrogen distribution may be obtained with a higher signal-to-noise ratio on a lower resolution map (which may be obtained in aperture synthesis observations by simply not including data from the larger interferometer spacings in the Fourier transform). A low resolution map generated from the above data agrees well with the map obtained by Gordon (1971) with the N.R.A.O. 300-foot telescope and described in section 4. Figure 5 is an integration in elliptical rings (circular in the plane of the galaxy) of the brightness temperatures of Figure 4, and shows that the average radial distribution is a plateau with a very sharp cut off at the edges. The radial distribution in Figure 5 is not in good agreement with the suggestion by Roberts (1967) that the HI has a ring distribution as in M31. The average

projected surface density is $\gtrsim 3 \times 10^{21}$ atoms cm^{-2} or 1.7×10^{21} cm^{-2} viewed normal to the plane of the galaxy. The sharp fall in density at the edges of the galaxy could be due to ionization by an intergalactic flux of UV photons as discussed by Sunyaev (1969). An alternative explanation is that the sharp gradients at the edges of the galaxy are associated with the warping of the plane of the HI disk indicated by the wings of the galaxy. A hat brim model is envisaged with an increased declination of the plane of the galaxy to the line-of-sight along the edges of the galaxy at the ends of the minor axis.

There is a marked asymmetry in the HI distribution with a massive HI complex in the south preceding quadrant of the galaxy.

d) Small Scale Structure

The HI distribution is broken up into a large number of concentrations only partially resolved by the 1.5 x 3.0 min arc beam. These concentrations have a typical peak surface density of 2.7×10^{21} cm^{-2} and a space density of ~ 1 to 2 atom cm^{-3}. They perhaps resemble the complexes discussed by McGee (1964) in the spiral arms of our Galaxy, having sizes $\gtrsim$ 500 to 2500 pc and densities $\gtrsim 0.5$ cm^{-3}, and those in the Large Magellanic Cloud having mean diameter 600 pc and density $\gtrsim 1$ cm^{-3}. A spiral arm structure can be seen in the inner regions of the galaxy and is most evident in the trough running south from the galactic center (Figure 4). A best fitting logarithmic spiral structure agrees with the optical spiral arms and the measured ratio of the average projected HI density in the arm and inter-arm regions is between 2 or 3 to 1. The troughs between HI concentrations are barely resolved by the beam and the true density ratio may be as large as 6 to 1. An infinite contrast ratio is, however, ruled out by these observations.

e) Comparison with Optical Features

The extent of the HI distribution corresponds well with that of a well exposed blue print of the galaxy and the major and minor axis widths are close to the 83 x 53 min arc given for the optical size by Holmberg (1958).

Figure 6 shows a superposition of the HI peaks onto a plate taken through a narrow-band red filter. It can be seen that the HI concentrations follow the line of the optical spiral arms well in the south of the galaxy. The correlation is not so clear, and there are no strong HI concentrations on the northern spiral arm between the nucleus and NGC 604 where there is again a large concentration of HI. The contrast of the spiral arms is better in the composite HI + HII distribution in Figure 6 than in either the HI or HII regions separately, which indicates that the HI and HII are in some sense complementary.

f) Rotation Curve and Total Mass

The isovelocity contours (Figure 7) conform well to the pattern expected for a rotating galaxy and the rotation curve measured along the major axis is shown in Figure 8. The total mass can be derived by fitting a model rotation curve. The observed rotation curve has been fitted to three different types of rotation curve, a Brandt rotation curve with n = 1.0, a curve corresponding to an exponential distribution of mass (as discussed by Freeman 1971), and an 8th order polynomial. In all three cases the fitted curves agree with the observed rotation curve within 3 km s^{-1}, and it will clearly be difficult to distinguish among them. The distribution of mass with radius deduced from these three fitted rotation curves is very similar within $\approx$ 20 min arc radius but diverges outside this radius. Using a Brandt curve with R_{max} = 30 min arc,

V_{max} = 100 km s^{-1} and n = 1.0 gives a mass within 45 min arc of 1.7 x 10^{10} $M_\odot$. The HI content is then some 9%, typical for an Sc galaxy. Because of the very flat rotation curve the total mass of the galaxy extrapolated beyond the observed rotation curve is some 5 x 10^{10} $M_\odot$, but this may not have much meaning.

g) Peculiar Velocities and Streaming Motions

It is clear from Figure 7 that there are local departures of the isovelocities from circular motion which exceed the noise level. It is essential, however, to consider the effect of beam averaging. A superposition of Figure 4 and Figure 7 shows that the deformation in the isovelocity contours often correspond to their crossing between HI peaks. The velocity in the interarm region is a beam average of the velocities of all HI concentrations within the beam at that time, and we may consequently discount many of the departures from smooth isovelocities. Some of the departures are real, however, and local peculiar velocities can be 20 to 30 km s^{-1}.

The line-of-sight velocity due to the rotation of the galaxy may be computed by selecting values for the rotation center, position angle, inclination and rotation curve of the galaxy. If this model velocity field is subtracted from the observed velocity field, errors in the parameters selected show up in the residual velocity field with characteristic symmetries and enable best values for the rotation parameters to be determined. The residual velocity field may then be examined for systematic streaming motions predicted by the density wave theory of spiral arms. From the present observations of M33 it appears that such streaming motions are less than about 5 km s^{-1}.

h) Comparison of Neutral and Ionized Hydrogen Velocities

In Figure 9 are plotted the velocities of the large HII regions measured by Mayall and Aller (1942) against the HI velocity at the HII region position. Because of the relatively large beamwidth (1.5 x 3 min arc), the HI velocities are best regarded as an average velocity of HI in the vicinity of the HII region. The HII region velocities are local velocities of ionized gas within the HII region. The straight line has a slope of one showing that there is no systematic difference between the velocities of neutral and ionized gas. The vertical scatter in Figure 9 shows that the velocity of an HII region can differ by 20 to 30 km s^{-1} from that of the neutral gas. Indeed, measurements within a single HII region can differ by the same magnitude. Estimates of the mass of gas in large HII regions (e.g. in 30 Doradus in the LMC (Faulkner 1967) and in NGC 604 in M33 (Wright 1970)) show that velocity dispersions of this magnitude will disperse the HII region in $\approx 10^7$ years.

11.7.2 Observations at the Owens Valley Radio Observatory

a) Observations

The two element interferometer at the Owens Valley Radio Observatory has been used to map a number of late type galaxies to an angular resolution of 2 min arc and a velocity resolution of 21 km s^{-1}. The Owens Valley interferometer is able to track sources over only a limited hour angle range but both E-W and N-S spacings are available so that good coverage of the u-v plane can still be obtained. Fixed observing stations are positioned at 100-foot intervals giving a grating sidelobe response at 20 min arc radius and enabling sources smaller than this to be mapped without confusion.

For larger galaxies special techniques must be used to eliminate the sidelobe response. A powerful technique, first used in the case of M101

(Rogstad and Shostak 1971), is to iteratively subtract the synthesized beam together with its sidelobes from the maximum of the source region of the synthesized map. The iteration stops when the sources being subtracted are a small percentage of the original maximum or the residual map approaches the noise level. A map, corrected for the sidelobe response, is then reconstituted by convolving the subtracted sources with a clean, sidelobe-free beam and adding them back into the residual map.

This procedure may not result in a unique map, but there are some tests on the validity of the procedure which is discussed in more detail in chapter 10.

b) Integrated Hydrogen Distribution of M101.

Figure 10 shows the integrated HI brightness of M101 observed with a 4 min arc beam. Most remarkable in Figure 10 is the ring distribution and the marked asymmetry in the hydrogen distribution. If the gas is assumed to be optically thin, then the contour interval corresponds to a HI surface density of 1.4 atom cm^{-2}. For an assumed distance of 6.9 Mpc the integrated HI mass is 9×10^9 $M_\odot$. If the HI distribution is really symmetric and the asymmetry in the integrated brightness is due to variations in the spin temperature of the gas, then this mass would be increased by $\tilde{\sim}$ 25%. Assuming that the gas is optically thin, the central depression in the integrated brightness represents a surface density of $\sim 3.5 \times 10^{20}$ atom cm^{-2}. Monnet (1971) has observed a weak background of Hα radiation in several galaxies. In M101 the estimated plasma density is nearly sufficient to account for the missing hydrogen suggesting that the gas is highly ionized.

c) Velocity Field and Streaming Motions in M101

The velocity field of M101 (Figure 11) derived from the HI observations (Rogstad and Shostak 1971) displays many deviations of $10 \sim 20$ km s^{-1} from

circular rotation of the gas. Many of these deviations are in the form of ridges in the vicinity of the luminous spiral arms. Rogstad (1971) has interpreted this as evidence for the density wave theory of spiral structure (see chapter 4).

There are further deviations in the isovelocity contours near the nucleus of M101 which could indicate expansion motions $\gtrsim$ 40 km s^{-1} in the vicinity of an inner spiral arm and coincident with a central nonthermal radio source. The outflow of HI is sufficient to account for the even deeper hole in the HI distribution of the nuclear region.

11.7.3 Comparison of the HI Distributions of Late-Type Galaxies

a) Observations

Several other galaxies have recently been mapped at the Owens Valley. NGC 6946 and IC 342 (Rogstad et al. 1972); NGC 2403, NGC 4236, and IC 10 (Shostak 1972); M51, M81 and M82 (Gottesman and Weliachew 1972); and Maffei 2, IC 2574 and NGC 7640 (Seielstad and Wright 1972). Papers describing these results are in preparation. These observations have an angular resolution of 2 min arc and a velocity resolution of 10 or 21 km s^{-1}.

NGC 2403 is an Sc^- (Holmberg system) galaxy and is very similar in morphological form and stellar content to M33 (see Hubble Atlas - Sandage 1961). The integrated brightness distribution (Figure 12a) has a marked depression in the central region, similar to that in M101, but quite different from the HI distribution in M33. The three highest peaks in the integrated HI brightness distribution do not correspond well with the luminous spiral features, but rather lie in the dust lanes between the luminous spiral arms. A number of bright HII regions can be seen around the edges of these HI peaks. This can also be seen in places in M33. The rotation curve, as in M33, is

very steep at the center and has a large constant-velocity region extending to the boundary of the detected hydrogen (as suggested in section 5).

NGC 4236 is classified Sc^+ by Holmberg (1958) and SB 7 by de Vaucouleurs (1964). A number of hydrogen concentrations can be seen in Figure 12b, the largest peak in the north corresponding to a bright HII complex at the end of the "bar". The HII regions in the south, on the other hand, tend to lie around the HI peaks. The rotation curves of NGC 4236, NGC 2403 and M33 all have the same characteristic shape if scaled to common rotation curve maxima, R_{max} and V_{max}.

IC 10 is an irregular galaxy in a heavily obscured region of the sky. The integrated HI distribution in Figure 12c shows a number of peaks and a large depression where the integrated brightness falls to zero. The peak brightness of all three galaxies is very similar ($\approx$ 1200 K km s^{-1}), although the inclinations are different.

b) Five Scd Galaxies

In a comparison of the five Scd galaxies M33, NGC 2403, IC 342, M101 and NGC 6946, Rogstad and Shostak (1972) find substantial similarities in the hydrogen distributions and rotation curves. The integral HI parameters are nearly constant or scale with the Holmberg (1958) diameter. 80% of the observed HI mass lies within the Holmberg diameter for each galaxy. The mean hydrogen content is 11% of the total mass within this same boundary and the central HI surface density is also nearly constant ($\simeq 8 \times 10^{20}$ atom cm^{-2}).

The rotation curves are all observed to be flat topped with a maximum velocity proportional to the Holmberg diameter. Because of the flat-topped rotation curves, the total masses extrapolated to infinite radius are indeterminate, but the total mass within the Holmberg radius is proportional

to $R_{H_o} V^2_{max}$ and therefore scales as $R^3_{H_o}$ for these five galaxies. The constancy of the integral properties within one morphological class is an important justification for the use of the morphological classification system for spiral galaxies.

11.7.4 Central Hydrogen Depressions

As suggested by Roberts (1967) (see section 4.5), it appears that a central depression in the HI surface brightness is a common feature in late-type spiral galaxies. M31 is the most obvious case where an HI "ring" is a good overall description. For the other galaxies so far observed, the HI distribution is better described in terms of an asymmetry and a central depression. In no observed galaxy does the surface brightness resemble the overall light distribution, which is exponentially decreasing, or the total mass distribution (deduced from rotation curves or from an assumed mass-to-light ratio). The total mass and light distribution are centrally peaked; the HI surface brightness is rather flat or centrally depressed. There are several possible explanations:

i) The usual assumption that the gas is everywhere optically thin may not be correct. It is almost certainly true that small, cold, optically-thick clouds occur locally in every galaxy. If the spin temperature or the cloudiness of the HI varies systematically across the galaxy, then the surface brightness of HI line radiation may not resemble the HI surface density distribution. This explanation requires lower spin temperatures or very clumpy HI in the central regions of galaxies.

ii) The thickness of the HI layer may increase with radius as observed in our Galaxy (Kerr and Westerhout 1965). The HI layer thickness

in M33 can be estimated from the measured velocity dispersion in the HI line profiles (Wright 1972). If we assume that the vertical velocity dispersion (c^2) supports the gas against gravitational attraction, then the half-thickness ($\bar{z}$) of the gas layer is given by Mestel (1963) as

$$\bar{z} = c^2/2\pi G\sigma \qquad 11.12$$

where σ is the total mass surface density in the plane of the galaxy. σ has been estimated from a mass, model-fit to the rotation curve and decreases with radius. To first order the observed velocity dispersion in M33 is constant, therefore the HI layer-thickness increases with radius. In M33 the HI surface density is roughly constant with radius (see Figure 5), therefore the HI volume density decreases with radius. This is consistent with the observed decrease in the rate of star formation with radius in M33 (Madore et al. 1972). In M31 a ten-fold increase in layer thickness would make the HI volume density in the central regions equal to that at the position of the ring.

iii) The gas in the central regions may be ionized. Monnet (1971) has observed a weak background of Hα radiation in the central regions of several galaxies. In the case of M31, however, the emission measure was less than 10 cm^{-6} pc which is too small by an order of magnitude to give a surface density comparable with that of the HI peak.

iv) The gas could be in molecular form without any observable consequences. Molecular hydrogen has been seen in the far-ultraviolet absorption spectra of the star ξ Persei which has a strong ultraviolet continuum emission (Carruthers 1970).

Observation of H_2 in external galaxies is far beyond present techniques.

v) Neutral hydrogen is expanding away from the central regions of the Milky Way (see Oort 1964 and Kerr 1967). The 3 kpc arm feature of our Galaxy is expanding at a velocity of some 53 km s^{-1}, whilst asymmetry in the rotation curve for our Galaxy can be interpreted as a 7 km s^{-1} expansion in the vicinity of the sun. The outflow of neutral gas from the central regions (about 1 $M_\odot$ per year) might be partially balanced by an inflow (under one interpretation of the high velocity gas seen at high latitudes in the Galaxy (see Oort 1967)), but is otherwise sufficient to deplete the central regions of HI in some 10^7 to 10^8 years.

Expansion motions have been observed in the central regions of some external galaxies (e.g. M101) but in M31 are less than 10 km s^{-1} (Gottesman and Davies 1970) and are too small to have removed a significant mass of HI away from the central regions.

vi) The gas in the central regions may have been used up by star formation. Star formation would initially be fastest in the central regions of galaxies where the gas density is highest. At the present epoch the rate of star formation in M31 is at its peak in the region of the ridge at 10 kpc radius.

The correct explanation of the deficit of HI in the central regions is probably a combination of explanations ii) and vi) although in some instances explanations iii) and v) may be highly significant . Explanations i) and iv) are unknown factors.

11.7.5 Rate of Star Formation

The rate of star formation is presumed to depend on the gas density. Attempts to find a relationship of the form:

$$d\rho_*/dt = \text{const.} \times \rho_g^n \qquad 11.13$$

(where ρ_* is the star (or HII region), and ρ_g the gas density), have derived different values for the exponent n. Comparison of HII region and bright star counts with HI surface densities have been made for the SMC, M31 and M33. For bright stars in the SMC Sanduleak (1969) obtained a value of n = 1.84 ± 0.14. In M31 Hartwick (1971) obtained a value, n = 3.50 ± 0.12 by comparing HII region counts with Robert's (1966) HI density.

A comparison of the HI surface density in M33 (Wright et al. 1972) with HII region and star counts in M33 (Madore 1971) finds a value of n = 1.72 ± 0.01 for stars and n = 3.15 ± 0.18 for HII regions. Most of the stars counted in M33 are the less massive O and B stars, whilst only large HII regions (excited by massive O stars) are included. The different values of n obtained in M33 tend support to the suggestion by Schmidt (1963) that n is largest for the most massive stars. The values of n obtained for HII regions are in good agreement in M31 and M33.

11.8 CONCLUSIONS

The observations presented in the previous section represent the present state of the art of mapping neutral hydrogen in external galaxies. Aperture synthesis observations of a number of nearby late type spiral galaxies are in progress at the present time, and we should soon be able to see if the HI distributions of, say, Sb and Sc galaxies are characteristically different.

Maps made with the Westerbork telescope to an angular resolution of 23 sec arc should soon be available allowing a detailed comparison of HI structure in many more galaxies. Details of the HI density and velocity distribution in the luminous spiral arms should make possible a much better understanding of star formation and of the dynamics of the spiral patterns.

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FIGURE CAPTIONS

Figure 1. Model rotation curve showing

i) solid body rotation out to 3 units radius

ii) constant velocity region between radii 3 and 4

iii) region of decreasing rotation velocity.

Figure 2. Isovelocity contours (lines of constant line-of-sight velocity) in a rotating galaxy. The contours are drawn at intervals of the units of velocity in Figure 1. The region of solid body rotation is shown enclosed by the dashed line.

Figure 3. Plot against morphological type of galaxy and a histogram for:

(a) Turnover radius, ρ/a, for galaxies observed by RRW.

(b) Radius of maximum rotation velocity for optically derived rotation curves.

(c) Radius of maximum HII region count, R(HII)/a for galaxies observed by Hodge.

Figure 4. Integrated HI brightness in M33 to an angular resolution of 1.5 x 3 min arc.

Figure 5. Integration in circular rings in the plane of M33 of the integrated brightness distribution.

Figure 6. Superposition of the peaks of the HI distribution of M33 on a red print showing mainly HII regions.

Figure 7. Isovelocity contours in M33 drawn at intervals of 10 km s^{-1}.

Figure 8. Rotation curve measured along the major axis of M33. The rotation velocities uncorrected for inclination are referred to a heliocentric systematic velocity of -175 km s^{-1}.

Figure 9. Velocities of HII regions (ordinate) plotted against the neutral hydrogen velocity at the position of the HII region. (Open circles, o, are HII regions measured by Mayall and Aller (1942) with velocities by Brandt (1965), (o) velocities by Mayall and Aller, vertical columns, x, velocities by Carranza et al. (1968). The left ordinate and abscissa scale are heliocentric, right ordinate velocity with respect to a systematic velocity of -175 km s^{-1}. The line has a slope of one.)

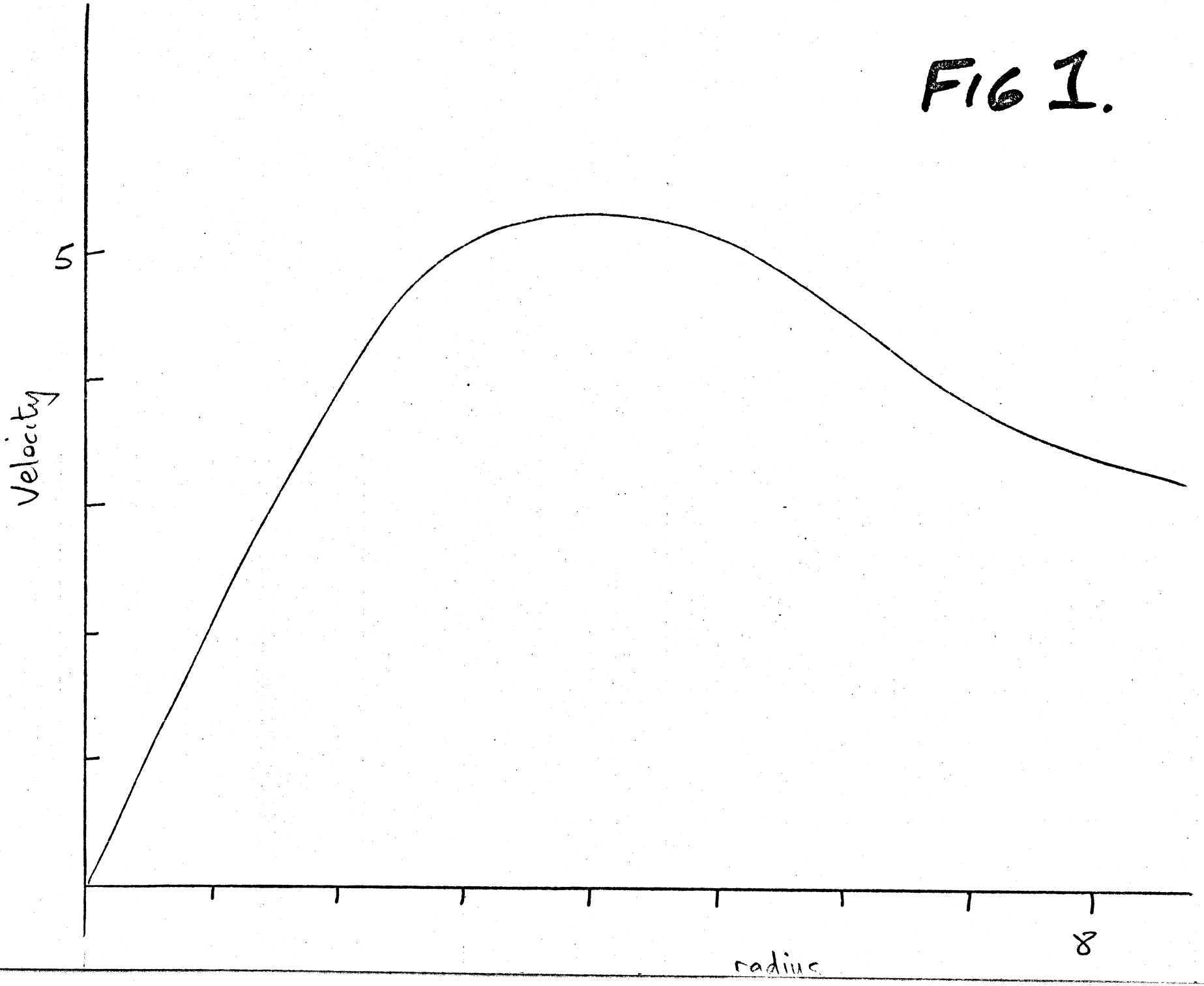
Figure 10. Integrated HI brightness in M101 to an angular resolution of 4 min arc.

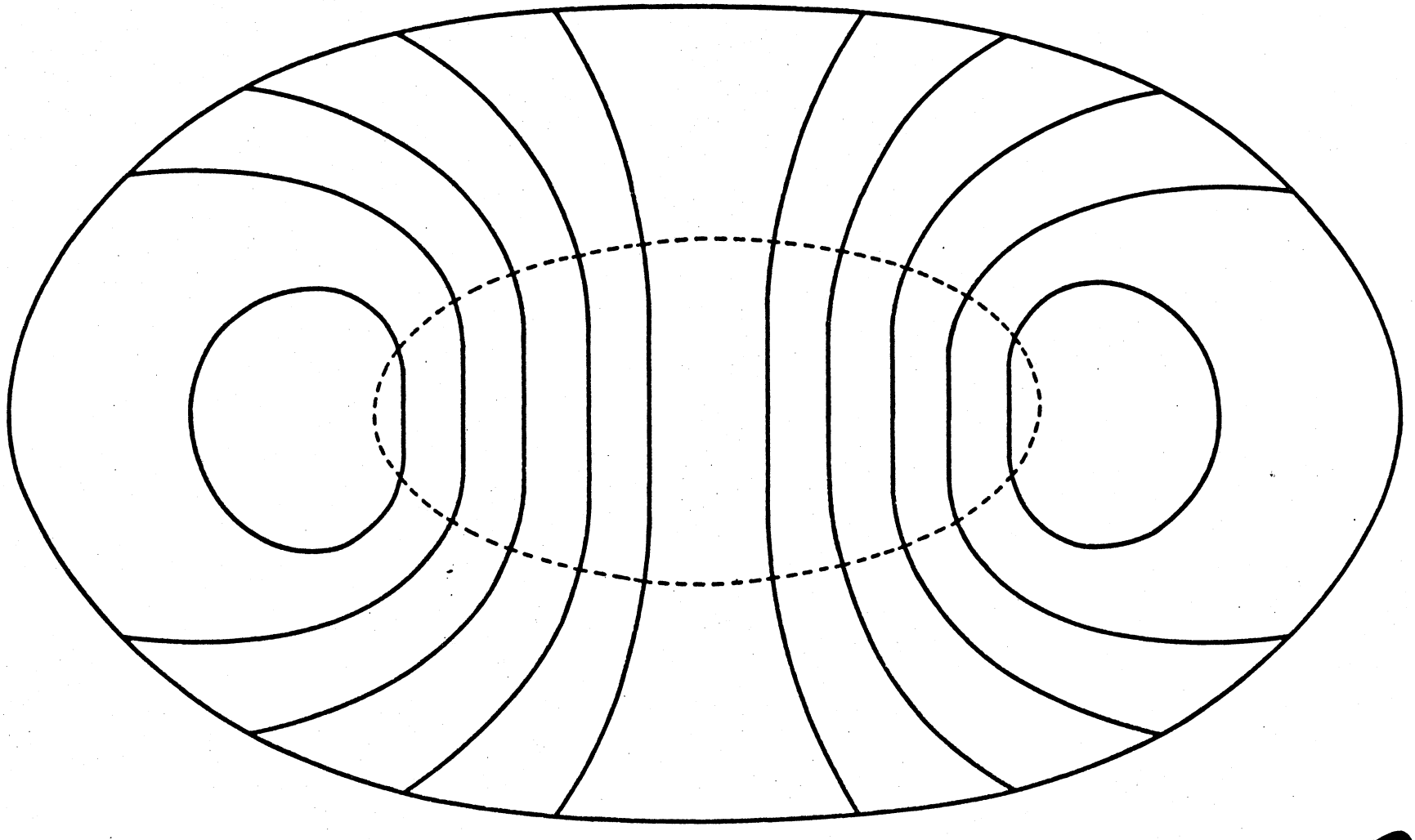
Figure 11. Isovelocity contours in M101.

Figure 12. Integrated HI brightness contours to a 2 min arc angular resolution superposed on blue sky survey print. Contour interval 600 K x km s^{-1}.

a) NGC 2403
b) NGC 4236
c) IC 10

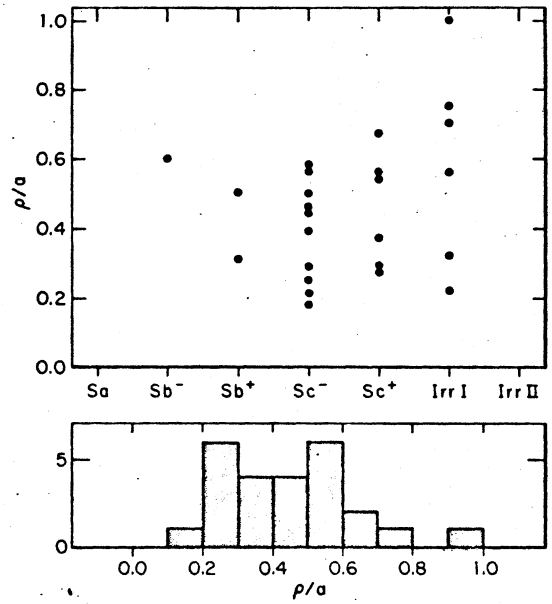
FIG 1.





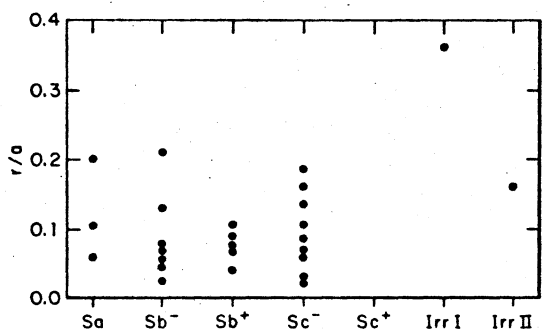
Lines of constant radial velocity in a rotating galaxy

2

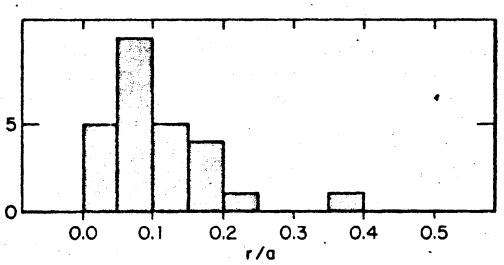

1.0
0.8
0.6
0.4
0.2
0.0
ρ/a
Sa
Sb⁻
Sb⁺
Sc⁻
Sc⁺
Irr I
Irr II

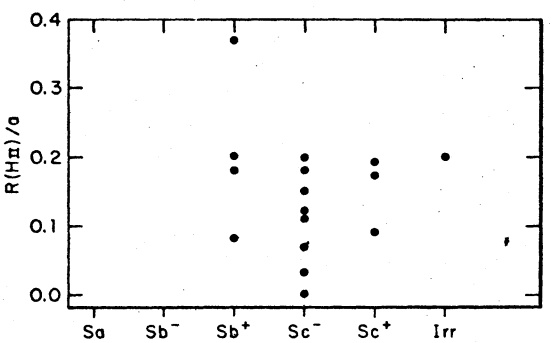
a

5
0
0.0
0.2
0.4
0.6
0.8
1.0
ρ/a

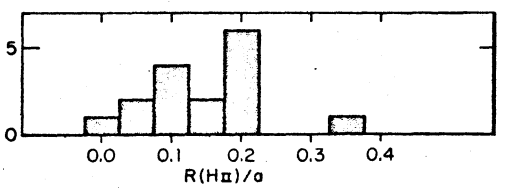

0.4
0.3
0.2
0.1
0.0
r/a
Sa
Sb⁻
Sb⁺
Sc⁻
Sc⁺
Irr I
Irr II

b

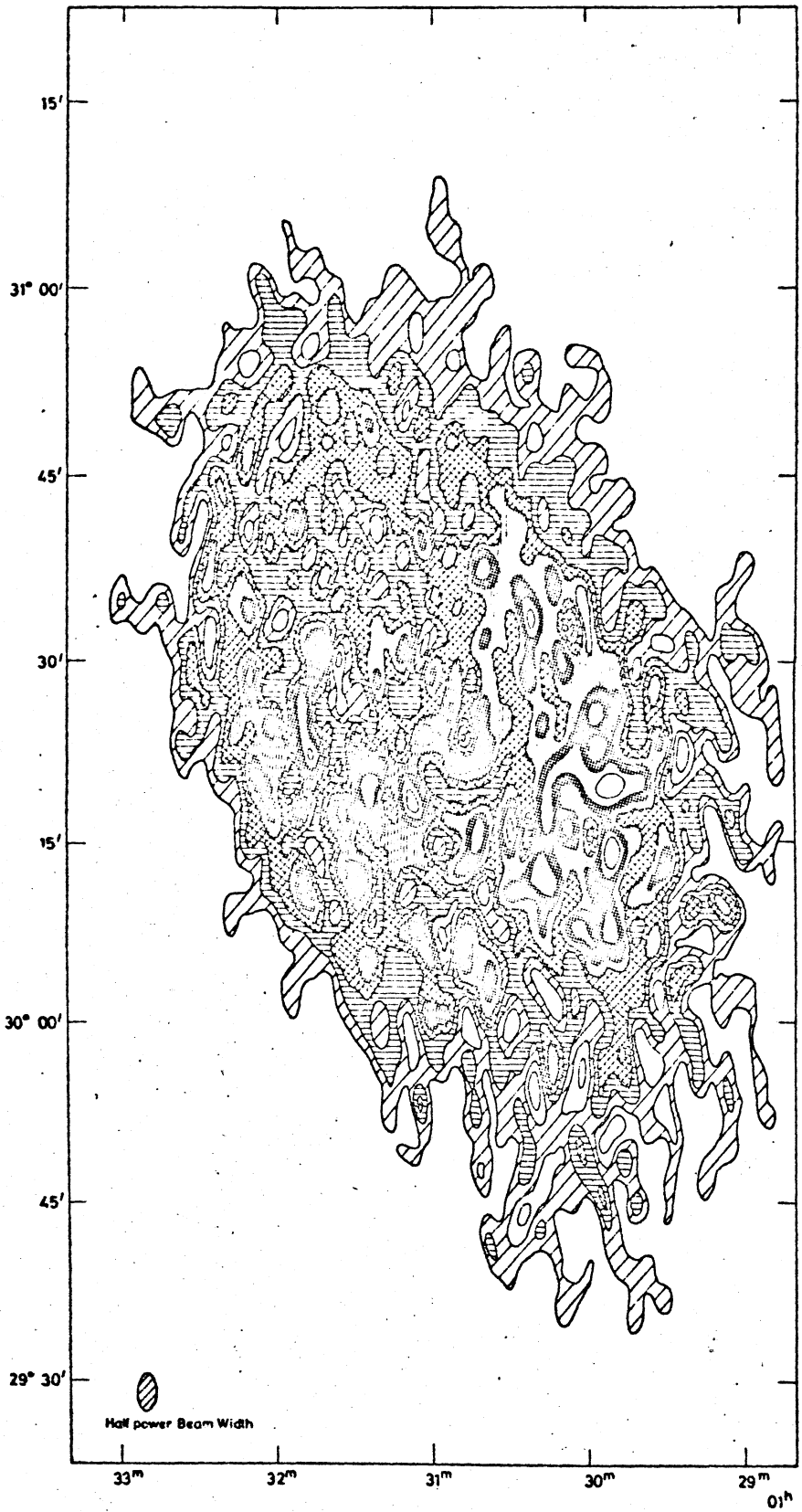

5
0
0.0
0.1
0.2
0.3
0.4
0.5
r/a


0.4
0.3
0.2
0.1
0.0
R(Hα)/a
Sa
Sb⁻
Sb⁺
Sc⁻
Sc⁺
Irr

c


5
0
0.0
0.1
0.2
0.3
0.4
R(Hα)/a

3


15′
31° 00′
45′
30′
15′
30° 00′
45′
29° 30′
Half power Beam Width
33m
32m
31m
30m
29m
01h

4

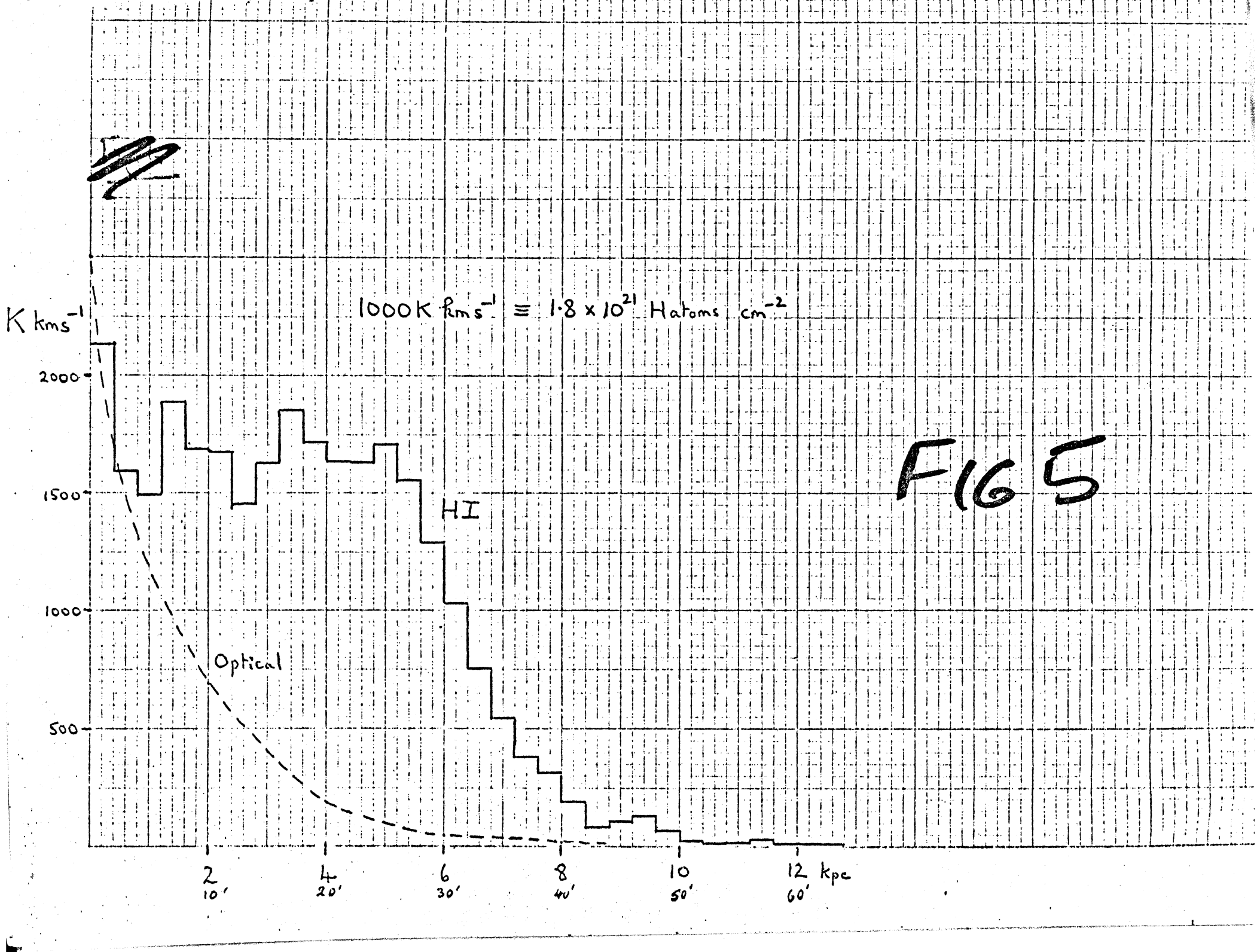
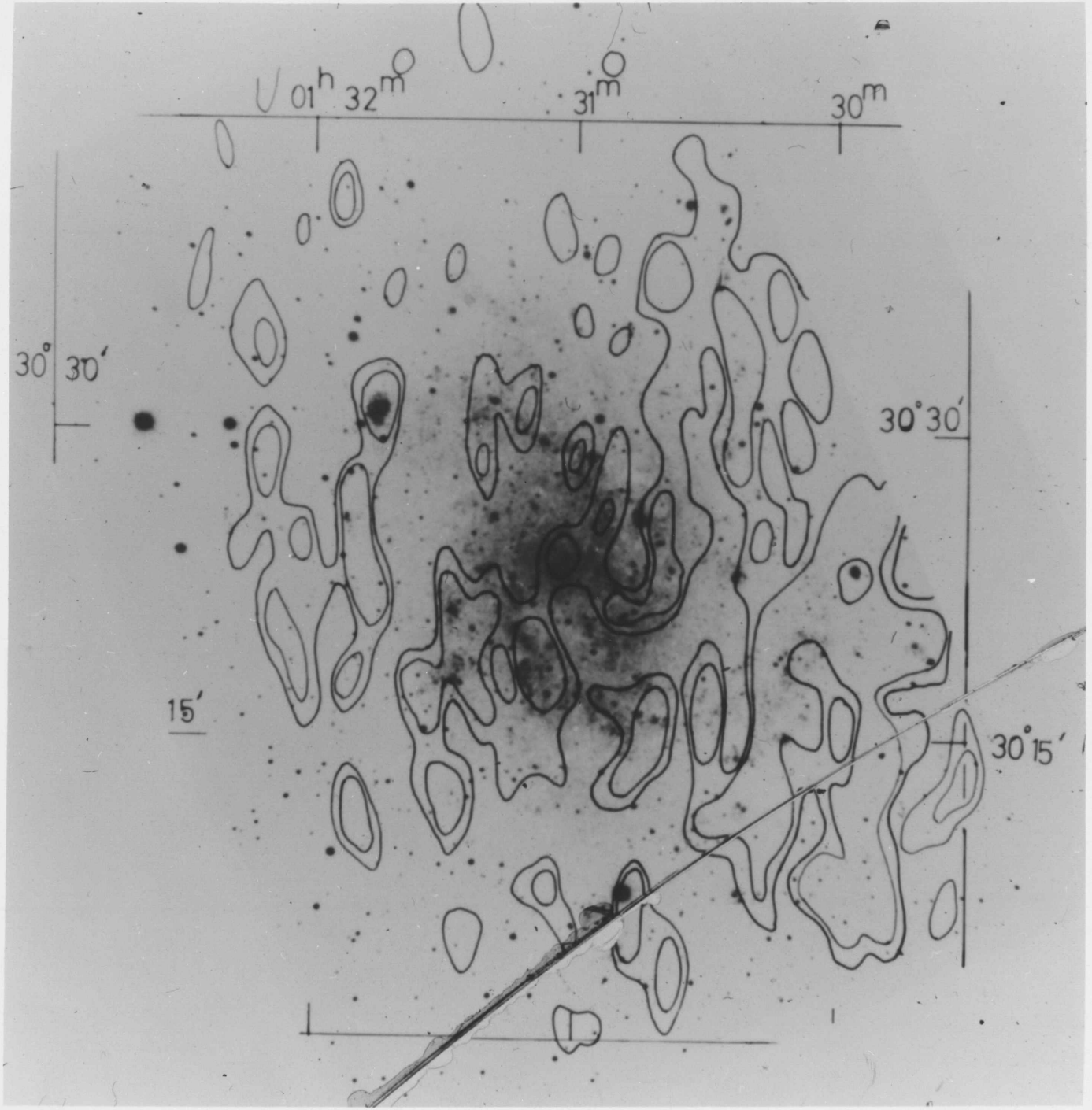
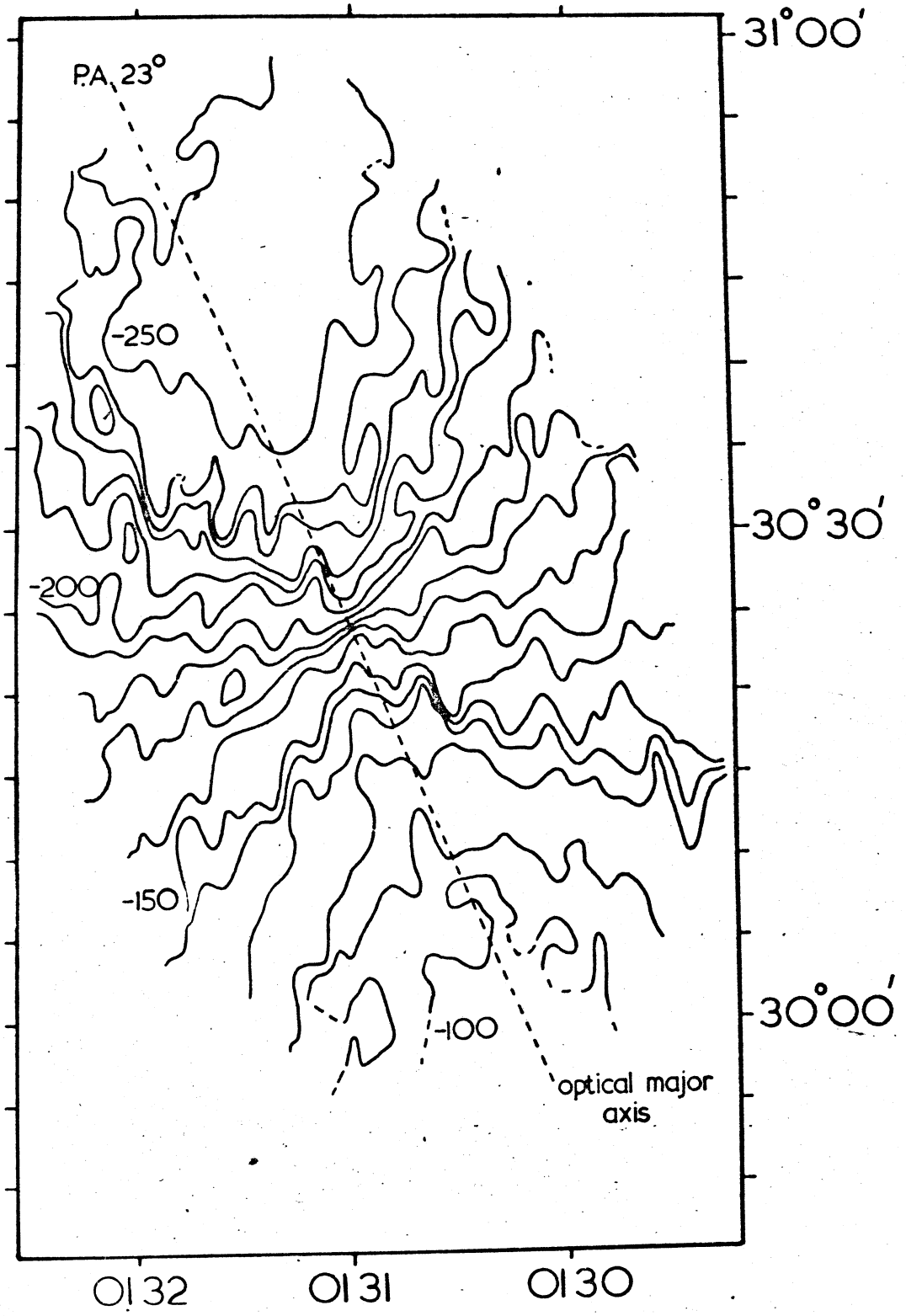

1000K kms^{-1} ≡ 1·8 × 10^{21} Hatoms cm^{-2}
K kms^{-1}
2000
1500
1000
500
HI
Optical
2
10'
4
20'
6
30'
8
40'
10
50'
12 kpc
60'

FIG 5


01h 32m
31m
30m
30° 30′
30° 30′
15′
30° 15′


P.A. 23°
-250
-200
-150
-100
optical major axis
31°00′
30°30′
30°00′
01 32
01 31
01 30

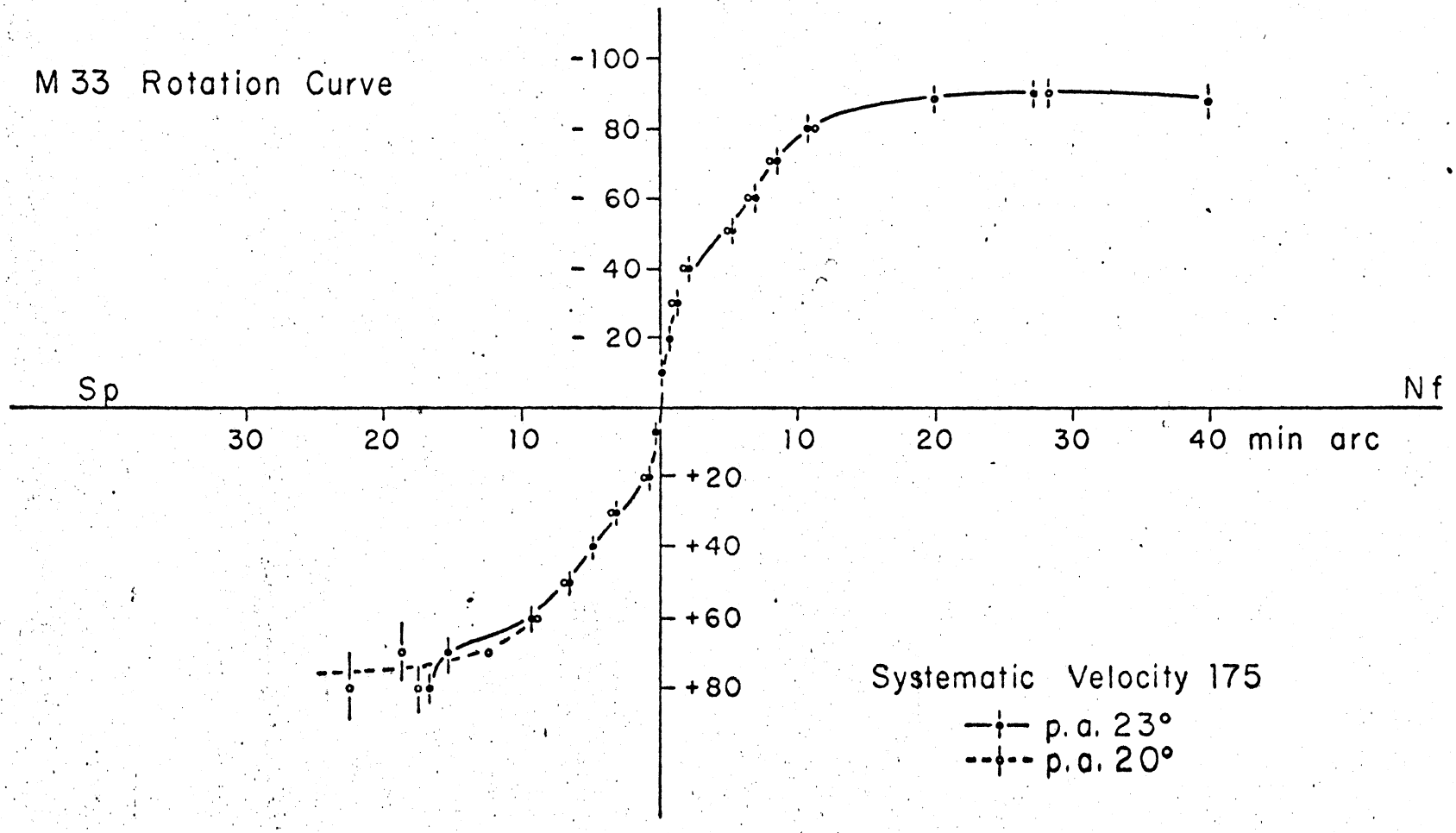

M 33 Rotation Curve
-100
- 80
- 60
- 40
- 20
Sp
Nf
30
20
10
10
20
30
40 min arc
+20
+40
+60
+80
Systematic Velocity 175
p. a. 23°
p. a. 20°

FIG 8

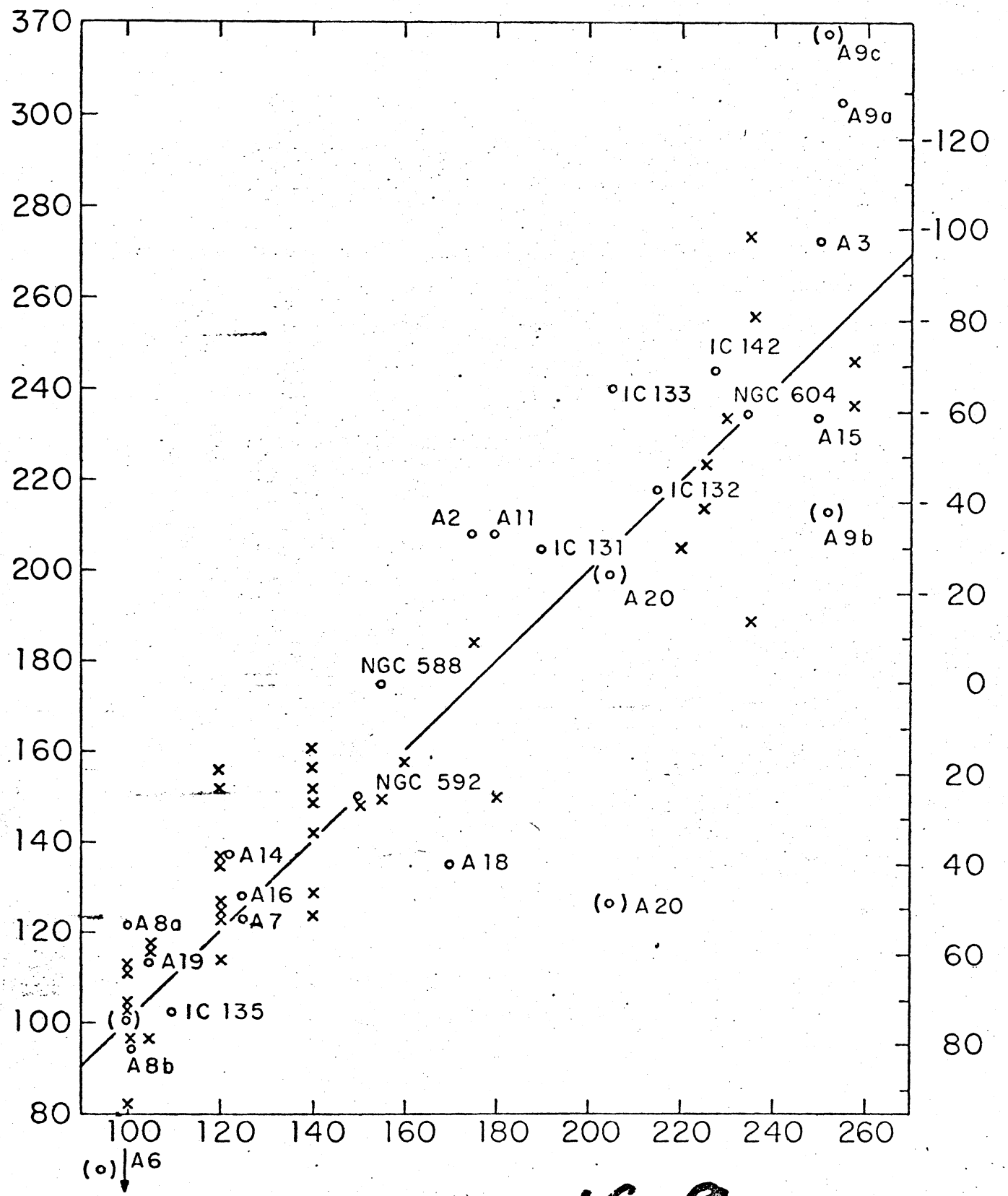

HII REGION VELOCITIES vs HI VELOCITIES
370
300
280
260
240
220
200
180
160
140
120
100
80
-120
-100
- 80
- 60
- 40
- 20
0
20
40
60
80
100
120
140
160
180
200
220
240
260
(o) A9c
A9a
A3
IC 142
IC 133
NGC 604
A15
IC 132
A2
A11
(o) A9b
IC 131
(o) A20
NGC 588
NGC 592
A14
A18
A16
A7
(o) A20
A8a
A19
IC 135
(o)
A8b
(o) A6

FIG 9

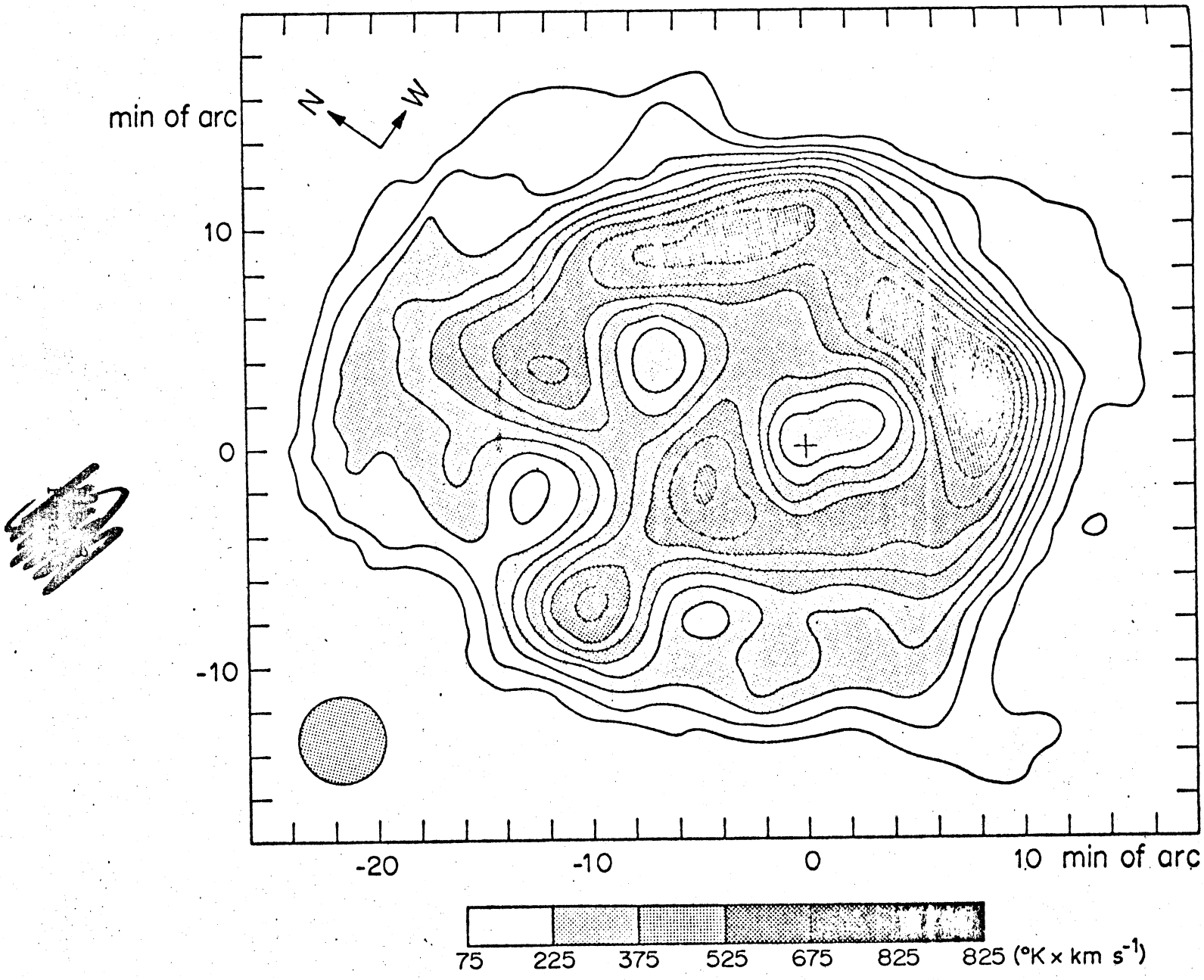

min of arc
N
W
10
0
-10
-20
-10
0
10 min of arc
75
225
375
525
675
825
825 (°K × km s⁻¹)

FIG 10

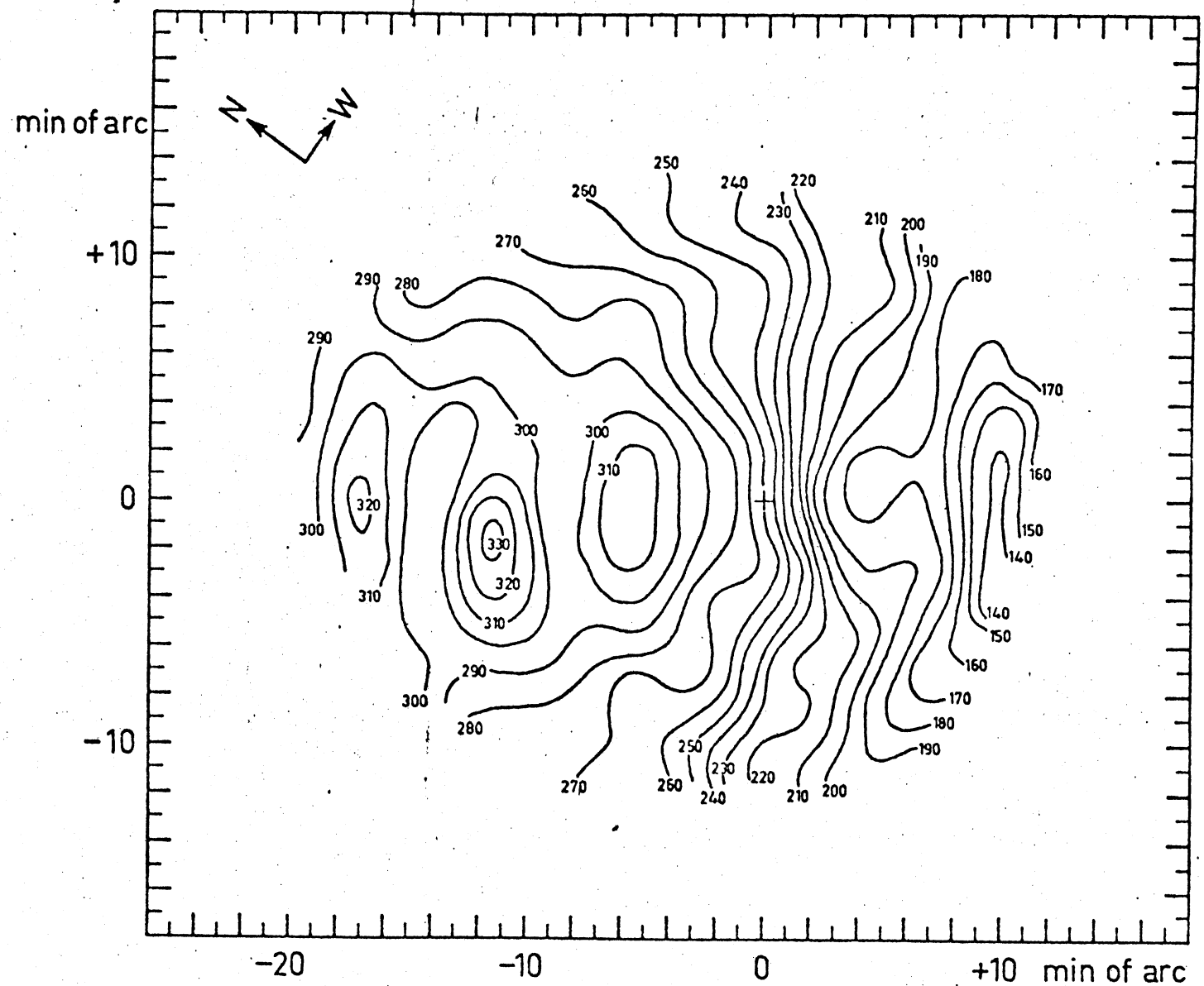
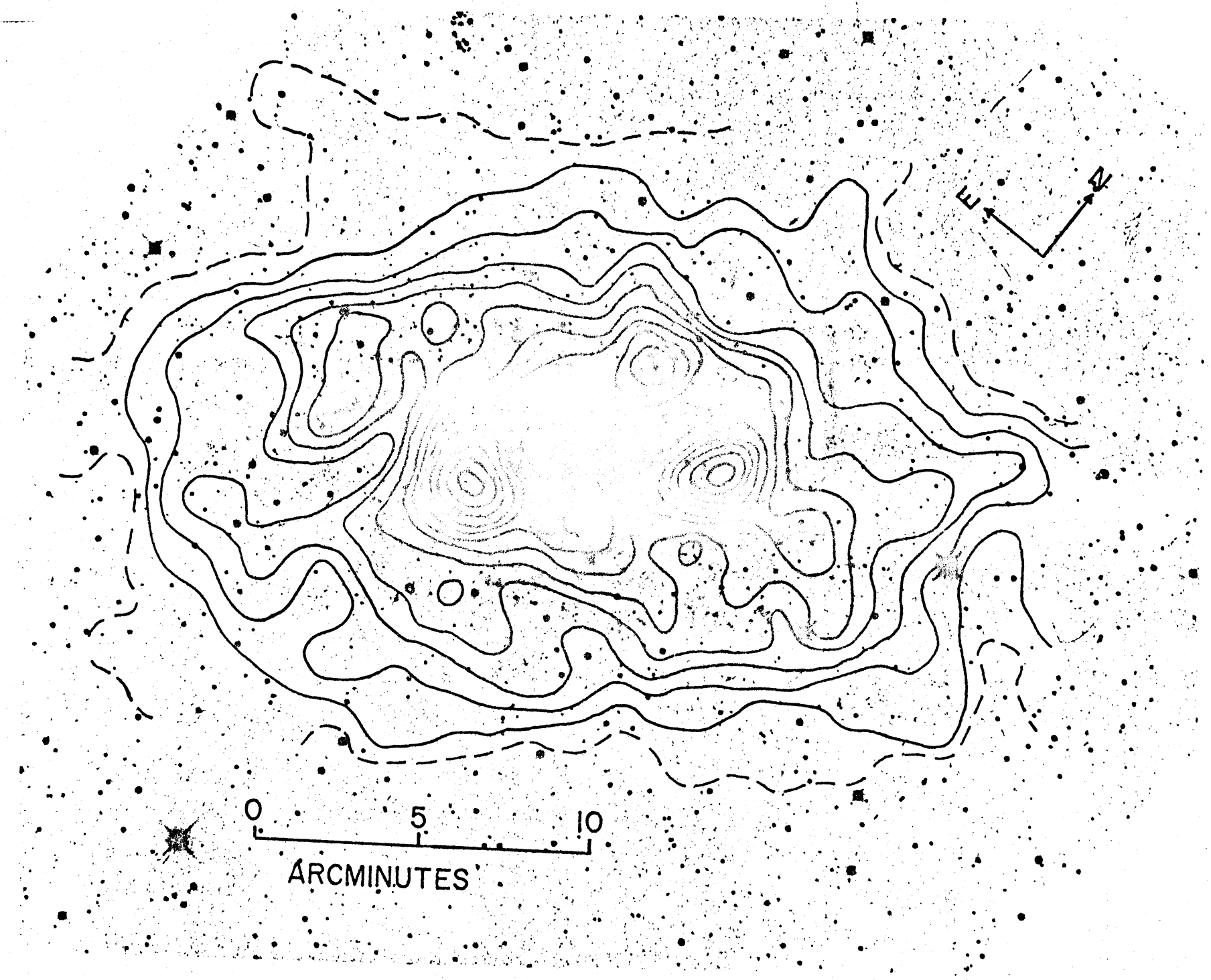
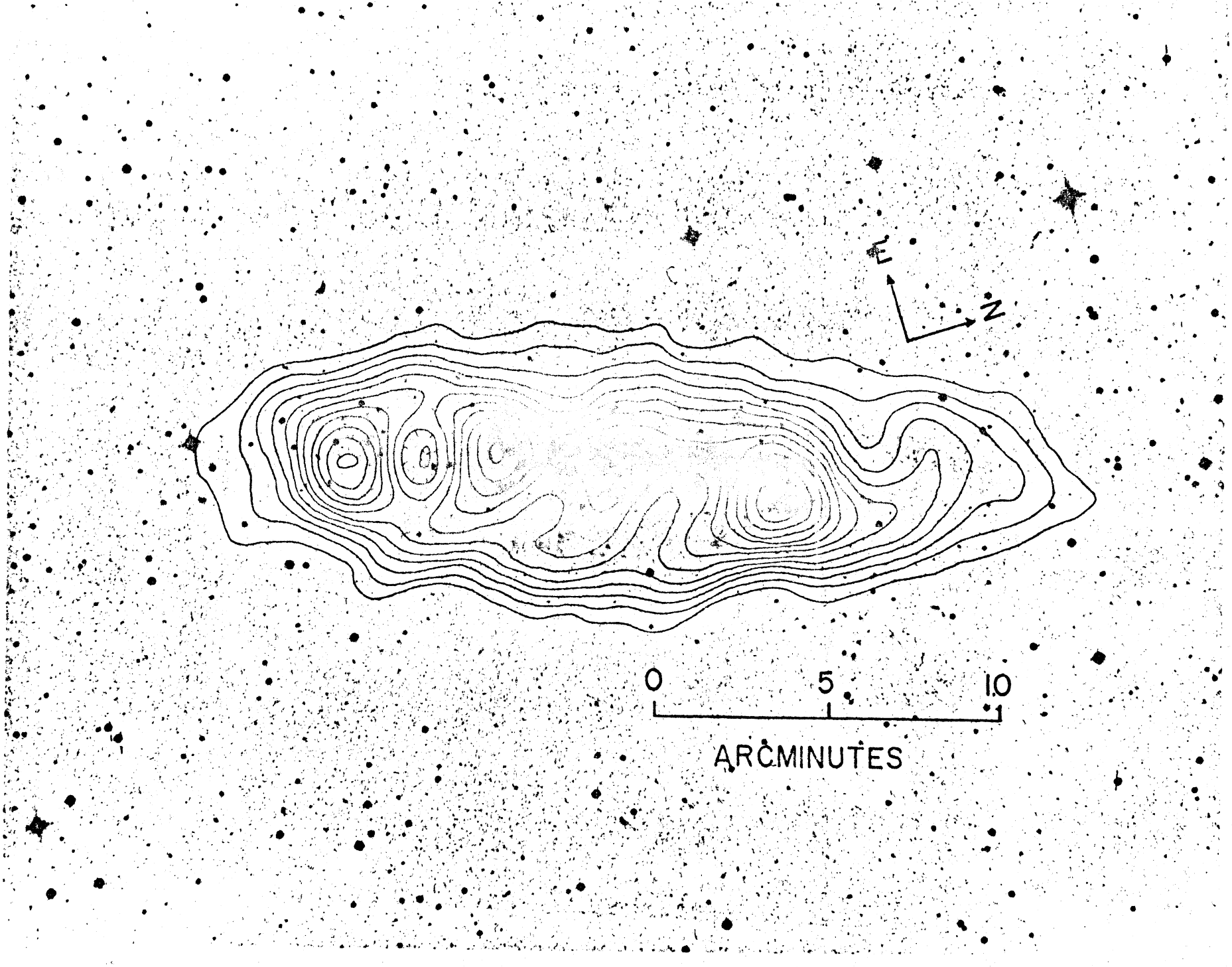
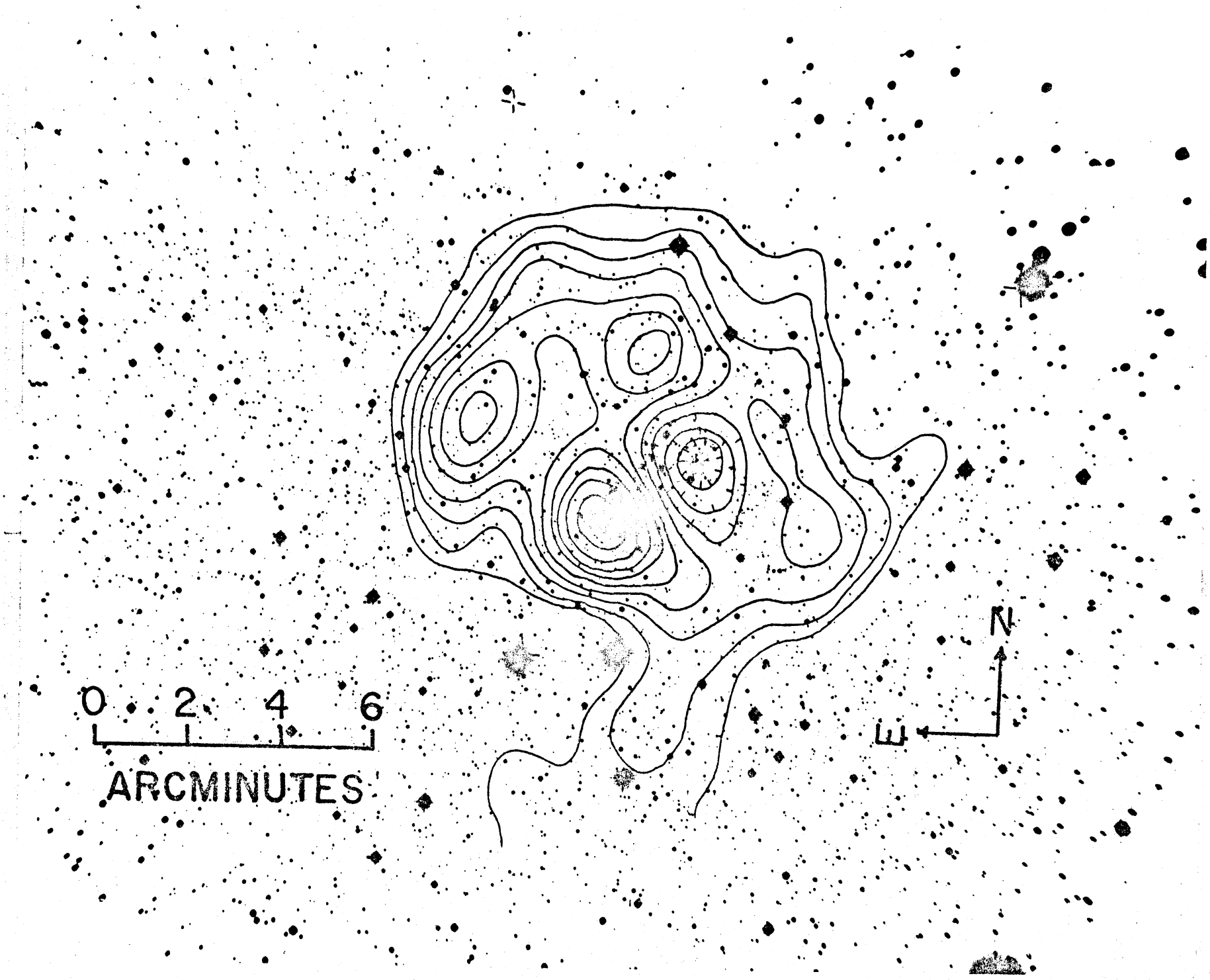

min of arc
N
W
+10
0
−10
−20
−10
0
+10 min of arc
250
260
240
220
230
210
200
270
190
180
290
280
290
170
300
300
310
160
320
300
150
330
140
320
310
140
310
150
290
160
300
170
280
180
270
250
260
240
220
210
200
190

FIG 11


E
N
0
5
10
ARCMINUTES


E
N
0
5
10
ARCMINUTES


0 2 4 6
ARCMINUTES
N
E